

# CONTENTS

---

---

<b>LIST OF FIGURES .....</b>	<b>XVII</b>
<b>LIST OF TABLES .....</b>	<b>XXII</b>
<b>ABBREVIATIONS .....</b>	<b>XXIII</b>
<b>LIST OF SYMBOLS .....</b>	<b>XXV</b>
<b>PREFACE.....</b>	<b>XXXI</b>

## **CHAPTER 1: INTRODUCTION AND LITERATURE REVIEW .....***Error! Bookmark not defined.*

1.1	Background and Motivation .....	3
1.2.	Classification of Microwave Devices .....	6
1.3.	Gyrotron Oscillator .....	8
1.3.1.	Dispersion Relation.....	9
1.3.2	CRM Interaction Mechanism .....	10
1.3.3.	Operating Principle .....	14
1.3.4.	Schematic and Working .....	15
1.4.	Dynamic Nuclear Polarizatio and Nuclear Magnetic Resonance .....	<b>Error!</b>
	<b>Bookmark not defined.</b>	
1.5.	DNP / NMR Gyrotrons .....	18
1.6.	Current Effort .....	<b>Error! Bookmark not defined.</b> 1
1.7.	Plan and Scope.....	<b>Error! Bookmark not defined.</b> 3

## **CHAPTER 2: MULTIMODE THEORY OF GYROTRON OSCILLATORS..... **27****

2.1.	Introduction .....	29
2.2.	Multimode Theory.....	32
2.3.	Design Methodology and Limiting Constraints .....	43
2.3.1	Mode Selection .....	44
2.3.2	Cavity losses .....	44
2.3.3	Voltage depression and Limiting Current .....	46
2.3.4	Start Oscillation Current.....	48

2.4.	Results and Discussion .....	52
2.4.1	Design procedure of 260 GHz Gyrotron .....	53
2.4.1.a	RF Interaction Structure .....	53
2.4.1.b	Cavity Field Profile .....	53
2.4.1.c	Coupling Coefficient .....	55
2.4.2	Numerical Benchmarking.....	56
2.5.	Conclusion.....	57

**CHAPTER 3: PIC SIMULATION, MAGNETIC AND THERMAL TUNING STUDIES OF MILLIMETER-WAVE GYROTRON.....59**

3.1.	Introduction .....	61
3.2.	Descriptions of PIC Simulation .....	63
3.3.	PIC Simulation of 260 GHz Gyrotron Cavity.....	66
3.3.1	Modelling and Beam-wave Interaction Process .....	64
3.3.2	PIC Simulation Results .....	67
3.4.	Thermal Study of Gyrotron cavity .....	69
3.5.	Continuous Frequency Tuning of Millimeter-Wave Gyrotron .....	71
3.5.1	Magnetic Tuning Scheme.....	74
3.5.2	Thermal Tuning Scheme .....	77
3.6.	Output System of the Gyrotron.....	80
3.6.1	RF Output Window.....	80
3.6.2	Electron Beam Depressed Collector .....	82
3.7.	Conclusion.....	83

**CHAPTER 4: DESIGN AND SIMULATION STUDIES OF MILLIMETER-WAVE GYROTRON USING METAL PBG RF CAVITY .....85**

4.1.	Introduction .....	87
4.2.	Design Methodology of the PBG Cavity.....	89
4.2.1	Dispersion Relation and Global Band Diagram .....	89
4.2.2	Mode Analysis.....	90

4.2.3	PBG Cavity Design .....	92
4.3.	Cold Analysis of PBG Cavity.....	93
4.3.1	Time Domain Analysis.....	93
4.3.2	Eigenmode Analysis .....	94
4.4.	Calculation of Quality Factor.....	96
4.5.	Design and PIC Simulation of PBG Gyrotron .....	97
4.5.1	Modelling of PBG Gyrotron.....	97
4.5.2	PIC Simulation of PBG Gyrotron .....	101
4.6.	Tuneability of PBG Gyrotron .....	102
4.7.	Thermal and Structural Analysis of PBG Cavity .....	104
4.8.	Conclusion .....	106

**CHAPTER 5: DESIGN AND SIMULATION STUDIES OF GYROTRON USING MULTI-SECTION SLIGHTLY TAPERED RF CAVITY ..... 109**

5.1.	Introduction.....	111
5.2.	Design of Multi-Section Cavity .....	112
5.2.1	Diffractive Quality Factor and Resonating Frequency....	112
	<b>Error!</b> <b>Bookmark not defined.</b>	
5.2.2	Cavity Field Profile.....	116
5.2.3	Effective Length, Total Quality Factor and Start Oscillation Current .....	119
5.3.	PIC Simulation of Multi-Section Cavity Gyrotron .....	121
5.4.	Thermal and Static Structural Analysis.....	122
5.5.	Tuneability of Multi-Section cavity Gyrotron.....	124
5.5.1	Magnetic Tuning Scheme .....	124
5.5.2	Thermal Tuning Scheme .....	127
5.6.	Discussion on Fabrication Aspects of the Cavity .....	128
5.7.	Conclusion.....	129

**CHAPTER 6: SIMULATION INVESTIGATIONS OF SECOND HARMONIC SUBMILLIMETER-WAVE GYROTRON ..... 131**

6.1.	Introduction .....	133
6.2.	Modelling of Gyrotron .....	<b>Error! Bookmark not defined.</b> 134
6.2.1	Magnetron Injection Gun .....	134
6.2.2	Cavity Field Profile.....	135
6.2.3	Coupling Coefficient and Start Oscillation Current.....	136
6.3.	Multimode Simulation of Submillimeter-Wave Gyrotron.....	137
6.4.	Thermal and Static Structural Analysis.....	138
6.5.	Tuneability of Submillimeter-Wave Gyrotron.....	141
6.5.1	Magnetic Tuning Scheme.....	141
6.5.2	Thermal Tuning Scheme .....	143
6.6.	Output System .....	146
6.6.1	RF Window .....	146
6.6.2	Output Collector .....	146
6.7.	Conclusion.....	148
<b>CHAPTER 7:</b>	<b>SUMMARY, CONCLUSION AND FUTURE SCOPE.....</b>	<b>149</b>
7.1.	Summary and Conclusion .....	151
7.2.	Limitations of the Present Work and Scope for Further Studies. ....	<b>Error!</b> <b>Bookmark not defined.</b> 156
<i>References</i> .....		157
<i>Author's relevant publications</i> .....		171

## **LIST OF FIGURES**

---

<b>Figure 1.1</b>	Comparison of average power versus frequency for various types of devices	4
<b>Figure 1.2</b>	Classification chart of vacuum electron devices	6
<b>Figure 1.3</b>	Dispersion diagram of gyrotron oscillator	10
<b>Figure 1.4</b>	RF electric field of TE <sub>0n</sub> mode with electron beamlets	10
<b>Figure 1.5</b>	Illustration of phase bunching phenomenon in an annular electron beam (a) random distribution, and (b) phase bunched electrons in their cyclotron orbits	12
<b>Figure 1.6</b>	Time evolution of electrons phase distribution (shown as  ) in the Larmor orbit	
<b>Figure 1.7</b>	Schematic arrangement of a gyrotron oscillator	13
<b>Figure 2.1</b>	The arrangement of electrons in the Larmor orbit with cylindrical coordinates and Cartesian coordinates	15
<b>Figure 2.2</b>	Radial profile and cavity field profile along the axial length of the cavity	32
<b>Figure 2.3</b>	(a) Relation between the coupling coefficient and normalized beam radius, and (b) SOC of TE <sub>7,2</sub> mode and competing modes	54
<b>Figure 2.4</b>	The output power of operating TE <sub>7,2</sub> mode and other competing modes using Multimode code (For beam parameters $V_b = 15.5$ keV, $I_b = 0.1$ A, $B_o = 9.52$ T and $\alpha = 1.12$ )	55
<b>Figure 3.1</b>	Boundary conditions implementations around the RF interaction cavity	57
<b>Figure 3.2</b>	CST model of the gyrotron cavity	65
<b>Figure 3.3</b>	Particle preview of electron beam at the input side and at the output side	66
<b>Figure 3.4</b>	(a) Particle energy of the electron beam (b) fraction of the particle energy	67
<b>Figure 3.5</b>	(a) Amplitude of port signals, (b) power of TE <sub>7,2</sub> mode, (c) frequency spectrum of the port signal of TE <sub>7,2</sub> mode and (d) theoretically calculated power	68
<b>Figure 3.6</b>	(a) ANSYS model of the RF interaction cavity, (b) Heat transfer coefficient with a hydraulic diameter for different water flow rates in the grooves	69
<b>Figure 3.7</b>	(a) The temperature and deformation of the inner surface of straight section of the cavity, (b) the resonating frequency with respective water flow rate and shifting in resonating frequency at corresponding water flow rate at 290K	72
<b>Figure 3.8</b>	(a) The temperature distribution in the cavity, and (b) the total deformation of the cavity at coolant temperature 290K	72
<b>Figure 3.9</b>	The smooth transition between the $q = 1$ –like mode and $q = 2$ – like mode	73
<b>Figure 3.10</b>	SOC for axial mode number $q = 1 - 6$	74

<b>Figure 3.11</b>	The cavity field profile for axial mode number $q = 1 - 6$	76
<b>Figure 3.12</b>	The spectrum of the E-field monitors at the frequency (a) 260.46 GHz, (b) 260.69 GHz, (c) 261.05 GHz, and (d) 261.57 GHz	76
<b>Figure 3.13</b>	(a) Power Vs magnetic field (b) resonating frequency with the respective magnetic field (beam parameters are 15.5 kV, 100 mA, $\alpha = 1.12$ , and total velocity spread is 2%)	77
<b>Figure 3.14</b>	Power Vs magnetic field for various velocity spread (beam parameters are 15.5 kV, 100mA, and $\alpha = 1.12$ )	78
<b>Figure 3.15</b>	(a) Deformation distribution in the cavity and (b) The total quality factor ( $Q_T$ ) and ohmic quality factor ( $Q_\Omega$ ) at the respective temperature	78
<b>Figure 3.16</b>	(a) Power versus magnetic field for thermal tuning and magnetic tuning and (b) Frequency versus magnetic field for thermal tuning and magnetic tuning	80
<b>Figure 3.17</b>	Transmission and reflection characteristics of single disk Sapphire window at $\epsilon_r = 9.394$ and loss tangent $\tan(\delta) = 4.5 \times 10^{-4}$	81
<b>Figure 3.18</b>	The temperature distribution of the collector	83
<b>Figure 4.1</b>	Metal PBG structures (a) unit cell in the triangular lattice (b) reciprocal lattice and Brillouin's zone (shaded area)	90
<b>Figure 4.2</b>	(a) Plot of normalized frequency verses peaks at certain location in the unit cell, (b) dispersion curve at $r/a = 0.40$	90
<b>Figure 4.3</b>	Global band-gap of the PBG cavity, where ● denotes the operating point	90
<b>Figure 4.4</b>	The relation between $r/a$ and $fa/c$ of different modes those confines in the defect after removing nineteen rods and shaded regions are the global bandgap	92
<b>Figure 4.5</b>	(a) Model of PBG cavity (b) S-Parameters of $TE_{7,2}$ -like mode	93
<b>Figure 4.6</b>	Boundary condition around the PBG cavity in the Eigenmode analysis	95
<b>Figure 4.7</b>	(a) E- field pattern of the $TE_{7,2}$ mode in the conventional cavity and (b) $TE_{7,2}$ -like mode in the PBG cavity	95
<b>Figure 4.8</b>	(a) Spectrum of the probed E-field, and (b) Stored energy decay	96
<b>Figure 4.9</b>	(a) Model of PBG gyrotron (b) normalized field profile with the radius of the gyrotron cavity	98
<b>Figure 4.10</b>	Confined frequencies in the PBG cavity with respective cells per wavelength	99
<b>Figure 4.11</b>	(a) Relation between coupling coefficient and normalized beam radius (b) SOC of $TE_{7,2,1}$ mode and its nearby competing modes	99
<b>Figure 4.12</b>	(a) Amplitudes of port signals (b) power in $TE_{7,2,1}$ -like mode (c) frequency spectrum of the port signal of $TE_{7,2,1}$ -like mode (d) output power through Multimode time-dependent calculation. The beam parameters 15.5kV, 140mA, and $\alpha = 1.7$ with 2% velocity spread are considered in the PIC simulation and Multimode simulation	100

<b>Figure 4.13</b>	Axial electric field variation inside the cavity in absence of electron beam, for (a) $q = 1$ (b) $q = 2$ (c) $q = 3$ and (d) $q = 4$	103
<b>Figure 4.14</b>	Comparison of (a) power and (b) frequency / bandwidth of PBG gyrotron and conventional gyrotron over magnetic field using PIC simulation and Multimode code (PBG gyrotron) for $V_0 = 15.5$ keV, $I_0 = 140$ mA, and $\alpha = 1.7$ with 2 % velocity spread.	104
<b>Figure 4.15</b>	Temperature (a) profile in the PBG cavity and (b) distribution in the radial direction	106
<b>Figure 4.16</b>	Deformation of rods in the PBG cavity (a) inner layer (b) middle layer (c) outer layer (d) E-field pattern resonating at 260.324 GHz	106
<b>Figure 5.1</b>	(a) Resonant frequency $V_s$ taper angle $\theta_2$ , and (b) diffractive Q factor $V_s$ taper angle $\theta_2$ for different taper length $L_2$ of TE <sub>7,2,1</sub> mode [for $L_4 = 0$ , $\theta_4 = 0$ , $\theta_3 = 0$ , $L_1 = 10$ mm, $L_3 = 22$ mm, $L_5 = 10$ mm, and $L_6 = 63$ mm]	113
<b>Figure 5.2</b>	(a) Resonant frequency $V_s$ taper angle $\theta_4$ , and (b) diffractive Q factor $V_s$ taper angle $\theta_4$ for different taper length $L_4$ of TE <sub>7,2,1</sub> mode [for $L_2 = 0$ , $\theta_2 = 0$ , $\theta_3 = 0$ , $L_1 = 10$ mm, $L_3 = 22$ mm, $L_5 = 10$ mm, and $L_6 = 63$ mm]	113
<b>Figure 5.3</b>	Resonant frequency and diffractive Q factor $Q_d$ Vs taper angle $\theta_3$ of TE <sub>7,2,1</sub> mode [for $L_2 = 0$ , $\theta_2 = 0$ , $L_4 = 0$ , $\theta_4 = 0$ , $L_1 = 10$ mm, $L_3 = 22$ mm, $L_5 = 10$ mm, and $L_6 = 63$ mm]	113
<b>Figure 5.4</b>	Cavity field profile and radial profile of the multi-section cavity	116
<b>Figure 5.5</b>	Cavity field profile for TE <sub>7,2,q</sub> mode (a) $q = 2$ , (b) $q = 3$ , (c) $q = 4$ , (d) $q = 5$ , (e) $q = 6$ , (f) $q = 7$ , (g) $q = 8$ , and (e) $q = 9$	117
<b>Figure 5.6</b>	Comparison of the cavity field profile between the three-section cavity and multi-section cavity	118
<b>Figure 5.7</b>	Cavity field profile for (a) $q = 1$ , (b) $q = 2$ , (c) $q = 3$ , (d) $q = 4$ , (e) $q = 5$ , (f) $q = 6$ , (g) $q = 7$ , (h) $q = 8$ , and (i) $q = 9$ [for $\theta_2 = 0$ , $\theta_3 = 0$ , $\theta_4 = 0$ , $L_2 = 12$ mm, $L_4 = 12$ mm, $L_1 = 10$ mm, $L_3 = 22$ mm, $L_5 = 10$ mm, and $L_6 = 63$ mm]	119
<b>Figure 5.8</b>	SOC for the TE <sub>7,2,q</sub> mode ( $q = 1$ to 9)	120
<b>Figure 5.9</b>	(a) Amplitudes of port signals (b) power in TE <sub>7,2</sub> mode (c) frequency spectrum of the port signal of TE <sub>7,2</sub> mode (d) output power through Multimode time-dependent calculation. The beam parameters 15.5kV, 100 mA, and $\alpha = 1.12$ with a 2% velocity spread are considered in the PIC simulation and Multimode simulation	122
<b>Figure 5.10</b>	(a) Temperature distribution of cavity, (b) deformation distribution of cavity, and (c) temperature profile of the internal surface of the cavity and field profile of the cavity	123
<b>Figure 5.11</b>	The start oscillation current of TE <sub>7,2,1</sub> mode with other competing modes field (for the beam parameters 15.5 kV, 100 mA, $\alpha = 1.12$ )	125
<b>Figure 5.12</b>		xx

<b>Figure 5.13</b>	(a) Power Vs magnetic field, and (b) resonating frequency with the corresponding magnetic field (for the beam parameters 15.5 kV, 100 mA, $\alpha = 1.12$ , and velocity spread is 2 %)	126
<b>Figure 6.1</b>	(a) Power Vs magnetic field, and (b) resonating frequency with the respective magnetic field at the respective coolant (water) temperature	128
<b>Figure 6.2</b>	Model of MIG with electron beam profile and magnetic field profile	135
<b>Figure 6.3</b>	Velocity ratio ( $\alpha$ ) and velocity spread with respect to (a) modulating cathode voltage and (b) compression ratio ( $F_m$ )	135
<b>Figure 6.4</b>	Normalized cavity field profile and radial profile of the cavity	136
<b>Figure 6.5</b>	(a) Coupling coefficient and (b) start oscillation current of $TE_{11,2,1}$ mode along with other competing modes	137
<b>Figure 6.6</b>	Output power in operating $TE_{11,2}$ mode along with competing modes	138
<b>Figure 6.7</b>	(a) Cavity inner surface temperature and inner surface temperature with respective water flow rate and (b) resonant frequency, and shifting in resonating frequency of the cavity with respective water flow rate	139
<b>Figure 6.8</b>	(a) Temperature distribution of the cavity, (b) deformation distribution of the cavity with the coolant (water) temperature 290 K, and 0.7 L /m fluid flow between the grooves	140
<b>Figure 6.9</b>	SOC of the $TE_{11,2,q}$ mode with axial mode number $q = 1 - 4$	142
<b>Figure 6.10</b>	The cavity field profile for axial mode number $q = 1 - 4$	142
<b>Figure 6.11</b>	(a) Power Vs magnetic field (b) resonating frequency with respective magnetic field (beam parameters are 16.75 kV, 90 mA, $\alpha = 1.8$ , and total velocity spread is 3%)	143
<b>Figure 6.12</b>	(a) Temperature distribution and (b) deformation distribution at the inner surface of the cavity for different coolant temperatures along the axial length of the cavity	144
<b>Figure 6.13</b>	(a) Power and (b) resonant frequency with respect to B-field for both thermal and magnetic tuning schemes	145
<b>Figure 6.14</b>	Transmission and reflection characteristics of the single disk Fused Quartz window at $\epsilon_r = 3.78$ , $\tan(\delta) = 6 \times 10^{-5}$	147
	Temperature distribution of the collector	147

## LIST OF TABLES

---

<b>Table 1.1</b>	State-Of-The-Art of the DNP/NMR Gyrotrons	20
<b>Table 2.1</b>	Structural and Electrical Parameters of the Gyrotron	52
<b>Table 3.1</b>	Properties of OFHC-Cu material at 290 K	68
<b>Table 3.2</b>	Quality factors and $f_r$ for axial mode number ( $q = 1 - 6$ )	74
<b>Table 4.1</b>	Resonating frequency and quality factor of RF cavities	95
<b>Table 4.2</b>	Design Parameters of PBG Gyrotron	100
<b>Table 4.3</b>	Deformation of the PBG Cavity	105
<b>Table 5.1</b>	Structural Parameters of Multi-Section RF Cavity	115
<b>Table 5.2</b>	Resonant Frequency, Quality Factors, Effective Length, and Frequency of the Multi-Section RF Cavity	115
<b>Table 5.3</b>	Resonant Frequency, Quality Factors, and Effective Length of the RF Cavity ( For $\theta_2 = \theta_3 = \theta_4 = 0^0$ , $L_2 = L_4 = 12$ mm)	120
<b>Table 5.4</b>	Design and Simulation Parameters of Gyrotron	121
<b>Table 6.1</b>	Design Parameters of 527 GHz Gyrotron	134
<b>Table 6.2</b>	Structural Parameters of 527 GHz Gyrotron	135
<b>Table 6.3</b>	Comparison of Deformation Obtained by ANSYS and Theory	144