

## Appendix-A

### Calculation of film thickness and Hertzian diameter in case of four-ball tester

#### Film Thickness

Considering hard EHL,

$$\frac{h_{min}}{R_x} = 3.63 U^{0.68} G^{0.49} W^{-0.073} (1 - e^{-0.68k}) \quad \dots\dots(i)$$

$$\frac{h_{min}}{R_x} = 3.63 \left[ \frac{v\eta_0}{E'R_x} \right]^{0.68} [\xi E']^{0.49} \left[ \frac{w}{E'R_x^2} \right]^{-0.073} (1 - e^{-0.68k}) \quad \dots\dots(ii)$$

Where,  $h_{min}$ : film thickness;  $U, G$  and  $W$ : dimensionless speed, material and load parameter, respectively;  $k$ : ellipticity parameter ;  $R_x$ : effective radii in x-direction (i.e.  $\frac{1}{R_x} = \frac{1}{R_{ax}} + \frac{1}{R_{bx}}$ ) ;  $v$ : top ball speed;  $\eta_0$ : dynamic viscosity of oil (for castor oil 0.28 PaS);  $E'$ : effective young's modulus;  $\xi$ : pressure-viscosity coefficient;  $w$ : load (392 N in case of antiwear test as per ASTM standard)

$$v = Friction\ radius * \frac{2\pi * 1200}{60} = 0.00367 * \frac{2\pi * 1200}{60} = 0.46\ m/s$$

$$R_x = \frac{R_{ax} * R_{bx}}{R_{ax} + R_{bx}} = \frac{6.35 * 6.35}{6.35 + 6.35} = 3.175\ mm = 3.175 \times 10^{-3}\ m$$

$$R_x^2 = 10.08 \times 10^{-6}\ m^2$$

$$\xi = (0.6 + 0.965 \log_{10} \eta_0) \times 10^{-8} = (0.6 + 0.965 \log_{10} 0.28) \times 10^{-8} = 6.6507 \times 10^{-10}\ m^2/N$$

For similar balls young's modulus and poisson's ratio will same i.e.  $E_1=E_2= 204\ GPa$  and

$v_1=v_2= 0.3$ , thus

$$E' = \frac{2E_1E_2}{E_2(1-v_1^2)+E_1(1-v_2^2)} = 226.37 \times 10^9\ N/m^2$$

$k = 1$  (for similar balls in contact)

From equation (ii)

$$\frac{h_{min}}{R_x} = 3.63 \left[ \frac{0.46 * 0.28}{226.37 * 10^9 * 3.175 * 10^{-3}} \right]^{0.68} [6.6507 * 10^{-10} * 226.37 * 10^9]^{0.49} \left[ \frac{392}{226.37 * 10^9 * 10.08 * 10^{-6}} \right]^{-0.073} (1 - e^{-0.68})$$

$$\frac{h_{min}}{R_x} = 9.263 * 10^{-6}$$

$$h_{min} = 9.263 * 10^{-6} * 3.175 * 10^{-3} \text{ m} = 29.41 * 10^{-9} \text{ m} = 0.029 \mu\text{m}$$

Similarly, for epoxidized castor, epoxidized rapeseed, epoxidized sunflower, cottonseed, sesame, neemseed, olive, rapeseed and sunflower oil the film thickness was calculated and summarized in Table A.1:

Table A.1: Summary of calculated film thickness for modified and unmodified biolubricants.

Oil	Calculated film thickness ( $\mu\text{m}$ )
Castor	0.029
Epoxidized castor oil (ECO)	0.093
Epoxidized rapeseed oil (ERO)	0.0324
Epoxidized sunflower oil (ESO)	0.0257
Cottonseed	0.030
Sesame	0.031
Neemseed	0.023
Olive	0.032
Rapeseed	0.033
Sunflower	0.0319
CO+0.5%w/v CeO <sub>2</sub>	0.031
ECO+0.5%w/v CeO <sub>2</sub>	0.094

Since, the value of film thickness is less than 0.1  $\mu\text{m}$ , hence system is working in the boundary lubrication.

### **Hertzian Contact Diameter**

For sphere on sphere contact,

$$\text{The Hertzian contact radius "a"} = \sqrt[3]{\frac{3w(\frac{1-v_1^2}{E_1} + \frac{1-v_2^2}{E_2})}{4(\frac{1}{R_1} + \frac{1}{R_2})}}$$

Here,  $w = 392\text{N}$ ,  $E_1=E_2= 204 \text{ GPa}$  and  $v_1=v_2= 0.3$

$$a = \sqrt[3]{\frac{3*392*(\frac{1-0.3^2}{204*10^3} + \frac{1-0.3^2}{204*10^3})}{4(\frac{1}{6.35} + \frac{1}{6.35})}}$$

$$a = 0.2027 \text{ mm i.e. } 202.7 \mu\text{m}$$

$$\text{Hertzian contact diameter} = 2a = 2*202.7 = 405.4 \mu\text{m}$$



## Appendix-B

### Calculation of Friction Factor and Sommerfeld Number

Friction Factor is calculated by

$$f = \frac{\text{Torque}}{\text{Radius of the ball} * \text{Applied load}} = \frac{T}{r * w}$$

Sommerfeld Number calculated by

$$Z = \frac{\text{Viscosity} * \text{Sliding velocity} * \text{Ball radius}}{\text{Applied load}} = \frac{\eta_0 * v * r}{w}$$

Since, sliding velocity (v) = 0.46 m/s, w = 392 N, r = 6.35 mm

Table B.1: List of calculated Friction factor and Sommerfeld number for different oils.

Base oil	Viscosity (N-s/m <sup>2</sup> )	Torque (N-m)	Friction factor (f)	Sommerfeld number (z)
CO	0.28	0.138	0.055	2.08x10 <sup>-6</sup>
SO	0.076	0.108	0.043	0.5 x10 <sup>-6</sup>
RO	0.089	0.115	0.046	0.66 x10 <sup>-6</sup>
OO	0.087	0.135	0.054	0.65 x10 <sup>-6</sup>
NO	0.033	0.140	0.056	0.24 x10 <sup>-6</sup>
SSO	0.063	0.144	0.058	0.47 x10 <sup>-6</sup>
CTO	0.065	0.154	0.062	0.48 x10 <sup>-6</sup>
ERO	0.153	0.050	0.020	1.14 x10 <sup>-6</sup>
ESO	0.196	0.051	0.021	1.46 x10 <sup>-6</sup>
ECO	0.502	0.095	0.039	3.74 x10 <sup>-6</sup>
CO+0.5%w/v CeO <sub>2</sub>	0.285	0.101	0.041	2.12 x10 <sup>-6</sup>
ECO+0.5%w/v CeO <sub>2</sub>	0.505	0.132	0.053	3.76 x10 <sup>-6</sup>

Table B.1 and Figure B.1 have shown that the friction factor values were much higher than the limiting value i.e. 0.01 (dashed pink line) with the variation in Sommerfeld number, thus system may consider in boundary lubrication (Unsworth et al., 2005).

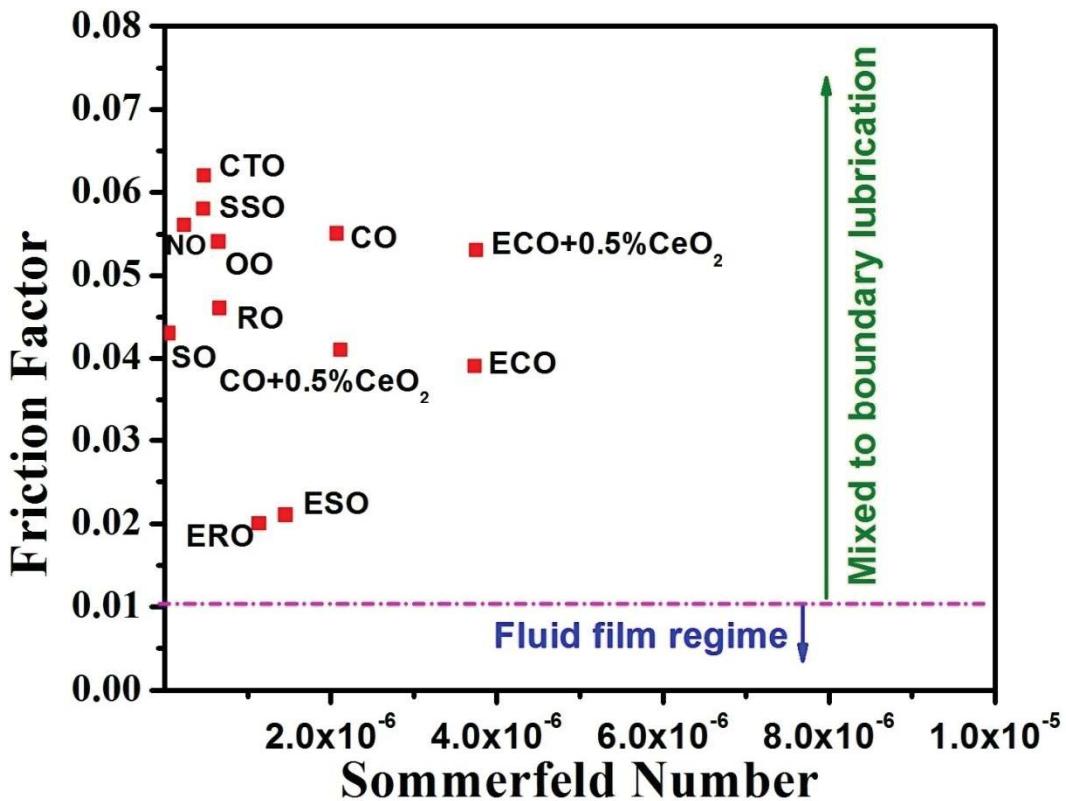
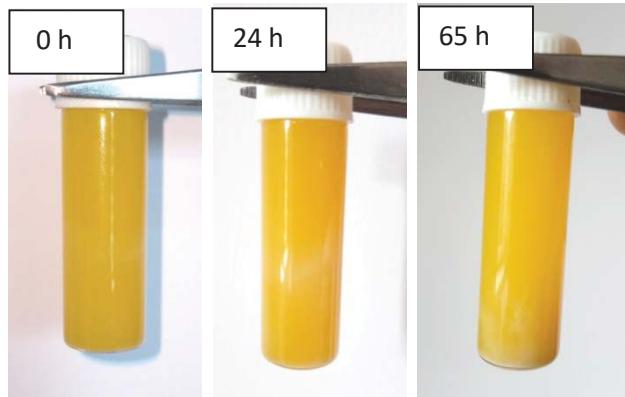


Figure B.1: Stribeck plot for all base oils and  $CeO_2$  based epoxidized and unmodified castor oil

## Appendix-C

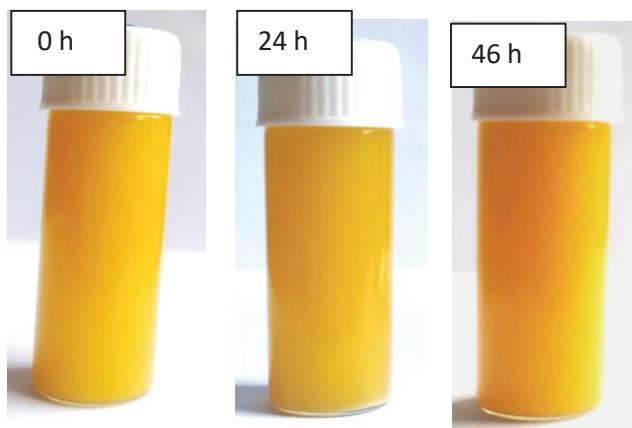
Suspension images of PTFE nanoparticles in different tested biolubricants with  
**0.25%w/v concentration**



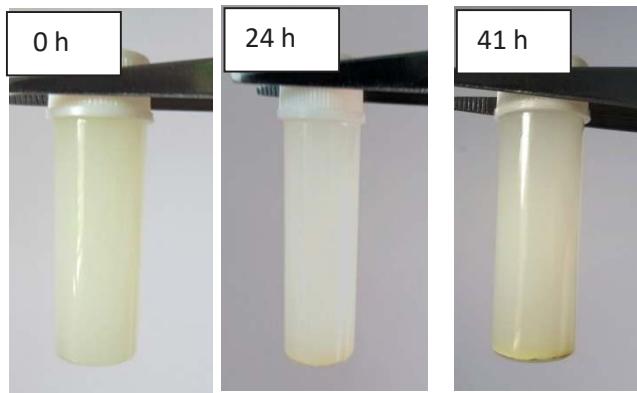
Rapeseed oil + PTFE



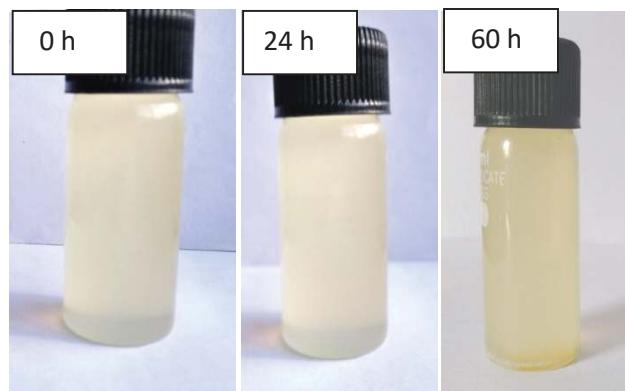
Cottonseed oil + PTFE



Sunflower oil + PTFE



Sesame oil + PTFE



Castor oil + PTFE