## PREFACE

The term thermoelasticity involves a large category of phenomena. It comprises the general theory of heat conduction, thermal stresses, and strains set up by thermal flow in elastic bodies and the reverse result of temperature distribution caused by the elastic deformation itself. It is well known that the latter is an important cause of internal damping in elastic bodies. The domain of science dealing with the mutual interactions of deformation and temperature fields is called as thermoelasticity. Initially, the investigations in this area were based on the "uncoupled theory of thermoelasticity" with the simplifying assumption that the influence of the strain and stresses on the temperature field may be neglected. However, the absence of any elasticity term in the heat conduction equation for uncoupled thermoelasticity appears to be unrealistic. Moreover, the parabolic type of the heat conduction equation results in an infinite velocity of thermal wave propagation, which also contradicts the actual physical phenomena. Introducing the strain-rate term in the uncoupled heat conduction equation, Biot (1956) extended the analysis to incorporate the coupling effects of temperature and strain fields in theory of thermoelasticity. However, although the first shortcoming was eliminated in this theory, there remained the parabolic type partial differential equation of heat conduction, which leads to the paradox of infinite velocity of the thermal wave. To eliminate this paradox, generalized thermoelasticity theory was developed subsequently. During the last three decades, non-classical theories involving finite speed of heat transportation in elastic solids have been developed. The various non-Fourier heat conduction models have been introduced with the purpose to eliminate the inherent drawback in classical heat conduction theory and/or classical coupled thermoelasticity theory. Hence,
$C_{S} \quad$ Specific heat at zero stress
$\lambda, \mu \quad$ Lame's elastic constants
$\alpha_{t} \quad$ Coefficient of linear thermal expansion
$C_{i j k l}$ Elasticity tensor
$\beta=(3 \lambda+2 \mu) \alpha_{t}$ Thermoelasticity constant
$\tau_{q} \quad$ Phase-lag of heat flux vector
$\tau_{T} \quad$ Phase-lag of temperature gradient
$\tau_{v} \quad$ Phase-lag of thermal displacement
$\delta_{i j} \quad$ Kronecker delta
$\delta($.$) \quad Dirac delta function$
$\nabla \quad$ Gradient operator
$\nabla^{2}=\Delta \quad$ Laplacian operator
Throughout the thesis, the subscripted comma notations are used to represent the partial derivatives with respect to the space variables.

The over-headed dots denote partial derivatives with respect to time variable, $t$.

Subscripts $i, j, k$ take the values 1, 2, 3 and summation is implied by index repetition.

## LIST OF SYMBOLS

| $u_{i}$ | Components of displacement vector |
| :---: | :---: |
| $e_{i j}$ | Components of strain tensor |
| $e_{i i}=e$ | Dilatation |
| $\sigma_{i j}$ | Components of stress tensor |
| $q_{i}$ | Components of heat flux vector |
| $\theta$ | Temperature above the reference temperature |
| $\theta_{0}$ | Reference temperature |
| $b_{i}$ | Components of the body force vector |
| $h_{i}$ | Components of the body force per unit mass |
| $r$ | External heat source |
| $\varpi$ | Heat source per unit mass |
| $\rho$ | Mass density of the material |
| $S$ | Entropy per unit mass |
| $S_{0}$ | Initial Entropy |
| $k$ | Thermal conductivity of the material |
| $k^{*}$ | Rate of thermal conductivity of the material |
| $c_{E}$ | Specific heat at constant strain and volume |

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