

## **LIST OF ABBREVIATIONS**

CLPT - Classical Laminated Plate Theory  
CZM- Cohesive Zone Model  
DOF- Degree of Freedom  
ERR- Energy Release Rate  
FE- Finite Element  
FEA- Finite Element Analysis  
FEM- Finite Element Method  
FG- Functionally Graded  
FGA- Functionally Graded Adhesive  
FMGB- Functionally Modulus Graded Bondline  
FRP- Fiber Reinforced Polymer  
FSDT - First-order Shear Deformation Theory  
HSDT - Higher-order Shear Deformation Theory  
LEFM- Linear Elastic Fracture Mechanics  
LSE- Least Square Estimation  
MCCI- Modified Crack Closure Integral  
MLM- Maximum Likelihood Method  
NA- Neutral Axis  
PMCE- Principle of Minimum Complementary Energy  
SERR- Strain Energy Released Rate  
VCCT- Virtual Crack Closure Technique

## LIST OF SYMBOLS

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$a_{ii}$  - Diagonal elastic compliance

$a_{ij}(i \neq j)$  - Off-diagonal compliance

$A$  - Crack surface created by the delamination opening

$c_E$  - Specific heat capacity

$C$  - Suffix for the notation of compression behaviour under bimodularity

$C_{ijkl}$  - Elastic stiffness

$D$  - Constant

$E_C$  - Modulus of elasticity for compression

$E_T$  - Modulus of elasticity for tension

$EI$  - Flexural rigidity of the beam

$E_1(I)$  - Lower bound Young Modulus

$E_2(I)$  - Upper bound Young Modulus

$f(x)$  - Probability density function of Weibull distribution

$f_i$  - Body force

$F$  - Sum of axial forces

$F_i$  - Force at delamination tip for the fracture mode  $i$

$G_I$  - First mode of SERR

$G_{II}$  - Second mode of SERR

$G_{III}$  - Third mode of SERR

$G_T$  - Total strain energy release rate

$G_c$  - Critical value of the energy release rate

$G_M, G_{MT}$ , and  $G_{TH}$  - SERR components due to mechanical, superposition of individual effects thermo-mechanical loading and only thermal loading, respectively

Gr/E- Graphite/Epoxy

$h_C$  - Height of the beam above neutral axis in compression region

$h_T$  - Height of the beam below neutral axis in tension region

$h$  – Total height of the beam

$I$  - Hydrostatic stress

$k_{ij}$  - Thermal conductivity coefficient

$l$  - Length of the projection of the deformed beam on x-axis

$L$  - Length of the beam without deformation

$L_b$  - Length of bond

$L_s$  - Length of substrate

$m$  - Shape Parameter

$M(x)$  - Bending moment

$ne$  - Total number of elements

$N$  - Ratio of length of bond and substrate

$N$  - Shape function for displacement

$N$  - Shape function for temperature

$P_f$  - Failure distribution of Weibull parameter

$q_i$  - Heat flux

$\bar{Q}$  - Flux

$R$  - Bimodular ratio

$s$  - Distance measured along the bond length

$t$  – Width of the beam

$T$  - Temperature change

$T$  - Suffix for the notation of tension behaviour under bimodularity

$T_0$  - Reference temperature

$\bar{T}_i$  - Surface traction

$u(x, z)$  - In-plane displacement

$u_i$  - Opening displacement for the fracture mode  $i$

$C$  - Poisson's ratio for compression

$T$  - Poisson's ratio for tension

$w$  - Lateral deflection

$W$  - Energy released by the propagation of a crack

$x_0$  - Scale parameter

$x$  - Location parameter

$z$  - Global coordinate

$\sigma_1$  and  $\sigma_2$  - Principal stress directions

$\alpha_{ij}$  - Thermal constant

$\theta$  - Fiber orientation

$\beta$  - Coefficient of thermal expansion

$T_i$  - Temperature gradient

$w_b(x)$  - Deflection of the beam due to bending stresses only

$w_m$  - Maximum deflection of the beam due to bending stresses

$(x, a)$  - Crack opening displacement between the upper and lower delaminated surfaces

$\sigma(x)$  - Stress at the crack front required to close the delaminated area

$u_z, u_x, u_y$  - Relative opening, sliding and tearing displacements, respectively

$\epsilon$  - Strain

$\gamma_{xz}$  - Transverse shear strain

$\sigma$  - Stress

$\sigma_{xx}, \sigma_{yy}$  and  $\sigma_{zz}$  - Normal stresses components of any stress tensor

$[\sigma_{zz}, \sigma_{zx}, \sigma_{zy}]$  - Interlaminar stress

$\rho$  - Mass density

$\eta$  - Entropy density