## CHAPTER 3

## SEISMIC ACCELERATION AMPLIFICATION FACTOR MODEL FOR NONSTRUCTURAL COMPONENTS IN RC FRAME STRUCTURES

In this chapter, the peak horizontal floor acceleration of non-structural components for low to moderate hazard level has been obtained. For this $2,4,6,8$ and 10 stories momentresisting RC frame models with low to moderate hazard level ( $0.01 \mathrm{~g}-0.31 \mathrm{~g}$ ) have been considered. For the analysis 32 ground motion data in the range of 0.01 g to $0.1 \mathrm{~g}, 29$ ground motion data in the range of 0.1 g to 0.2 g and 31 data in the range of 0.2 g to 0.31 g are considered using linear time history method. Based on analysis results, mathematical models are proposed to determine the absolute acceleration amplification factor.

### 3.1 BUILDING MODELS

This chapter deals with five RC moment-resisting frame models having a base to first storey height is 4 m and above floor height is 3.4 m respectively (Fig. 3.1). The sizes of the beams and columns are given in Table 3.1. Fundamental natural period of the structures lies within the range of 0.5 sec to 1.3 sec ., as obtained from linear time history analysis with the damping ratio 5\%.

Table 3.1 Size of beams and columns

| Beam | Size in mm |
| :---: | :---: |
| B1 | 300 x 400 |
| B2 | 300 x 450 |
| B3 | 450 x 500 |
| B4 | 450 x 600 |
| B5 | 450 x 650 |


| B6 | $450 \times 675$ |
| :---: | :---: |
| Column | Size in mm |
| $\mathrm{C}_{0}$ | 300 X 400 |
| C1 | $300 \times 450$ |
| C2 | $450 \times 500$ |
| C3 | $525 \times 550$ |
| C4 | $550 \times 600$ |
| C5 | $600 \times 700$ |
| C6 | $650 \times 850$ |



Figure 3.1 Moment resisting frame models (a) 2 (b) 4 (c) 6 (d) 8 and (e) 10 stories

### 3.2 CONSIDERED GROUND MOTIONS

In this study, 31-time history recorded data between 0.01 g to 0.1 g , 29 data between 0.1 g to 0.2 g and 31 data between 0.2 g to 0.31 g are considered. These ground motion data are obtained from the website of Strong ground motion site [140]. The list of the different recorded time history data is given in Table 3.2, 3.3, and 3.4 respectively.

Table 3.2 Time History Data for Peak Ground Acceleration between 0.01g to 0.1g

| Earthquake Station | PGA (g) | $\mathrm{T}_{\mathbf{t}}(\mathbf{s e c})$ | Tp(sec) |
| :---: | :---: | :---: | :---: |
| Chamoli (NW | 0.028 | 9.04 | 7.3 |
| Himalaya) |  |  |  |
| Uttarkashi | 0.021 | 21.32 | 1.62 |
| Uttarkashi | 0.017 | 21.34 | 3.2 |
| North East INDIA | 0.057 | 12.18 | 2.36 |
| North East INDIA | 0.058 | 12.18 | 4.86 |
| North East INDIA | 0.03 | 11.72 | 0.26 |
| North East INDIA | 0.022 | 11.72 | 2.28 |
| North East INDIA | 0.021 | 12.60 | 1.06 |
| Chamoli (NW | 0.022 | 14.98 | 1.24 |
| Himalaya) |  |  |  |
| Uttarkashi | 0.093 | 31.74 | 6.06 |
| Uttarkashi | 0.081 | 31.74 | 5.48 |
| Chamoli (NW | 0.052 | 24.96 | 4.38 |
| Himalaya) |  |  |  |
| North East INDIA | 0.039 | 9.52 | 1.06 |
| Chamoli (NW | 0.081 | 28.58 | 1.50 |
| Himalaya) |  |  |  |
| Chamoli (NW | 0.1 | 28.58 | 1.36 |
| Himalaya) |  |  |  |
| North East INDIA | 0.093 | 27.42 | 9.26 |
| North East INDIA | 0.077 | 27.42 | 9.78 |


| Chamoli (NW | 0.037 | 10.64 | 1.92 |
| :--- | :--- | :--- | :--- |
| Himalaya) |  |  |  |
| Chamoli (NW | 0.024 | 10.66 | 2.42 |
| Himalaya) |  |  |  |
| North East INDIA | 0.044 | 12.94 | 0.44 |
| North East INDIA | 0.031 | 12.94 | 1.08 |
| North East INDIA | 0.078 | 16.56 | 2.02 |
| North East INDIA | 0.086 | 16.58 | 1.82 |
| North East INDIA | 0.045 | 18.84 | 5.36 |
| North East INDIA | 0.043 | 18.88 | 4.14 |
| North East INDIA | 0.022 | 16.50 | 3.12 |
| Chamoli (NW | 0.071 | 25.04 | 5.62 |
| Himalaya) |  |  |  |
| North East INDIA | 0.084 | 27.36 | 7.68 |
| North East INDIA | 0.009 | 10.38 | 1.38 |
| Uttarkashi | 0.033 | 13.32 | 11.80 |
| Uttarkashi | 0.042 | 15.94 | 0.22 |

Table 3.3 Time History Data for Peak Ground Acceleration between 0.1 g to 0.2 g

| Earthquake | PGA (g) | $\mathbf{T}_{\mathbf{t}}(\mathbf{s e c})$ | $\mathbf{T}_{\mathbf{p}}(\mathbf{s e c})$ |
| :--- | :--- | :--- | :--- |
| Station |  |  |  |
| Chi-chi | 0.135 | 150 | 40.89 |
| Chi-chi | 0.142 | 146 | 45.58 |
| Chi-chi | 0.113 | 144 | 49.57 |


| Chi-chi | 0.150 | 150 | 48.52 |
| :---: | :---: | :---: | :---: |
| Chi-chi | 0.193 | 150 | 34 |
| Chi-chi | 0.124 | 150 | 34.77 |
| Chi-chi | 0.162 | 150 | 55.02 |
| Bhuj | 0.106 | 133.53 | 46.94 |
| Camarillo | 0.124 | 65 | 10.52 |
| Elizabath Lake | 0.114 | 60.01 | 10.87 |
| Northridge | 0.183 | 60.01 | 15.34 |
| Northridge | 0.106 | 60 | 11.38 |
| Costa Rica | 0.105 | 72 | 11.84 |
| Mammoth Lake | 0.121 | 44.66 | 10.14 |
| Mammoth Lake | 0.196 | 65 | 10.70 |
| Mammoth Lake | 0.163 | 65 | 3.14 |
| Coalinga | 0.133 | 60 | 11.56 |
| Coalinga | 0.192 | 65 | 6.94 |
| Pomona | 0.160 | 79 | 28.08 |
| Northridge | 0.120 | 65.02 | 7.44 |
| Chi-Chi | 0.146 | 120 | 36.82 |
| Mammoth Lakh | 0.155 | 67.78 | 2.44 |
| Costa Rica | 0.114 | 80 | 14.8 |
| Coalinga | 0.131 | 21.40 | 2.08 |
| Coalinga | 0.124 | 65 | 6.96 |
| Coalinga | 0.164 | 21.02 | 4.62 |
| Chi-Chi | 0.160 | 150 | 38.21 |
| Chi-Chi | 0.113 | 144 | 49.57 |


| Chi-Chi | 0.136 | 150 | 49.54 |
| :--- | :--- | :--- | :--- |

Table 3.4 Time History Data for Peak Ground Acceleration between 0.2 g to 0.3 g

| Earthquake | PGA $(\mathbf{g})$ | $\mathbf{T}_{\mathbf{t}}(\mathbf{s e c})$ | $\mathbf{T}_{\mathbf{p}}(\mathbf{s e c})$ |
| :--- | :--- | :--- | :--- |
| Station |  |  |  |
| Cartago | 0.262 | 80 | 15.58 |
| Chi-Chi | 0.263 | 68.05 | 15.39 |
| Baigao | 0.221 | 54.82 | 23.32 |
| Berlongfer | 0.300 | 119.7 | 29.58 |
| Batwari | 0.247 | 36.16 | 5.82 |
| Bokjan | 0.224 | 57.82 | 26.90 |
| Chi-Chi | 0.225 | 120 | 38.12 |
| Chi-Chi | 0.232 | 68.05 | 15.39 |
| Chi-Chi | 0.240 | 68.05 | 15.22 |
| Chi-Chi | 0.242 | 64 | 14.28 |
| Chi-Chi | 0.227 | 140.01 | 35.80 |
| Chi-Chi | 0.248 | 150 | 37.53 |
| Chi-Chi | 0.272 | 150 | 30.44 |
| Chi-Chi | 0.204 | 150 | 30.11 |
| Chi-Chi | 0.234 | 0.20 | 35.21 |
| Chi-Chi | 0.245 | 11.95 |  |
| Chi-Chi | 0.218 | 21.09 |  |
| Chi-Chi |  |  |  |
| Diphu |  |  |  |


| Chi-Chi | 0.282 | 105 | 12.82 |
| :--- | :--- | :--- | :--- |
| Chi-Chi | 0.233 | 48.01 | 8.05 |
| Chi-Chi | 0.223 | 124.08 | 10.12 |
| Chi-Chi | 0.254 | 60.05 | 10.61 |
| Chi-Chi | 0.223 | 62.00 | 19.62 |
| Uttarkashi | 0.310 | 23.92 | 5.9 |
| Lacc-nor | 0.221 | 60 | 8.92 |
| Whittier | 0.292 | 40 | 3.02 |
| Chalfant Vally | 0.231 | 40 | 4.00 |
| Landers | 0.273 | 40 | 25.98 |
| Northwest China | 0.273 | 60 | 6.14 |
| Northwest China | 0.233 | 45.02 | 5.5 |

In these tables, $T_{t}$ represents the total Recorded time period and $T_{p}$ represents the time of the peak acceleration. The ground acceleration to time period is shown in Figure 3.2.


Figure 3.2 $T_{t}$ and $T_{p}$ for Time history data of Bhuj Earthquake

### 3.3 FLOOR SPECTRAL ACCELERATION

Dynamic analysis is performed for each model, for selected accelerogram to record the horizontal acceleration time histories at a different level. The floor spectral acceleration is obtained by using the ground acceleration with $5 \%$ damping. The mean response spectral acceleration for each floor with the ground motion ranging between 0.2 g to 0.31 g is shown in Figure 3.3. These floor spectra give the acceleration demand on the nonstructural component, connected to the floor with a fundamental period T. It observed that as the height of the building increases, the amplification value decreases. For twostorey model, the amplification value is large, but it reduces as building height increases.




Figure 3.3 Mean floor spectral acceleration in the ground motion range 0.2 g to 0.3 g (a) 2 (b) 4 (c) 6 (d) 8 and (e) 10 stories.

### 3.4 DYNAMIC ANALYSIS AND COMPARISON OF THE MODELS

The lateral seismic force on the on structural components is described by ASCE/SEI 705 , depicted in chapter 2 . Based on this equation it was observed that the acceleration amplification factor on NSCs is maximum values 3 at the top of the building. However, wiser [86] gives the amplification formula (describe in chapter 2) based on the structural period of the building.

To compare these two models with the actual PFA/PGA model has been found by the linear time history analysis for all the building models using Etabs software [141], considering different ground motion data as given in Table 3.2, 3.3 and 3.4. The results of all the models are shown in Figures 3.4(a) to (e), when the ground acceleration ranges from 0.01 g to 0.1 g . These figures show the behaviour of the building in terms of peak floor amplification factor $(\Omega)$ for normalised height, defined as the ratio between the height of the floor and total height of the structure to the base.





Figure 3.4 Comparison between PFA/PGA with respect to normalize height when ground motion range 0.01 g to 0.1 g (a) 2 (b) 4 (c) 6 (d) 8 and (e) 10 stories It is found that when seismic ground motion is in the range of 0.01 g to 0.1 g , some of the $\Omega$ values are outside the equation proposed by the Drake and Wiser [134, 86]. The shapes of the $\Omega$ behave as nonlinear ( S shape) to normalise height.

For another case, when the ground motions observed in the range of 0.1 g to 0.2 g the amplification value is large at the top storey, are represented in Figure 3.5 (a) to (e). The two-storey model, amplification values are high and when the storey height increases and vice versa.






Figure 3.5 Comparisons between PFA/PGA with respect to normalised height when ground motion ranges are 0.1 g to 0.2 g (a) 2 (b) 4 (c) 6 (d) 8 and (e) 10 stories

In this case, the shapes of the $\Omega$ are not linear as defined by the Drake equation, with some of the $\Omega$ values lying outside the limits of formulas presented by Drake and J.Wiser.

When the ground motion is in the range of 0.2 g to 0.31 g , results are shown in Figures 3.6
(a) to (e)






Figure 3.6 Comparisons between PFA/PGA with respect to normalised height when ground motion ranges are 0.2 g to 0.31 g (a) 2 (b) 4 (c) 6 (d) 8 and (e) 10 stories The shapes of all acceleration amplification factor are nonlinear except when the natural period of the structure is low (less than 0.6 sec ), to the nominal height of the building. The above figures also represented that the formula proposed by the Drake and J. Wiser need some modification so that the actual values $(\Omega)$ lies below the required formula for the safe design of the structures.

### 3.5 PROPOSED MATHEMATICAL MODELS

From Figures 3.4, 3.5, and 3.6, it is observed that the amplification factor to the normalised height formed a nonlinear curve; having the avg. $\Omega$ as lower value at lower floor and higher values on the upper floor. These figures also showed that the relative average acceleration distribution depends upon the nature, flexibility, rigidity and the fundamental natural period of the buildings. Drake model [134] proposes that the absolute acceleration amplification factor $(\Omega)$ depends upon the normalise height and there is no
role of the fundamental natural period. Wiser [86] proposed that it should account the natural period of the structures.

Wiser [86] recommended the maximum structural period as 2.5 sec , but from the above figures, it observed that this value gives a lower amplification factor. To overcome this drawback, mathematical models are proposed in this study. In these models, no single maximum structural period is found to satisfy the actual amplification factor. To find the realistic amplification factor, two steps have been followed. Firstly, the ground acceleration has been divided into three ranges viz. $0.01-0.1 \mathrm{~g}, 0.1-0.2 \mathrm{~g}$ and $0.2-0.31 \mathrm{~g}$. Secondly, $\mathrm{T}_{\text {max }}$ is divided into three ranges in each acceleration range based on natural period. About 90 simulation studies have been carried out to arrive at the Tmax values. The proposed models based on observed results are given below:

$$
\begin{equation*}
\Omega=\frac{P F A}{P G A}=\left(1+\frac{\mathrm{Tmax}-\mathrm{T}}{T} \frac{z}{h}\right) \tag{3.1}
\end{equation*}
$$

When -

1) The ground motion acceleration ranges between 0.01 g to 0.1 g

$$
\begin{aligned}
\text { Tmax } & =2.5 \mathrm{sec} \quad \text { for } & & 0.0<\mathrm{T}<0.6 \mathrm{sec} \\
& =3.2 \mathrm{sec} \text { for } & & 0.6<\mathrm{T}<1.0 \mathrm{sec} \\
& =5.5 \mathrm{sec} \text { for } & & 1.0<\mathrm{T}<1.3 \mathrm{sec}
\end{aligned}
$$

2) Ground motion acceleration range between 0.1 g to 0.2 g

$$
\begin{aligned}
\text { Tmax } & =2.5 \mathrm{sec} \quad \text { for } & & 0<\mathrm{T}<0.6 \mathrm{sec} \\
& =4.3 \mathrm{sec} \text { for } & & 0.6<\mathrm{T}<1 \mathrm{sec} \\
& =5.5 \mathrm{sec} \quad \text { for } & & 1<\mathrm{T}<1.3 \mathrm{sec}
\end{aligned}
$$

3) Ground motion acceleration range between 0.2 g to 0.31 g

$$
\begin{aligned}
\text { Tmax } & =2.5 \mathrm{sec} \quad \text { for } & & 0<T<0.6 \mathrm{sec} \\
& =4.0 \mathrm{sec} \quad \text { for } & & 0.6<T<1 \mathrm{sec} \\
& =5.0 \mathrm{sec} \text { for } & & 1<\mathrm{T}<1.3 \mathrm{sec}
\end{aligned}
$$

Where Tmax = maximum structural period
$\mathrm{T}=$ Fundamental natural period of the buildings.

The final results after the investigation are represented in Figures 3.7,8, and 3.9 for the ground motion accelerations ranges between 0.01 g to $0.1 \mathrm{~g}, 0.1 \mathrm{~g}$ to 0.2 g and 0.2 g to 0.31 g respectively.




Figure 3.7 Comparison between PFA/PGA with respect to normalize height when ground motion range 0.01 g to 0.1 g (a) 2 (b) 4 (c) 6 (d) 8 and (e) 10 stories






Figure 3.8 Comparisons between PFA/PGA with respect to normalised height when ground motion ranges are 0.2 g to 0.31 g (a) 2 (b) 4 (c) 6 (d) 8 and (e) 10 stories






Figure 3.9 Comparisons between PFA/PGA with respect to normalised height when ground motion ranges are 0.2 g to 0.31 g (a) 2 (b) 4 (c) 6 (d) 8 and (e) 10 stories

Comparison of the proposed model with other modes is given in Table 3.5 and shown in
Figure 3.10.

Table 3.5 Number of $\Omega$ data exceed the actual $\Omega$ data given by different mathematical models

| Storey Models | Actual Data $\boldsymbol{\Omega}$ |  | Exceed $\Omega$ Data |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  | Drake Model | Wiser | Proposed Model |
|  |  | Model |  |  |
| 2 Storey | 276 | 43 | 5 | 5 |
| 4 Storey | 455 | 67 | 34 | 1 |
| 6 Storey | 637 | 86 | 132 | 5 |
| 8 Storey | 819 | 64 | 129 | 2 |
| 10 Storey | 1001 | 60 | 274 | 4 |



Figure 3.10 Percentage increases of $\Omega$ values with respect to actual $\Omega$ values It is observed, when the fundamental period of the building is less ( $\mathrm{T}<0.6 \mathrm{sec}$ ), the Wiser model gives better results, and when the natural periods are more, Drake model gives the better result. The floor amplification decreases when the height of the buildings increases. For the more realistic results when the natural period is more than 0.6 sec ., the proposed model performs better results.

### 3.6 CONCLUDING REMARKS

In this Chapter, analyses of different building models have been attempted considering the linear time history method and large numbers of ground motion data in the ranges of $0.01-0.1 \mathrm{~g}, 0.1-0.2 \mathrm{~g}$ and $0.2-0.31 \mathrm{~g}$. Mathematical models have been proposed to find the acceleration amplification factor, which is compared with the popular model due to Wiser and Drake. The following conclusions are drawn from the study:

- The Drake model does not consider the natural period of the structure, which plays a major role in an acceleration amplification factor. The proposed model consider the natural period between 0.1 to 1.3 sec .
- The Wiser model considers the fundamental natural period but accounts maximum structural period as 2.5 sec , which is not always true.
- The wiser model gives better results when the natural periods observed in the range of 0 to 0.6 sec .
- The values of structural period are not constant for all types of ground motion. It varies between 2.5 to 5.5 sec . with the range of the ground motion.
- Proposed mathematical models provide a realistic estimation of the acceleration amplification factor for low to moderate hazard levels.

