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- A. Singh and D. Ghosh. A globally convergent improved BFGS method for generalized Nash equilibrium problems. SeMA Journal. (A revision has been submitted)
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- 5. A. Singh, D. Ghosh. Improved nonmonotone adaptive trust region method based on interior point method to solve generalized Nash equilibrium problems. Computational Optimization and Applications. (Communicated Manuscript)