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It is further certified that the student has fulfilled all requirements of Comprehensive Examination, Candidacy, and SOTA for the award of Ph.D. Degree.

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I, **Anshul**, certify that the work embodied in this Ph.D. thesis is my own bonafide work carried out by me under the supervision of **Prof. Sanjay Kumar Singh** from **January 2017** to **March 2021** at **Department of Computer Science and Engineering**, Indian Institute of Technology (BHU) Varanasi. The matter embodied in this thesis has not been submitted for the award of any other degree/diploma. I declare that I have faithfully acknowledged and given credits to the research workers wherever their works have been cited in my work in this thesis. I further declare that I have not willfully copied any other's work, paragraphs, text, data, results, *etc.* reported in journals, books, magazines, reports, dissertations, theses, *etc.*, or available at websites and have not included them in this thesis and have not cited as my own work.

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Dedicated

to

My family

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# List of Symbols

$\mathbf{Symbol}$	Description
${\cal D}$	A training dataset with labeled instance
X	A time series
M	A number of instances in training set
T	Length of a complete time series
${\mathcal Y}$	A set of class labels
$X_t$	A incomplete time series of length $t$
$X_T$	A complete time series of length $T$
${\cal D}_t$	A truncated training dataset in which each $X \in \mathcal{R}^t$
X	A Multivariate Time series
h	A classifier
${\cal H}$	A set of classifiers
$C_{f}$	A cost function
$\alpha$	A balancing parameter between accuracy and earliness
K	Number of classes in training set
$\pi$	A vector of class probabilities for UTS
П	A matrix of class probabilities for MTS
$\hat{y}_t$	A predicted class label at time step $t$
$t^*$	A time step at which decision of class prediction is made.
δ	Confidence threshold
$\lambda$	A regularization parameter
$h_t^v$	A classifier at time step $t$ for $v^{th}$ variable of MTS

## Abbreviations

Abbreviation	Description
CD	Critical Difference
ECTS	Early Classification on Time Series
EDSC	Early Distinctive Shapelet Classification
ESR	Early Stopping Rule
ETMD	Early Transportation Mode Detection
GA	Genetic Algorithm
GP	Gaussian Process
ITS	Intelligent Transportation Systems
MCFEC	Mining Core Feature method for Early Classification
MPL	Minimum Predictive Length
MTS	Multivariate Time Series
PC	Probabilistic Classifier
PSO	Particle Swarm Optimization
QDA	Quadratic Discriminant Analysis
REACT	Reliable EArly ClassificaTion
RNN	Recurrent Neural Network
SGD	Stochastic Gradient Descent
SHL	Sussex-Huawei Locomotion and Transportation
SVM	Support Vector Machine
TMD	Transportation Mode Detection
TSC	Time Series Classification
UTS	Univariate Time Series

## Preface

Early classification of time series is valuable in many real-world applications where data is generated over time. The aim of early classification is to predict the class label of incoming time series as early as possible before observing its complete sequence. In general, whenever early prediction time improves, the prediction accuracy decreases. In other words, one can achieve better accuracy by waiting for more data points in the series, but it will delay the response time. In time-sensitive applications, it is worth sacrificing some classification accuracy in favour of early predictions, preferably early enough for taking actionable decisions. Thus, there exists a trade-off between earliness and accuracy. However, existing approaches do not consider trade-off optimization well in their decision criteria.

Time Series Classification (TSC) is one of the major research areas that developed over the past few years, mainly due to its practical applicability in various domains such as agriculture, healthcare, medicine, finance, and industries. The main objective of TSC is to maximize prediction accuracy. In contrast, an early classification of time series has two conflicting objectives, i.e., accuracy and earliness. Nowadays, the early classification of time series attracts researchers more due to its useful applications in various domains such as early disease prediction, early gas leakage prediction, drought prediction, etc.

This thesis focuses on the problem of early classification of time series by learning optimal decision criteria. The problem of early classification has been identified as the composition of two sub-problems. The first one is to design the early classifier that can label the incomplete time series. The second is to define the decision criteria that can estimate the right time for making an online decision. Initially, we propose an early classification model for Univariate Time Series (UTS), which relies on two factors (i) a set of probabilistic classifier and (ii) a confidence threshold. The confidence threshold ensures the reliability of class prediction defined by measuring the uncertainty in predicted output. In this method, decision policy is more inclined toward accuracy and does not take trade-off optimization into consideration. In this regard, a further optimization-based approach has been adapted for early classification and defines the early stopping rules for optimal decision making, which have been learned through optimization between accuracy and earliness simultaneously.

Furthermore, this optimization-based approach has been extended for Multivariate Time Series (MTS), which is more challenging than UTS because of the multiple variables involved in decision making. An ensemble-based system has been designed to label the incomplete MTS, and collective output from all the variables has been utilized for decision making. These proposed methods are highly effective for small training data sets, but feature transformation is required for training the classifiers. Finally, a deep learning-based hybrid classifier has been proposed that can capture the temporal information from the raw sensory data effectively to perform the classification task. Moreover, the optimal confidence threshold has been defined by balancing the trade-off between accuracy and earliness. The proposed approaches have been evaluated on publicly available datasets and they demonstrated effective solutions for early classification on time series.