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# **APPENDIX**

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**Table 1 A. Langmuir isotherm parameters determined by different error functions for removal of chromium by nano crystalline zirconia**

<b>20 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	6.820000	6.115234	6.022722	6.112055	6.112071	6.112059
<b>b</b>	0.291300	0.904197	0.980543	1.136825	1.136817	1.136837
<b>R<sup>2</sup><sub>adj</sub></b>	-0.516427	0.312591	0.302098	0.270482	0.270477	0.270476
<b>ERRSQ</b>	3.421719	1.551095	1.574772	1.646110	1.646121	1.646123
<b>HYBRID</b>	19.181305	7.949681	7.847716	8.518162	8.518253	8.518245
<b>MPSD</b>	30.393142	22.906364	23.169870	20.411491	20.411495	20.411606
<b>ARE</b>	10.131047	7.635455	7.723290	6.803830	6.803832	6.803869
<b>EABS</b>	2.818269	2.353298	2.427402	2.119473	2.119468	2.119480
<b>SUM</b>	5.000000	3.210111	3.255349	3.020376	3.607977	3.020394
<b>30 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	7.230000	6.501885	6.392386	6.657742	6.668750	6.671580
<b>b</b>	0.312100	0.914413	0.997212	1.060039	1.054577	1.042776
<b>R<sup>2</sup><sub>adj</sub></b>	-0.295064	0.361665	0.350427	0.265820	0.259745	0.262992
<b>ERRSQ</b>	3.827729	1.886682	1.919897	2.169965	2.187919	2.178323
<b>HYBRID</b>	20.998827	9.379984	9.244262	11.156509	11.259377	11.211073
<b>MPSD</b>	30.441846	24.755093	24.969921	21.093320	21.027032	21.133547
<b>ARE</b>	10.147282	8.251698	8.323307	7.031107	7.009011	7.044516
<b>EABS</b>	2.858702	2.651746	2.736418	2.208820	2.195980	2.204502
<b>SUM</b>	5.000000	3.493580	3.539527	3.256675	3.257417	3.262589
<b>40 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	7.800000	7.040311	6.938564	7.304378	7.302857	7.304514
<b>b</b>	0.381100	1.135885	1.238132	1.251942	1.252659	1.251593
<b>R<sup>2</sup><sub>adj</sub></b>	-0.154884	0.506317	0.498146	0.372574	0.373542	0.372603
<b>ERRSQ</b>	4.337774	1.854287	1.884976	2.356627	2.352992	2.356521
<b>HYBRID</b>	22.825596	8.107479	7.986746	10.693689	10.676598	10.693237
<b>MPSD</b>	31.165683	24.272849	24.213141	20.061941	20.070554	20.064361
<b>ARE</b>	10.388561	8.090950	8.071047	6.687314	6.690185	6.688120
<b>EABS</b>	3.139052	2.892377	2.952223	2.319142	2.320948	2.319285
<b>SUM</b>	5.000000	3.261749	3.278768	3.038017	4.024316	3.038174

**Table 1 A (continued). Langmuir isotherm parameters determined by different error functions for removal of chromium by nano crystalline zirconia**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	8.370000	7.478105	7.364118	7.671222	7.670258	7.671366
<b>b</b>	0.418400	1.456300	1.596474	1.648861	1.649405	1.648779
<b>R<sup>2</sup><sub>adj</sub></b>	-0.212036	0.525135	0.516482	0.452554	0.452935	0.452497
<b>ERRSQ</b>	5.933817	2.324816	2.367181	2.680155	2.678291	2.680436
<b>HYBRID</b>	30.547837	9.452519	9.293090	11.261862	11.252836	11.263221
<b>MPSD</b>	34.988882	24.471190	24.289735	20.646326	20.651328	20.647132
<b>ARE</b>	11.662961	8.157063	8.096578	6.882109	6.883776	6.882377
<b>EABS</b>	3.677001	3.099294	3.160666	2.601849	2.602991	2.601910
<b>SUM</b>	5.000000	2.942909	2.951148	2.708104	2.708091	2.708258
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	9.010000	7.916734	7.776751	8.044463	8.044316	8.044469
<b>b</b>	0.452000	1.979855	2.190706	2.287742	2.288571	2.286756
<b>R<sup>2</sup><sub>adj</sub></b>	-0.293594	0.497237	0.486534	0.459708	0.459661	0.459814
<b>ERRSQ</b>	8.465273	3.290078	3.360117	3.535671	3.535977	3.534974
<b>HYBRID</b>	42.832916	12.641592	12.393597	13.915451	13.916484	13.912487
<b>MPSD</b>	40.521918	26.739503	26.436541	23.197861	23.200112	23.203911
<b>ARE</b>	13.507306	8.913168	8.812180	7.732620	7.733371	7.734637
<b>EABS</b>	4.381795	3.581695	3.656618	3.149241	3.149517	3.149757
<b>SUM</b>	5.000000	2.820952	2.825581	2.606209	2.606444	2.606474
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	9.680000	8.492286	8.322282	8.653810	8.653861	8.584393
<b>b</b>	0.477400	2.730704	3.066008	3.167320	3.167092	3.226756
<b>R<sup>2</sup><sub>adj</sub></b>	-0.260747	0.502088	0.489828	0.464894	0.464896	0.476466
<b>ERRSQ</b>	11.378729	4.493845	4.604501	4.829540	4.829516	4.725093
<b>HYBRID</b>	57.310609	15.840023	15.465655	17.490279	17.490299	16.901872
<b>MPSD</b>	41.839612	30.290985	29.694638	26.312478	26.310804	26.569576
<b>ARE</b>	13.946537	10.096995	9.898213	8.770826	8.770268	8.856525
<b>EABS</b>	4.535233	4.374508	4.455353	3.865710	3.865502	3.946217
<b>SUM</b>	5.000000	3.083841	3.076353	2.839771	2.839643	2.850366

**Table 1B. Freundlich isotherm parameters determined by different error functions for removal of chromium by nano crystalline zirconia**

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	3.74524300	0.37843011	0.39107148	0.38281576	0.38264809	0.38177617
$1/n$	0.13641000	0.50320390	0.49968741	0.48027573	0.48048652	0.48158454
$R^2_{adj}$	-209.43042373	-13.02070259	-13.06824863	-13.10326737	-13.10326409	-13.10325772
<b>ERRSQ</b>	474.82268428	31.63681145	31.74409602	31.82311356	31.82310616	31.82309178
<b>HYBRID</b>	1906.25650215	162.83069105	162.39509507	164.73514526	164.73509242	164.73498972
<b>MPSD</b>	362.80861897	116.40283699	116.83231437	115.83689642	115.83689507	115.83691692
<b>ARE</b>	120.93620632	38.80094566	38.94410479	38.61229881	38.61229836	38.61230564
<b>EABS</b>	43.20437004	11.78856834	11.89372224	11.65000111	11.65000226	11.65000761
<b>SUM</b>	5.00000000	1.06657995	1.07137877	1.06164434	1.06164431	1.06164447
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	3.88347000	0.41519439	0.42108123	0.36103137	0.36043728	0.39862163
$1/n$	0.14569000	0.50683242	0.51290702	0.55988609	0.56080891	0.50708833
$R^2_{adj}$	-179.01313822	-11.21640987	-11.25721689	-11.30789948	-11.30789958	-11.30790096
<b>ERRSQ</b>	532.05233276	36.10719436	36.22780483	36.37760386	36.37760415	36.37760822
<b>HYBRID</b>	2013.62283758	177.27854290	176.81757920	179.69245822	179.69246005	179.69248602
<b>MPSD</b>	357.55244660	121.45109536	122.01598573	120.60526641	120.60526596	120.60525959
<b>ARE</b>	119.18414887	40.48369845	40.67199524	40.20175547	40.20175532	40.20175320
<b>EABS</b>	45.06661576	12.92677524	13.05226642	12.73887317	12.73887307	12.73887165
<b>SUM</b>	5.00000000	1.12208766	1.12802976	1.11489405	1.11489405	1.11489400
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	4.26235900	0.44141711	0.44371177	0.34912438	0.34921096	0.35674208
$1/n$	0.14762000	0.55220404	0.56423881	0.65743468	0.65727127	0.64339560
$R^2_{adj}$	-144.63871250	-10.97614538	-11.01541689	-11.15820484	-11.15820846	-11.15820964
<b>ERRSQ</b>	547.02282002	44.98271583	45.13022066	45.66653592	45.66654954	45.66655396
<b>HYBRID</b>	1903.31203148	207.28498729	206.76898664	211.89914314	211.89921290	211.89923555
<b>MPSD</b>	321.76657319	129.31002506	130.10449499	127.59943778	127.59942075	127.59942752
<b>ARE</b>	107.25552440	43.10334169	43.36816500	42.53314593	42.53314025	42.53314251
<b>EABS</b>	44.11426141	14.77471171	14.93896428	14.42105659	14.42105307	14.42105370
<b>SUM</b>	5.00000000	1.32980909	1.33846915	1.31483417	1.31483404	1.31483412

**Table 1B (continued). Freundlich isotherm parameters determined by different error functions for removal of chromium by nano crystalline zirconia**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>K<sub>F</sub></b>	4.60076400	0.45750964	0.47119371	0.37984209	0.37996352	0.38889271
<b>1/n</b>	0.14887000	0.60730407	0.60649417	0.67440331	0.67418778	0.65870780
<b>R<sup>2</sup><sub>adj</sub></b>	-108.88577737	-9.73700991	-9.77462518	-10.01826454	-10.01826454	-10.01826721
<b>ERRSQ</b>	537.97246953	52.56563566	52.74979035	53.94258592	53.94258590	53.94259895
<b>HYBRID</b>	1746.53464342	230.26059590	229.66203079	238.00962166	238.00962158	238.00967953
<b>MPSD</b>	299.52774001	133.73331262	134.69594018	131.10106968	131.10106970	131.10106041
<b>ARE</b>	99.84258000	44.57777087	44.89864673	43.70035656	43.70035657	43.70035347
<b>EABS</b>	43.54333980	16.11853417	16.32309745	15.55916910	15.55916911	15.55916694
<b>SUM</b>	5.00000000	1.49268252	1.50380767	1.46925671	1.46925671	1.46925666
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>K<sub>F</sub></b>	4.96386500	0.52949598	0.54577695	0.43468845	0.43479909	0.44689560
<b>1/n</b>	0.15019000	0.60416479	0.60386503	0.69133101	0.69115508	0.67244700
<b>R<sup>2</sup><sub>adj</sub></b>	-77.13840757	-8.25649885	-8.29207539	-8.39944809	-8.39944823	-8.39944807
<b>ERRSQ</b>	511.33745966	60.57449538	60.80730813	61.50995470	61.50995563	61.50995456
<b>HYBRID</b>	1552.20571039	252.62282760	251.91964989	258.26730728	258.26731148	258.26730665
<b>MPSD</b>	274.18339860	136.28097997	137.37799431	134.08199966	134.08199857	134.08199982
<b>ARE</b>	91.39446620	45.42699332	45.79266477	44.69399989	44.69399952	44.69399994
<b>EABS</b>	42.10469425	17.20262976	17.45217287	16.70241717	16.70241692	16.70241721
<b>SUM</b>	5.00000000	1.68386800	1.69779906	1.66141344	1.66141343	1.66141344
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>K<sub>F</sub></b>	5.41477000	0.49760794	0.52299233	0.52833403	0.52841390	0.54736384
<b>1/n</b>	0.15377000	0.76870255	0.75484498	0.69595160	0.69584641	0.67175584
<b>R<sup>2</sup><sub>adj</sub></b>	-51.66906201	-6.94771162	-6.98091984	-6.99617563	-6.99617560	-6.99617600
<b>ERRSQ</b>	475.35852674	71.73115189	72.03086887	72.16855819	72.16855790	72.16856153
<b>HYBRID</b>	1340.64294770	283.11970033	282.28916313	286.33845416	286.33845265	286.33847104
<b>MPSD</b>	250.23972680	140.57456156	141.87562569	139.00280549	139.00280465	139.00281486
<b>ARE</b>	83.41324227	46.85818719	47.29187523	46.33426850	46.33426822	46.33427162
<b>EABS</b>	40.64891568	18.69290294	19.00691483	18.31355944	18.31355933	18.31356074
<b>SUM</b>	5.00000000	1.94546250	1.96359702	1.92688937	1.92688936	1.92688950

**Table 1C. Pseudo-first order kinetic parameters determined by different error functions for removal of chromium by nano crystalline zirconia**

<b>20 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.058450	0.080072	0.097690	0.110021	0.232102	0.085190
<b>q<sub>e</sub></b>	4.063300	4.072017	3.844224	3.483097	3.025749	3.793029
<b>R<sup>2</sup><sub>adj</sub></b>	0.385137	0.676274	0.385137	0.468836	-0.091073	0.602459
<b>ERRSQ</b>	2.338609	1.231279	1.313534	2.020260	4.149856	1.512034
<b>HYBRID</b>	12.754373	6.379762	5.998466	7.991471	14.539769	7.169821
<b>MPSD</b>	47.770700	36.361519	36.404523	31.374623	44.337533	32.069707
<b>ARE</b>	14.043266	10.689282	10.701924	9.223272	13.034010	9.427608
<b>EABS</b>	3.539563	2.875003	3.002680	2.804068	4.338913	2.593004
<b>SUM</b>	4.256517	2.920429	2.945252	2.996266	4.856265	2.797744
<b>30 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.069820	0.085519	0.103110	0.117129	0.115733	0.136428
<b>q<sub>e</sub></b>	4.557100	4.197413	3.988114	3.626269	3.630428	3.343875
<b>R<sup>2</sup><sub>adj</sub></b>	0.621074	0.661229	0.621074	0.452164	0.451799	0.116765
<b>ERRSQ</b>	1.446284	1.293020	1.372004	2.090982	2.092374	3.371133
<b>HYBRID</b>	7.854237	6.529099	6.184072	8.096865	8.143977	12.109533
<b>MPSD</b>	36.943689	34.549387	36.263300	33.734314	33.462085	39.146585
<b>ARE</b>	10.860424	10.156565	10.660408	9.916956	9.836928	11.508014
<b>EABS</b>	2.846268	2.806265	3.092731	3.131674	3.106533	3.846856
<b>SUM</b>	3.704968	3.417351	3.574320	3.826470	3.810330	5.000000
<b>40 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.074270	0.099265	0.120214	0.154602	0.231853	0.153447
<b>q<sub>e</sub></b>	4.740200	4.260754	4.066997	3.634152	3.446454	3.637026
<b>R<sup>2</sup><sub>adj</sub></b>	0.517698	0.605329	0.517698	0.300399	0.040443	0.302603
<b>ERRSQ</b>	1.796709	1.470259	1.558448	2.606207	3.574615	2.597996
<b>HYBRID</b>	9.029136	6.705367	6.341297	8.815880	11.557863	8.806524
<b>MPSD</b>	39.451724	38.477327	37.363835	34.257480	35.970119	34.346260
<b>ARE</b>	11.597717	11.311271	10.983935	10.070753	10.574221	10.096851
<b>EABS</b>	3.155985	3.358428	3.452149	3.518993	3.936339	3.520709
<b>SUM</b>	4.085598	3.795250	3.755782	4.122503	4.823500	4.124332

Table 1C (continued). Pseudo-first order kinetic parameters determined by different error functions for removal of chromium by nano crystalline zirconia

50 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.071160	0.103955	0.118026	0.108035	0.107644	0.076942
$q_e$	4.160700	4.427359	4.301970	4.329484	4.338219	4.656614
$R^2_{adj}$	-0.152009	0.715297	-0.152009	0.706630	0.708105	0.629278
<b>ERRSQ</b>	4.177681	1.032456	1.077434	1.063885	1.058537	1.344396
<b>HYBRID</b>	18.777111	4.864653	4.678066	4.843683	4.837672	7.212175
<b>MPSD</b>	62.197604	27.287138	29.710696	27.217925	27.222229	27.162251
<b>ARE</b>	18.284377	8.021665	8.734124	8.001318	8.002583	7.984951
<b>EABS</b>	5.616791	2.416087	2.709600	2.460909	2.456695	2.160084
<b>SUM</b>	5.000000	1.813798	1.944814	1.825959	1.823746	1.963893
60 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.094860	0.132697	0.140472	0.114953	0.120750	0.201156
$q_e$	3.887200	4.667984	4.611790	4.782593	4.697702	4.184430
$R^2_{adj}$	-1.372294	0.896775	-1.372294	0.873958	0.880336	0.675850
<b>ERRSQ</b>	6.786071	0.295281	0.304563	0.360549	0.342304	0.927249
<b>HYBRID</b>	36.127652	1.890361	1.835204	2.593812	2.382482	4.316462
<b>MPSD</b>	80.635542	15.606574	15.952429	13.703486	13.882163	20.931368
<b>ARE</b>	25.758079	4.985337	5.095817	4.377418	4.434494	6.686280
<b>EABS</b>	6.842671	1.188697	1.248656	0.954382	0.997030	1.970377
<b>SUM</b>	5.000000	0.656645	0.673827	0.604289	0.606415	1.063232
70 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.103880	0.346255	0.351781	0.364073	0.365005	0.366778
$q_e$	1.150100	4.702020	4.690766	4.778457	4.778690	4.775209
$R^2_{adj}$	-176.932195	0.526859	-176.932195	0.417180	0.414395	0.418035
<b>ERRSQ</b>	93.044082	0.247414	0.248081	0.304768	45.977954	0.304320
<b>HYBRID</b>	408.602108	1.127615	1.124709	1.411528	1.418404	1.409206
<b>MPSD</b>	250.979181	11.315021	11.250882	10.300397	10.274227	10.252855
<b>ARE</b>	80.172359	3.614451	3.593962	3.290341	3.281981	3.275154
<b>EABS</b>	25.509180	1.128467	1.125846	1.022274	1.019962	1.018986
<b>SUM</b>	5.000000	0.139823	0.139210	0.128886	0.619481	0.128368

**Table 1 D. Pseudo-second order kinetic parameters determined by different error functions for removal of chromium by nano crystalline zirconia**

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	0.014830	0.017947	0.023884	0.026832	0.026838	0.106611
$q_e$	5.249890	5.002088	4.667965	4.326870	4.326630	3.269760
$R^2_{adj}$	0.800509	0.805164	0.793931	0.675351	0.675308	0.078918
<b>ERRSQ</b>	0.843064	0.823389	0.870864	1.371990	1.372172	3.892556
<b>HYBRID</b>	4.385072	3.993490	3.766897	5.375343	5.375608	13.398914
<b>MPSD</b>	29.785901	29.668067	29.984288	23.809620	23.808518	41.215039
<b>ARE</b>	8.756232	8.721592	8.814552	6.999371	6.999047	12.116083
<b>EABS</b>	2.363895	2.412136	2.505625	2.157277	2.157308	4.151290
<b>SUM</b>	2.558681	2.530304	2.563454	2.428692	2.428713	5.000000
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	0.015290	0.019478	0.025279	0.028836	0.027554	0.027967
$q_e$	5.405400	5.096788	4.796531	4.435256	4.497863	4.477306
$R^2_{adj}$	0.798875	0.807059	0.796743	0.668270	0.691529	0.684203
<b>ERRSQ</b>	0.852948	0.818240	0.861991	1.406832	1.308194	1.339260
<b>HYBRID</b>	4.431721	3.911089	3.713979	5.391273	5.105580	5.194583
<b>MPSD</b>	27.930927	27.849277	29.460689	25.671995	25.805955	25.762477
<b>ARE</b>	8.210921	8.186918	8.660629	7.546857	7.586238	7.573456
<b>EABS</b>	2.245502	2.316457	2.540552	2.420960	2.405295	2.410456
<b>SUM</b>	4.208320	4.109466	4.301605	4.695723	4.575546	4.613217
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	0.017130	0.023629	0.029942	0.053272	0.054282	0.051895
$q_e$	5.464770	5.092826	4.836231	4.152480	4.134549	4.177194
$R^2_{adj}$	0.766242	0.782758	0.772594	0.543977	0.533024	0.558318
<b>ERRSQ</b>	0.967571	0.899207	0.941280	1.887570	1.932906	1.828211
<b>HYBRID</b>	4.653833	3.870855	3.692312	6.097774	6.232014	5.923729
<b>MPSD</b>	30.913192	29.686794	28.524329	25.739100	25.661393	25.886550
<b>ARE</b>	9.087624	8.727097	8.385365	7.566584	7.543740	7.609930
<b>EABS</b>	2.616282	2.664125	2.685789	2.785386	2.788504	2.784514
<b>SUM</b>	4.185579	3.962385	3.888063	4.619137	4.660223	4.569727



**Table 1 D (continued). Pseudo-second order kinetic parameters determined by different error functions for removal of chromium by nano crystalline zirconia**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.018870	0.024285	0.028482	0.023182	0.021399	0.024205
<b>q<sub>e</sub></b>	5.556790	5.262814	5.090416	5.221930	5.355176	5.152667
<b>R<sup>2</sup><sub>adj</sub></b>	0.858250	0.870499	0.865410	0.855507	0.863909	0.847155
<b>ERRSQ</b>	0.571161	0.521809	0.542314	0.582217	0.548360	0.615870
<b>HYBRID</b>	2.886100	2.396740	2.310406	2.677738	2.655781	2.740910
<b>MPSD</b>	19.778381	20.762262	21.570660	19.039839	19.135546	19.503276
<b>ARE</b>	5.814297	6.103531	6.341178	5.597187	5.625322	5.733424
<b>EABS</b>	1.678548	1.842787	1.970167	1.712740	1.677457	1.787374
<b>SUM</b>	4.613210	4.538106	4.681095	4.507845	4.436229	4.747161
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.025560	0.027729	0.029253	0.080744	0.088440	0.027486
<b>q<sub>e</sub></b>	5.706450	5.607937	5.545268	4.213943	4.113099	5.624534
<b>R<sup>2</sup><sub>adj</sub></b>	0.965750	0.967986	0.970116	0.972516	0.973929	0.967646
<b>ERRSQ</b>	0.109720	0.104780	0.106909	2.429579	2.884997	0.105082
<b>HYBRID</b>	0.747978	0.680812	0.668344	10.661829	12.671591	0.685919
<b>MPSD</b>	8.726907	8.356051	8.491932	34.325049	37.070262	8.233216
<b>ARE</b>	2.787708	2.669242	2.712648	10.964735	11.841661	2.630004
<b>EABS</b>	0.622461	0.610167	0.640822	3.410618	3.694623	0.595564
<b>SUM</b>	0.736367	0.706019	0.721401	4.458560	5.000000	0.695947
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.100840	0.136150	0.138914	0.159451	0.160174	0.228123
<b>q<sub>e</sub></b>	5.150920	5.027337	5.017283	5.015560	5.011783	4.752355
<b>R<sup>2</sup><sub>adj</sub></b>	0.998968	0.999393	0.999391	0.999138	0.999148	0.997669
<b>ERRSQ</b>	0.106080	0.066956	0.067126	0.091523	0.090574	0.210923
<b>HYBRID</b>	0.522306	0.313444	0.312688	0.426213	0.421575	0.886533
<b>MPSD</b>	5.796140	5.797191	5.820488	5.427367	5.446038	9.634934
<b>ARE</b>	1.851509	1.851845	1.859287	1.733709	1.739673	3.077767
<b>EABS</b>	0.542681	0.567736	0.572026	0.537010	0.539522	1.014425
<b>SUM</b>	2.830203	2.434039	2.443057	2.570657	2.567278	5.000000

**Table 2 A. Langmuir isotherm parameters determined by different error functions for removal of chromium by nano crystalline iron oxide/ oxide hydroxide**

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
<b>Q<sub>o</sub></b>	13.469828	12.726803	12.070369	12.866801	10.342335	13.481515
<b>b</b>	0.286674	0.349410	0.432903	0.317811	0.735040	0.289185
<b>R<sup>2</sup><sub>adj</sub></b>	0.833138	0.846276	0.832649	0.841525	0.608741	0.832439
<b>ERRSQ</b>	3.813137	3.512909	3.824313	3.621483	8.941076	3.829119
<b>HYBRID</b>	16.020038	13.017351	11.915856	14.358625	20.825031	15.926679
<b>MPSD</b>	25.713681	26.054020	26.386337	25.402564	30.240838	25.327167
<b>ARE</b>	8.571227	8.684673	8.795446	8.467521	10.080279	8.442389
<b>EABS</b>	3.289387	3.691429	4.105178	3.488187	5.996393	3.242534
<b>SUM</b>	3.444897	3.356687	3.429601	3.356259	5.000000	3.408825
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
<b>Q<sub>o</sub></b>	12.512513	9.921179	9.418281	9.706686	9.705535	9.706975
<b>b</b>	0.362581	2.335326	3.151903	3.569233	3.570318	3.565278
<b>R<sup>2</sup><sub>adj</sub></b>	0.106122	0.305173	0.266562	0.275519	0.275493	0.275683
<b>ERRSQ</b>	18.571143	14.435658	15.237854	15.051760	15.052299	15.048360
<b>HYBRID</b>	84.910020	44.085912	41.463277	43.820902	43.812284	43.809801
<b>MPSD</b>	58.744944	51.652059	47.804642	43.758013	43.758617	43.778445
<b>ARE</b>	19.581648	17.217353	15.934881	14.586004	14.586206	14.592815
<b>EABS</b>	7.350870	8.227157	8.262973	7.580804	7.582013	7.582504
<b>SUM</b>	4.889616	4.050709	3.936365	3.733784	3.733878	3.734371
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
<b>Q<sub>o</sub></b>	12.408487	10.146187	9.554595	9.847654	9.804420	9.847711
<b>b</b>	0.347146	1.397465	2.046986	2.438883	2.460377	2.438855
<b>R<sup>2</sup><sub>adj</sub></b>	0.222996	0.371021	0.330968	0.322118	0.322467	0.322117
<b>ERRSQ</b>	15.842228	12.824172	13.640804	13.821245	13.814139	13.821263
<b>HYBRID</b>	71.047898	40.361815	37.311483	40.642667	40.271276	40.643176
<b>MPSD</b>	55.647597	49.673930	46.070825	41.211865	41.273159	41.212285
<b>ARE</b>	18.549199	16.557977	15.356942	13.737288	13.757720	13.737428
<b>EABS</b>	7.156699	7.602583	7.779134	7.019363	7.065280	7.019398
<b>SUM</b>	4.919987	4.140194	4.042007	3.827982	3.830412	3.828010

**Table 2A (continued). Langmuir isotherm parameters determined by different error functions for removal of chromium by nano crystalline iron oxide/hydroxide**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	10.687186	9.501463	9.251749	9.263290	9.243737	9.264027
<b>b</b>	0.437959	1.101187	1.307886	1.584483	1.591494	1.584215
<b>R<sup>2</sup><sub>adj</sub></b>	0.402669	0.679036	0.666040	0.635479	0.635254	0.635484
<b>ERRSQ</b>	7.337774	3.942812	4.102461	4.477874	4.480641	4.477810
<b>HYBRID</b>	34.425528	13.093491	12.481246	13.744781	13.689301	13.746975
<b>MPSD</b>	39.852066	28.897569	27.690747	24.721196	24.811770	24.718558
<b>ARE</b>	13.284022	9.632523	9.230249	8.240399	8.270590	8.239519
<b>EABS</b>	4.868753	4.228907	4.295130	4.024802	4.051065	4.023946
<b>SUM</b>	5.000000	3.236496	3.193505	3.076819	3.085524	3.076565
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	11.584801	10.114067	9.528674	9.436142	9.436089	9.413069
<b>b</b>	0.272088	0.564902	0.780614	1.059899	1.059993	1.065192
<b>R<sup>2</sup><sub>adj</sub></b>	0.459696	0.561875	0.531980	0.481945	0.481922	0.481045
<b>ERRSQ</b>	8.397797	6.809657	7.274321	8.051997	8.052354	8.065986
<b>HYBRID</b>	38.715673	24.690643	22.888631	25.457636	25.458872	25.373606
<b>MPSD</b>	42.647477	41.672781	39.211972	35.119795	35.120768	35.197761
<b>ARE</b>	14.215826	13.890927	13.070657	11.706598	11.706923	11.732587
<b>EABS</b>	5.201384	5.861541	5.970884	5.634881	5.635017	5.663918
<b>SUM</b>	4.871125	4.384607	4.296304	4.207084	4.207227	4.215099
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	11.970314	11.188397	10.509669	9.574463	9.600243	12.293694
<b>b</b>	0.185184	0.233686	0.299658	0.477168	0.474744	0.162162
<b>R<sup>2</sup><sub>adj</sub></b>	0.772912	0.789782	0.771924	0.655449	0.658837	0.755129
<b>ERRSQ</b>	3.431692	3.176757	3.446618	5.206752	5.155548	3.700414
<b>HYBRID</b>	15.820115	12.902768	11.843081	15.408747	15.345906	18.171759
<b>MPSD</b>	29.416269	29.858800	29.571527	27.161467	27.041460	28.138798
<b>ARE</b>	9.805423	9.952933	9.857176	9.053822	9.013820	9.379599
<b>EABS</b>	3.564439	3.911758	4.182887	4.419605	4.386289	3.271839
<b>SUM</b>	4.590460	4.653403	4.755807	4.667278	5.367300	4.554668

**Table 2 B. Freundlich isotherm parameters determined by different error functions for removal of chromium by nano crystalline iron oxide/hydroxide**

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	4.48673067	0.87568730	0.88205427	0.70108912	0.70108909	0.85817011
$1/n$	0.31849000	0.78328353	0.81688806	1.00000000	1.00000000	0.81695820
$R^2_{adj}$	-5.26388082	-1.59613069	-1.64461930	-1.60544589	-1.60544584	-1.60544587
<b>ERRSQ</b>	2986.29586027	59.32690461	60.43496867	59.53977592	59.53977493	59.53977552
<b>HYBRID</b>	2110.33242587	215.42663847	212.89814080	213.69588590	213.69588882	213.69588707
<b>MPSD</b>	189.81849357	119.16704150	117.86052360	117.37839098	117.37839309	117.37839063
<b>ARE</b>	63.27283119	39.72234717	39.28684120	39.12613033	39.12613103	39.12613021
<b>EABS</b>	116.09858998	17.12556477	191.40999402	16.87623784	16.87623797	16.87623763
<b>SUM</b>	5.00000000	1.52504642	3.01162945	1.50330412	1.50330414	<b>1.50330411</b>
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	5.84561219	0.72363730	0.80561648	0.76552273	0.76639551	0.80520997
$1/n$	0.19410000	0.88868459	0.82945208	0.85722674	0.85625042	0.81497552
$R^2_{adj}$	-2.92877661	-1.70847614	-1.73945190	-1.71694331	-1.71694322	-1.71694314
<b>ERRSQ</b>	1873.03840169	56.27107435	56.91462418	56.44698771	56.44698571	56.44698403
<b>HYBRID</b>	1542.75514590	224.53690396	223.02901174	223.37234933	223.37235361	223.37235720
<b>MPSD</b>	171.31739992	115.27216525	113.78828267	113.54080043	113.54079888	113.54079759
<b>ARE</b>	57.10579997	38.42405508	37.92942756	37.84693348	37.84693296	37.84693253
<b>EABS</b>	96.47555507	15.68840811	207.65789624	15.44103970	15.44103863	15.44103774
<b>SUM</b>	4.46458891	1.59684939	2.50334308	1.57478486	1.57478484	1.57478482
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	5.54242723	0.83213104	0.74075716	1.00000000	0.56406789	0.59685799
$1/n$	0.21015000	0.75145692	0.87591370	1.00000000	1.00000000	0.94506195
$R^2_{adj}$	-3.06957315	-1.62623346	-1.65512332	-8.95264920	-1.82196373	-1.82196446
<b>ERRSQ</b>	1940.16294299	53.54592772	54.13495920	202.92325223	57.53664637	57.53666123
<b>HYBRID</b>	1573.76906389	216.91814122	215.52087531	526.75992560	233.65855282	233.65860160
<b>MPSD</b>	173.20982358	117.01990871	117.66032114	172.26670897	115.35298399	115.35298377
<b>ARE</b>	57.73660786	39.00663624	39.22010705	57.42223632	38.45099466	38.45099459
<b>EABS</b>	98.48273888	15.96330531	191.90152337	29.58405684	15.02132015	15.02131899
<b>SUM</b>	4.51319415	1.59980960	2.52343511	2.58257602	1.58834749	1.58834752

**Table 2 B (continued). Freundlich isotherm parameters determined by different error functions for removal of chromium by nano crystalline iron oxide/hydroxide**

50 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	5.16249923	0.65854749	0.70582592	0.59522811	0.59526020	0.59546827
$1/n$	0.19705000	0.68517940	0.66269828	0.71649667	0.71645804	0.71620756
$R^2_{adj}$	-2.59325805	-4.61299249	-4.64915659	-4.69406352	-4.69406358	-4.69406411
<b>ERRSQ</b>	1713.08042804	68.95153746	69.39578720	69.94743623	69.94743694	69.94744347
<b>HYBRID</b>	1480.69021944	269.46270604	268.30815311	275.50823595	275.50823903	275.50826732
<b>MPSD</b>	163.94055553	134.42998594	135.69101479	132.54191190	132.54191123	132.54190505
<b>ARE</b>	54.64685184	44.80999531	45.23033826	44.18063730	44.18063708	44.18063502
<b>EABS</b>	88.65136490	18.21291773	247.62883915	17.65845272	17.65845252	17.65845071
<b>SUM</b>	4.35800097	1.93576833	2.87708263	1.91515985	1.91515984	1.91515978
60 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	4.57098715	0.74232216	0.74640026	0.64095247	0.65782749	0.78012201
$1/n$	0.24157000	0.65681243	0.67973762	0.80892111	0.78817020	0.66461390
$R^2_{adj}$	-2.80921388	-2.17903511	-2.21698599	-2.27163960	-2.27163984	-2.27163929
<b>ERRSQ</b>	1816.03704894	49.41091508	50.00077564	50.85024253	50.85024623	50.85023770
<b>HYBRID</b>	1517.67822934	150.71165728	199.01215073	199.49147168	199.49147510	199.49146721
<b>MPSD</b>	169.40535266	101.37185938	111.97655233	110.04666239	110.04666011	110.04667139
<b>ARE</b>	56.46845089	38.46999699	37.32551744	36.68222080	36.68222004	36.68222380
<b>EABS</b>	94.44755765	15.28742957	181.14359580	14.56600037	14.56600038	14.56600158
<b>SUM</b>	4.52139606	<b>1.49056970</b>	2.48065769	1.53906834	1.53906832	1.53906845
70 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	3.57470329	0.66952635	0.73003192	0.58076170	0.61135747	0.63514679
$1/n$	0.31264000	0.67988184	0.65155927	0.75948385	0.72148706	0.69445233
$R^2_{adj}$	-2.85899987	-1.31892504	-1.36536576	-1.34104205	-1.34101898	-1.34104195
<b>ERRSQ</b>	1839.77244574	35.04290673	35.74470500	35.37713243	35.37678376	35.37713093
<b>HYBRID</b>	0.03378162	150.71165728	148.84555834	154.17597149	154.17370058	154.17596176
<b>MPSD</b>	170.24647047	101.37185938	101.43352164	101.32930632	101.32932828	101.32930618
<b>ARE</b>	56.74882349	33.79061979	33.81117388	33.77643544	33.77644276	33.77643539
<b>EABS</b>	95.33968244	12.72450200	137.20989379	12.51978438	12.51989114	12.51978479
<b>SUM</b>	3.69506465	2.28019864	3.17646329	2.30085827	2.30084439	2.30085821

Table 2 C. Pseudo-first order kinetic parameters determined by different error functions for removal of chromium by nano crystalline iron oxide/hydroxide

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.040694	0.376077	0.380126	0.412431	1	0.380126
$q_e$	1.373599	6.254717	6.246091	6.200046	1	6.246091
$R^2_{adj}$	-321.8269	0.51575	0.514984	0.479151	-305.1344	0.514984
<b>ERRSQ</b>	280.17079	0.420265	0.420929	0.452028	265.68391	265.68391
<b>HYBRID</b>	571.42919	0.84074	0.839377	0.888794	538.429	538.429
<b>MPSD</b>	305.43319	9.98213	9.888269	9.20316	295.86616	295.86616
<b>ARE</b>	571.42919	2.823373	2.796825	2.603047	83.683588	83.683588
<b>EABS</b>	52.925943	1.742694	1.729913	1.634121	1.63405	51.43714
<b>SUM</b>	5	0.073521	0.072926	0.068731	3.03654	3.977536
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.053798	0.318509	0.322541	0.346875	1	0.322541
$q_e$	1.524228	6.368376	6.360654	6.348565	1	6.360654
$R^2_{adj}$	-212.03185	0.743574	0.742994	0.723873	-218.96498	0.742994
<b>ERRSQ</b>	264.22804	0.318051	0.31877	0.342486	272.82736	272.82736
<b>HYBRID</b>	533.4709	0.646928	0.645368	0.688538	546.29748	546.29748
<b>MPSD</b>	293.75667	8.593447	8.496158	7.948708	296.38258	296.38258
<b>ARE</b>	533.4709	2.430594	2.403076	2.248234	83.829653	83.829653
<b>EABS</b>	51.392377	1.491849	1.479489	1.407498	1.407509	52.081268
<b>SUM</b>	4.967661	0.09669	0.095826	<b>0.090557</b>	2.215402	4.142415
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.053337	0.349484	0.353926	0.373332	1	0.353926
$q_e$	1.539324	6.292051	6.282767	6.308986	1	6.282767
$R^2_{adj}$	-212.03185	0.590076	0.589282	0.568144	-258.70799	0.589282
<b>ERRSQ</b>	258.65579	0.422543	0.423361	0.44515	267.70238	267.70238
<b>HYBRID</b>	526.45596	0.8616	0.859895	0.910375	540.57919	540.57919
<b>MPSD</b>	292.85398	9.922974	9.919821	9.262392	295.99479	295.99479
<b>ARE</b>	526.45596	2.806641	2.805749	2.6198	83.719969	83.719969
<b>EABS</b>	50.855225	1.715836	1.720081	1.613956	51.612811	51.612811
<b>SUM</b>	4.914791	0.075272	0.075342	0.070886	4.159026	4.159026

Table 2 C (continued). Pseudo-first order kinetic parameters determined by different error functions for removal of chromium by nano crystalline iron oxide/hydroxide

50 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.066672	0.381565	0.384142	0.392634	1	0.384142
$q_e$	1.334627	6.171963	6.166865	6.200029	1	6.166865
$R^2_{adj}$	-357.97407	0.663158	0.662815	0.64426	-360.7956	0.662815
<b>ERRSQ</b>	255.50383	0.239751	0.239995	0.253202	257.51209	257.51209
<b>HYBRID</b>	527.58524	0.494063	0.493554	0.525737	528.92301	528.92301
<b>MPSD</b>	295.24927	7.617661	7.609878	7.076068	295.14839	295.14839
<b>ARE</b>	527.58524	2.1546	2.152399	2.001414	83.480571	83.480571
<b>EABS</b>	50.533117	1.305667	1.306362	1.215546	50.656378	50.656378
<b>SUM</b>	4.987239	0.057525	0.057508	0.053733	4.15789	4.15789
60 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.047258	0.384751	0.388608	0.406151	1	0.388608
$q_e$	1.209344	6.021113	6.013693	6.040185	1	6.013693
$R^2_{adj}$	-361.59286	0.5261	0.525414	0.505181	-335.47129	0.662815
<b>ERRSQ</b>	261.80837	0.342177	0.342673	0.357282	242.94742	242.94742
<b>HYBRID</b>	553.99518	0.729431	0.728378	0.765313	511.18456	511.18456
<b>MPSD</b>	306.3383	8.665101	8.66709	8.06274	293.69991	293.69991
<b>ARE</b>	553.99518	2.450861	2.451423	2.280487	83.070879	83.070879
<b>EABS</b>	51.163289	1.438328	1.441634	1.34441	49.196353	49.196353
<b>SUM</b>	5	0.063446	0.063518	0.059459	3.920931	3.920931
70 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.075308	0.442516	0.444735	0.459742	1	0.444735
$q_e$	1.275675	5.83697	5.833591	5.833075	1	5.833591
$R^2_{adj}$	-597.05535	0.5821	0.581824	0.575931	-599.55405	0.581824
<b>ERRSQ</b>	226.70135	0.158411	0.158515	0.16075	227.64852	227.64852
<b>HYBRID</b>	492.59605	0.341527	0.3413	0.345945	492.54329	492.54329
<b>MPSD</b>	292.49133	6.55175	6.512039	6.275261	292.18333	292.18333
<b>ARE</b>	492.59605	1.853115	1.841883	1.774912	82.641925	82.641925
<b>EABS</b>	47.608361	1.071604	1.06606	1.031639	47.662155	47.662155
<b>SUM</b>	4.994711	0.050034	0.049759	0.048111	4.166608	4.166608

**Table 2 D. Pseudo-second order kinetic parameters determined by different error functions for removal of chromium by nano crystalline iron oxide/hydroxide**

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	0.072653	0.148272	0.148010	0.200399	0.145382	0.145700
$q_e$	6.761325	6.582324	6.580597	6.105291	6.548319	6.546251
$R^2_{adj}$	-0.252828	0.830397	0.830327	0.857709	0.810167	0.809084
<b>ERRSQ</b>	1.087288	0.147193	0.147254	0.053937	0.164750	0.165690
<b>HYBRID</b>	2.326977	0.297367	0.297241	0.116545	0.329388	0.331157
<b>MPSD</b>	15.499318	6.291445	6.286697	3.533651	6.221183	6.222071
<b>ARE</b>	4.383869	1.779489	1.778146	0.999467	1.759616	1.759867
<b>EABS</b>	2.601670	1.095971	1.095782	0.577906	1.094087	1.094376
<b>SUM</b>	5.000000	1.496259	1.495576	0.777795	1.516377	1.518227
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	0.077893	0.124291	0.121122	0.111750	0.103248	0.381441
$q_e$	6.815239	6.723126	6.730487	6.693685	6.732283	6.358122
$R^2_{adj}$	0.217423	0.789875	0.789216	0.730231	0.708405	0.358318
<b>ERRSQ</b>	0.679172	0.260622	0.261440	0.334601	0.361672	0.795893
<b>HYBRID</b>	1.443158	0.541123	0.539309	0.670773	0.724174	1.745106
<b>MPSD</b>	13.044696	8.112672	8.076297	7.848190	7.737295	13.157267
<b>ARE</b>	3.689597	2.294610	2.284322	2.219803	2.188438	3.721437
<b>EABS</b>	2.208206	1.389010	1.386870	1.377310	1.367879	2.219324
<b>SUM</b>	4.658200	2.496596	2.490090	2.618364	2.661871	5.000000
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	0.076463	0.133786	0.132331	0.128284	0.128709	0.121836
$q_e$	6.768190	6.642807	6.644732	6.594312	6.590823	6.649988
$R^2_{adj}$	0.014611	0.839080	0.838912	0.794996	0.792590	0.820408
<b>ERRSQ</b>	0.855187	0.165873	0.166047	0.211315	0.213794	0.185120
<b>HYBRID</b>	1.825679	0.337446	0.337063	0.422216	0.427034	0.371560
<b>MPSD</b>	14.060204	6.150838	6.078582	5.686722	5.688337	5.661698
<b>ARE</b>	3.976826	1.739720	1.719283	1.608448	1.608905	1.601370
<b>EABS</b>	2.367365	1.065777	1.054996	1.004482	1.004924	0.997556
<b>SUM</b>	5.000000	1.703919	1.689080	1.711577	1.717532	1.646715



**Table 2 D (continued). Pseudo-second order kinetic parameters determined by different error functions for removal of chromium by nano crystalline iron oxide/hydroxide**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.107563	0.176422	0.173170	0.142418	0.146599	0.137911
<b>q<sub>e</sub></b>	6.510417	6.439555	6.442781	6.483789	6.455741	6.517554
<b>R<sup>2</sup><sub>adj</sub></b>	0.200004	0.740375	0.739967	0.681894	0.672748	0.682041
<b>ERRSQ</b>	0.694290	0.184791	0.185081	0.226416	0.232925	0.226311
<b>HYBRID</b>	1.438523	0.383608	0.382965	0.460492	0.473356	0.460519
<b>MPSD</b>	12.733334	6.670032	6.646219	6.391020	6.403042	6.380050
<b>ARE</b>	3.601531	1.886570	1.879835	1.807653	1.811054	1.804551
<b>EABS</b>	2.182718	1.133935	1.131718	1.108192	1.111978	1.103929
<b>SUM</b>	5.000000	2.099981	2.095195	2.157763	2.179704	2.153954
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.091801	0.168689	0.167244	0.169639	0.169631	0.189201
<b>q<sub>e</sub></b>	6.429628	6.308338	6.308695	6.239100	6.239103	6.155859
<b>R<sup>2</sup><sub>adj</sub></b>	-1.064212	0.784308	0.784151	0.722348	0.722326	0.597331
<b>ERRSQ</b>	1.791462	0.155739	0.155853	0.200478	0.200493	0.290745
<b>HYBRID</b>	3.741103	0.329358	0.329103	0.416126	0.416159	0.598787
<b>MPSD</b>	22.217730	6.581847	6.521095	5.692769	5.692969	7.395860
<b>ARE</b>	6.284123	1.861627	1.844444	1.610158	1.610215	1.804551
<b>EABS</b>	3.798984	1.098452	1.089614	0.968020	0.968052	1.267573
<b>SUM</b>	5.000000	1.056602	1.048802	0.990401	0.990445	1.276054
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.136215	0.231700	0.230443	0.200399	0.210823	0.225557
<b>q<sub>e</sub></b>	6.121824	6.055559	6.056207	6.105291	6.067903	6.020373
<b>R<sup>2</sup><sub>adj</sub></b>	-2.149012	0.880851	0.880807	0.857709	0.866927	0.832884
<b>ERRSQ</b>	2.565318	0.045165	0.045182	0.053937	0.050443	0.063348
<b>HYBRID</b>	5.202696	0.098323	0.098285	0.116545	0.109067	0.136357
<b>MPSD</b>	28.279955	3.657100	3.651737	3.533651	3.562652	3.874983
<b>ARE</b>	7.998779	1.034384	1.032867	0.999467	1.007670	1.096011
<b>EABS</b>	4.913596	0.594006	0.593426	0.577906	0.583787	0.637499
<b>SUM</b>	5.000000	0.416030	0.415532	0.410945	0.411394	0.454689

**Table 3 A (continued). Langmuir isotherm parameters determined by different error functions for removal of cadmium by nano crystalline zirconia**

<b>20 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	3.188555	3.170709	2.940551	3.308068	3.323868	3.435922
<b>b</b>	8.531489	7.932849	12.953026	6.257553	6.159616	5.542239
<b>R<sup>2</sup><sub>adj</sub></b>	0.901497	0.904275	0.878716	0.896133	0.894645	0.879424
<b>ERRSQ</b>	0.619880	0.602397	0.763238	0.653639	0.663001	0.758787
<b>HYBRID</b>	7.135882	7.288362	6.500465	8.372929	8.467467	9.236324
<b>MPSD</b>	60.084074	59.220940	58.247646	59.064169	59.120570	59.439141
<b>ARE</b>	16.994343	16.750211	16.474922	16.705870	16.721823	16.811928
<b>EABS</b>	2.103222	2.018422	2.401193	1.898483	1.894691	1.868809
<b>SUM</b>	4.460668	4.390224	4.642665	4.519617	3.558452	4.750985
<b>30 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	3.140059	3.135859	3.021110	3.075542	3.078619	3.151625
<b>b</b>	7.253649	6.717300	8.373580	6.523788	6.386645	5.956100
<b>R<sup>2</sup><sub>adj</sub></b>	0.940636	0.942924	0.935485	0.937872	0.936691	0.939162
<b>ERRSQ</b>	0.355953	0.342233	0.386836	0.372524	0.379606	0.364791
<b>HYBRID</b>	4.302034	4.423294	4.129923	4.683759	4.791881	4.928859
<b>MPSD</b>	48.243738	48.027691	46.823686	47.010630	47.297576	47.750967
<b>ARE</b>	13.645390	13.584283	13.243738	13.296614	13.377775	13.506013
<b>EABS</b>	1.701045	1.641414	1.734982	1.569295	1.576378	1.560100
<b>SUM</b>	4.773432	4.719240	4.779037	4.766658	4.822881	4.821787
<b>40 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	3.188270	3.359543	3.320432	3.320500	3.320486	1.000000
<b>b</b>	6.532080	4.634801	4.714509	5.138016	5.138358	1.000000
<b>R<sup>2</sup><sub>adj</sub></b>	0.896158	0.918010	0.917337	0.915471	0.915467	-4.704159
<b>ERRSQ</b>	0.670488	0.529395	0.533739	0.545788	0.545812	36.830657
<b>HYBRID</b>	6.819967	5.787906	5.769486	5.933236	5.933445	185.578379
<b>MPSD</b>	56.546971	52.671827	52.888953	50.495661	50.497089	299.965874
<b>ARE</b>	15.993899	14.897842	14.959255	14.282330	14.282734	84.843162
<b>EABS</b>	2.043375	1.884510	1.916759	1.796432	1.796452	17.948546
<b>SUM</b>	0.545823	0.501743	0.505006	0.483554	0.483567	5.000000

**Table 3 A (continued). Langmuir isotherm parameters determined by different error functions for removal of cadmium by nano crystalline zirconia**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	2.865850	2.893300	2.842456	2.897149	2.895984	2.898365
<b>b</b>	5.019520	4.332701	4.805559	4.257400	4.259947	4.245333
<b>R<sup>2</sup><sub>adj</sub></b>	0.965183	0.970857	0.968861	0.970779	0.970773	0.970758
<b>ERRSQ</b>	0.159235	0.133282	0.142411	0.133642	0.133669	0.133739
<b>HYBRID</b>	3.002948	2.994191	2.923028	3.023490	3.023157	3.028372
<b>MPSD</b>	35.296957	29.075412	32.632520	28.344962	28.334550	28.356757
<b>ARE</b>	9.983487	8.223768	9.229870	8.017166	8.014221	8.020502
<b>EABS</b>	0.894196	0.620139	0.791543	0.588382	0.588139	0.587092
<b>SUM</b>	4.991605	4.166718	4.593786	4.101749	4.100946	4.103196
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	2.574280	2.545124	2.510878	2.518993	2.514737	2.545552
<b>b</b>	4.524120	4.945687	5.181215	5.633431	5.644662	4.477419
<b>R<sup>2</sup><sub>adj</sub></b>	0.920155	0.921689	0.920681	0.918002	0.918076	0.918006
<b>ERRSQ</b>	0.292952	0.287323	0.291022	0.300852	0.300578	0.300835
<b>HYBRID</b>	1.911512	1.792043	1.768062	1.895853	1.887711	1.963449
<b>MPSD</b>	28.127009	26.958074	26.805557	25.910021	25.960387	27.237891
<b>ARE</b>	7.955519	7.624895	7.581756	7.328461	7.342706	7.704039
<b>EABS</b>	1.348829	1.330011	1.360919	1.354126	1.360666	1.293174
<b>SUM</b>	4.938407	4.761905	4.773852	4.802941	4.806270	4.886944
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	2.563400	2.514460	2.428693	2.462735	2.462790	2.470231
<b>b</b>	4.462310	4.942169	6.061601	5.826497	5.822228	5.317120
<b>R<sup>2</sup><sub>adj</sub></b>	0.900059	0.902098	0.894743	0.897947	0.897982	0.900493
<b>ERRSQ</b>	0.362488	0.355092	0.381770	0.370150	0.370020	0.360913
<b>HYBRID</b>	3.100377	2.802679	2.567237	2.590146	2.590148	2.665745
<b>MPSD</b>	38.616829	36.199487	33.897666	33.319435	33.300386	34.573746
<b>ARE</b>	10.922489	10.238761	9.587708	9.424159	9.418772	9.778932
<b>EABS</b>	1.486803	1.457508	1.536896	1.471331	1.470334	1.443993
<b>SUM</b>	4.916899	4.657249	4.583631	4.487974	4.486000	4.535338

**Table 3B. Freundlich isotherm parameters determined by different error functions for removal of cadmium by nano crystalline zirconia**

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	2.57717000	1.07040532	1.05322121	0.99647479	0.99647479	0.99647562
$1/n$	0.28328772	1.09361985	1.14694813	0.99649584	0.99649584	0.99649500
$R^2_{adj}$	-2.63805904	-1.71337953	-1.71967611	-1.85562051	-1.85562051	-1.85562051
ERRSQ	20.37469854	17.07530742	17.11493183	17.97043038	17.97043039	17.97043041
HYBRID	124.12545340	103.79476917	103.63221229	109.01219989	109.01219990	109.01220000
MPSD	245.92372538	222.18867869	224.14582154	220.66264763	220.66264763	220.66264766
ARE	139.11546710	125.68889712	126.79602431	124.82564360	124.82564360	124.82564361
EABS	12.81738865	11.36911678	11.56333510	11.06404897	11.06404897	11.06404897
SUM	5.00000000	4.36825243	4.39995698	4.41800733	4.41800733	4.41800733
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	2.46429000	1.03888588	1.05139655	0.95494040	0.95686849	0.95947195
$1/n$	0.29680989	1.06972845	1.09256999	0.97925711	0.97728392	0.97463197
$R^2_{adj}$	-2.63158888	-1.63524272	-1.64247036	-1.79566590	-1.79566588	-1.79566617
ERRSQ	22.48882718	15.80109592	15.84443332	16.76300427	16.76300413	16.76300587
HYBRID	131.01340843	97.91521982	97.73353879	103.65966451	103.65966384	103.65967266
MPSD	253.08250085	218.29573685	220.88272768	217.12468095	217.12468102	217.12468017
ARE	143.16508204	123.48671666	124.95013967	122.82426741	122.82426745	122.82426697
EABS	13.63230019	10.99923769	11.24292284	10.70996004	10.70996006	10.70995982
SUM	5.00000000	3.98193442	4.02079417	4.03807901	4.03807900	4.03807912
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	2.48780000	1.05014192	1.06322062	1.20418435	1.13769690	1.06281356
$1/n$	0.32575730	1.07930290	1.10272181	0.92333315	0.97729310	1.04615085
$R^2_{adj}$	-3.17365674	-1.85522083	-1.86209653	-1.85732005	-1.85732005	-1.85732006
ERRSQ	28.28403710	18.43561003	18.48000508	18.44916430	18.44916429	18.44916431
HYBRID	151.96792686	106.34810261	106.16366348	106.60823730	106.60823716	106.60823744
MPSD	257.64256500	228.45805904	229.02004381	228.14753482	228.14753496	228.14753468
ARE	145.74464387	129.23539421	129.55330080	129.05973519	129.05973526	129.05973511
EABS	14.46919325	12.08503289	12.17066377	12.03771763	12.03771765	12.03771760
SUM	5.00000000	3.96028360	3.97092021	3.95679402	3.95679402	3.95679401

**Table 3B (continued). Freundlich isotherm parameters determined by different error functions for removal of cadmium by nano crystalline zirconia**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>K<sub>F</sub></b>	2.05853000	0.93179743	0.97242051	2.97271136	2.15189467	0.71491588
<b>1/n</b>	0.30637630	0.92735639	0.92036284	0.33523532	0.46310718	1.03562831
<b>R<sup>2</sup><sub>adj</sub></b>	-1.99807902	-1.54987724	-1.55935006	-1.72424551	-1.72424562	-1.70202120
<b>ERRSQ</b>	12.94917991	11.66178052	11.70510415	12.45924814	12.45924865	12.35760598
<b>HYBRID</b>	88.33419444	79.98646650	79.78496508	81.96651813	81.96651994	84.83788782
<b>MPSD</b>	218.94165697	210.22682677	210.15876073	209.93479872	209.93479863	210.49961033
<b>ARE</b>	123.85210426	118.92225184	118.88374787	118.75705582	118.75705577	119.07656152
<b>EABS</b>	10.23795066	9.90203051	9.93376014	10.03816215	10.03816219	9.77486988
<b>SUM</b>	5.00000000	4.69365900	4.69720098	4.78828800	4.78828807	4.79238663
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>K<sub>F</sub></b>	1.78014000	1.00000000	0.88044322	2.55471009	1.93223248	0.62354580
<b>1/n</b>	0.31496261	1.00000000	0.81907456	0.38729447	0.51206316	0.92965184
<b>R<sup>2</sup><sub>adj</sub></b>	-1.67175016	-3.03211481	-1.59620962	-2.93131204	-2.93131204	-1.83918004
<b>ERRSQ</b>	9.83292216	14.79381708	9.52548528	14.42397203	14.42397205	10.41694302
<b>HYBRID</b>	74.55272322	94.64251682	70.51646636	92.84734227	92.84734239	76.72598462
<b>MPSD</b>	210.01658130	206.27743654	207.36498987	205.59158884	205.59158883	208.30014364
<b>ARE</b>	118.80331904	116.68813935	117.30335242	116.30016530	116.30016529	117.83235527
<b>EABS</b>	9.20068610	9.53135000	9.29338027	9.46767947	9.46767947	9.20146842
<b>SUM</b>	4.41770178	4.96439191	4.333874687	4.90721250	4.90721250	4.49760772
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>K<sub>F</sub></b>	1.77544000	0.87744136	0.88036917	1.00525038	1.00525038	0.79504678
<b>1/n</b>	0.30026063	0.80174625	0.81938637	1.00529583	1.00529583	0.83025666
<b>R<sup>2</sup><sub>adj</sub></b>	-2.03323233	-1.38574472	-1.39107384	-2.95822338	-2.95822338	-1.41714151
<b>ERRSQ</b>	10.62888266	8.65314143	8.67247023	14.35655139	14.35655139	8.76701818
<b>HYBRID</b>	78.90043779	66.52589058	66.42529274	92.75351719	92.75351719	67.60692084
<b>MPSD</b>	212.13508064	198.62368177	198.28040341	192.72695259	192.72695259	199.45690503
<b>ARE</b>	120.00172324	112.35852182	112.16433426	109.02282807	109.02282807	112.82986408
<b>EABS</b>	9.30507939	8.56626390	8.56724822	8.58317221	8.58317221	8.56387471
<b>SUM</b>	4.59099700	4.11318025	4.11031139	4.73943899	4.73943899	4.14036600

**Table 3 C. Pseudo-first order kinetic parameters determined by different error functions for removal of cadmium by nano crystalline zirconia**

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.12344080	1.75777030	1.78028869	1.01931356	1.01932133	1.01930342
$q_e$	0.08105504	0.46476717	0.46384871	0.46861743	0.46861742	0.46861884
$R^2_{adj}$	0.93397499	0.99987243	0.93397499	0.99956626	0.99956627	0.99956625
ERRSQ	2.18576988	0.00471981	0.00472907	0.01200637	0.01200612	0.01200647
HYBRID	43.50812802	0.09782350	0.09764183	0.26614045	0.26613476	0.26614307
MPSD	352.17000506	13.58642198	13.54418952	14.47485328	14.47488820	14.47493035
ARE	89.84736686	3.46623569	3.45546113	3.69289671	3.69290562	3.69291637
EABS	5.32928299	0.20179686	0.20161614	0.20860376	0.20860433	0.20860446
SUM	5.00000000	0.11943172	0.11915802	0.13295671	0.13295678	0.13295739
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.20107493	1.30130102	1.36198057	0.91471873	0.91471897	0.91489675
$q_e$	0.16667866	0.45538641	0.45260315	0.46789969	0.46789967	0.46789975
$R^2_{adj}$	0.95626470	0.99964617	0.95626470	0.99944087	0.99944087	0.99944099
ERRSQ	1.36239434	0.01140118	0.01148321	0.01443566	0.01443565	0.01443274
HYBRID	28.25612973	0.24518496	0.24346286	0.33570285	0.33570271	0.33562292
MPSD	289.24853698	23.70472834	23.79623018	22.73121085	22.73121267	22.73280457
ARE	73.79452833	6.04766844	6.07101284	5.79929980	5.79930027	5.79970640
EABS	4.20713020	0.33706515	0.34110474	0.31009909	0.31009913	0.31012373
SUM	5.00000000	0.26106892	0.26266105	0.25335874	0.25335875	0.25337065
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.09704842	0.72359563	0.75027555	0.60958834	0.61479052	0.60959563
$q_e$	0.14511423	0.45855543	0.45644450	0.45995607	0.45993749	0.45995605
$R^2_{adj}$	0.94398750	0.99977450	0.94398750	0.99968780	0.99969627	0.99968781
ERRSQ	1.62037255	0.00666380	0.00672490	0.00843462	0.00824925	0.00843435
HYBRID	34.45717272	0.17712838	0.17558630	0.23974035	0.23397785	0.23973203
MPSD	326.16241787	17.08724035	17.47295715	15.89805983	15.94814913	15.89810935
ARE	83.21218160	4.35938192	4.45778791	4.05599226	4.06877129	4.05600489
EABS	4.57091433	0.21044477	0.21729415	0.18952682	0.19042554	0.18952780
SUM	5.00000000	0.16007051	0.16392712	0.15111219	0.15133431	0.15111230

**Table 3 C(continued). Pseudo-first order kinetic parameters determined by different error functions for removal of cadmium by nano crystalline zirconia**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.07111664	1.01530326	1.07520015	0.85326703	0.84643285	0.84643319
<b>q<sub>e</sub></b>	0.13682958	0.38064058	0.37758811	0.37403502	0.37517991	0.37517986
<b>R<sup>2</sup><sub>adj</sub></b>	0.94377530	0.99967064	0.94377530	0.99963990	0.99963328	0.99963328
<b>ERRSQ</b>	1.22015921	0.01010066	0.01019526	0.01210020	0.01193013	0.01193014
<b>HYBRID</b>	30.51308122	0.25705738	0.25460958	0.31513705	0.31243489	0.31243498
<b>MPSD</b>	331.42490766	24.25752247	23.51605136	21.42392824	21.37092409	21.37092575
<b>ARE</b>	84.55477422	6.18870003	5.99953222	5.46577935	5.45225666	5.45225709
<b>EABS</b>	3.97571136	0.28453933	0.27780034	0.25206372	0.25076654	0.25076659
<b>SUM</b>	5.00000000	0.23465528	0.22848310	0.21292950	0.21205543	0.21205546
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.09716357	0.52015527	0.59406881	0.55650959	0.55718546	0.55651062
<b>q<sub>e</sub></b>	0.24910933	0.40397175	0.39520676	0.38938989	0.38913293	0.38938989
<b>R<sup>2</sup><sub>adj</sub></b>	0.96694968	0.99939597	0.96694968	0.99958274	0.99958497	0.99958274
<b>ERRSQ</b>	0.71054130	0.01755069	0.01816685	0.01911261	0.01916872	0.01911260
<b>HYBRID</b>	18.29799532	0.46723450	0.44978729	0.47656705	0.47738164	0.47656638
<b>MPSD</b>	260.42495539	32.47184648	32.86650888	29.56038576	29.57203784	29.56036209
<b>ARE</b>	66.44091254	8.28437931	8.38506755	7.54159294	7.54456568	7.54158690
<b>EABS</b>	3.03097822	0.37666393	0.38512017	0.35041071	0.35076456	0.35041059
<b>SUM</b>	5.00000000	0.42388244	0.42961695	0.39556974	0.39589945	0.39556947
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.15623552	0.86613421	0.91389893	0.83797271	0.83797154	0.83797251
<b>q<sub>e</sub></b>	0.14314955	0.41694507	0.41470569	0.41679542	0.41679564	0.41679565
<b>R<sup>2</sup><sub>adj</sub></b>	0.95214398	0.99980816	0.95214398	0.99980671	0.99980671	0.99980671
<b>ERRSQ</b>	1.18356792	0.00502381	0.00510719	0.00507015	0.00507015	0.00507014
<b>HYBRID</b>	27.45087220	0.12533431	0.12297317	0.12936230	0.12936241	0.12936222
<b>MPSD</b>	302.84269209	17.23488144	17.64189528	16.93169376	16.93167359	16.93168493
<b>ARE</b>	77.26273693	4.39704885	4.50088825	4.31969810	4.31969295	4.31969584
<b>EABS</b>	3.91769342	0.21407962	0.22245710	0.20898568	0.20898526	0.20898544
<b>SUM</b>	5.00000000	0.17727539	0.18208615	0.17415875	0.17415852	0.17415863

**Table 3 D. Pseudo-second order kinetic parameters determined by different error functions for removal of cadmium by nano crystalline zirconia**

<b>20 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	4.980821	2.207200	8.234320	6.723048	6.559478	6.547558
<b>q<sub>e</sub></b>	0.492383	0.499900	0.482173	0.482379	0.483383	0.483459
<b>R<sup>2</sup><sub>adj</sub></b>	0.458327	-4.568996	0.839712	0.764088	0.750415	0.749357
<b>ERRSQ</b>	0.003087	0.030825	0.001299	0.001799	0.001816	0.001817
<b>HYBRID</b>	0.068642	0.678399	0.027120	0.038407	0.039017	0.039067
<b>MPSD</b>	7.489663	29.653919	6.837141	6.563530	6.506237	6.508296
<b>ARE</b>	1.910800	7.565456	1.744326	1.674520	1.659904	1.660429
<b>EABS</b>	0.107530	0.422552	0.100809	0.096164	0.095012	0.095025
<b>SUM</b>	5.000000	31.717932	3.579030	3.789371	3.777646	3.779533
<b>30 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	2.676760	4.586176	4.818338	4.058760	4.061911	4.059226
<b>q<sub>e</sub></b>	0.503094	0.484096	0.481822	0.491293	0.491230	0.491282
<b>R<sup>2</sup><sub>adj</sub></b>	0.449369	0.761225	0.771391	0.712026	0.712573	0.712122
<b>ERRSQ</b>	0.007162	0.003716	0.003742	0.003956	0.003952	0.003956
<b>HYBRID</b>	0.174851	0.082554	0.082004	0.090542	0.090434	0.090524
<b>MPSD</b>	13.407607	12.527186	12.939763	11.474158	11.474266	11.474246
<b>ARE</b>	3.420616	3.195998	3.301257	2.927344	2.927372	2.927367
<b>EABS</b>	0.175347	0.175371	0.182641	0.156240	0.156270	0.156246
<b>SUM</b>	4.960061	3.819887	3.921714	3.637254	3.636220	3.637090
<b>40 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.499990	2.447848	2.443162	3.001619	3.019033	3.018281
<b>q<sub>e</sub></b>	2.207216	0.495838	0.495358	0.486549	0.485737	0.485773
<b>R<sup>2</sup><sub>adj</sub></b>	-653.462936	0.922468	0.922612	0.908845	0.909184	0.909171
<b>ERRSQ</b>	27.900937	0.002959	0.002964	0.003568	0.003594	0.003593
<b>HYBRID</b>	583.445654	0.076893	0.076800	0.094278	0.094537	0.094524
<b>MPSD</b>	1330.936951	11.711793	11.704401	8.888691	8.879497	8.873005
<b>ARE</b>	339.555268	2.987971	2.986085	2.267727	2.265382	2.263725
<b>EABS</b>	18.843800	0.147816	0.147486	0.111368	0.111223	0.111123
<b>SUM</b>	5.000000	0.025681	0.025653	0.019557	0.019536	0.019521



Table 3 D (continued). Pseudo-second order kinetic parameters determined by different error functions for removal of cadmium by nano crystalline zirconia

50 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	0.431369	4.277685	4.535515	6.165145	5.729535	3.616794
$q_e$	2.179091	0.407283	0.404446	0.394653	0.395486	0.411033
$R^2_{adj}$	-1814.410196	0.787907	0.810447	0.827700	0.846134	0.742086
<b>ERRSQ</b>	28.016592	0.004621	0.004656	0.005540	0.005301	0.004924
<b>HYBRID</b>	684.606251	0.113289	0.112386	0.129953	0.123384	0.125720
<b>MPSD</b>	1545.422783	15.455880	15.112326	14.469582	14.562939	15.465175
<b>ARE</b>	394.275963	3.943181	3.855532	3.691552	3.715370	3.945552
<b>EABS</b>	18.804130	0.183900	0.180875	0.177633	0.178180	0.182396
<b>SUM</b>	5.000000	0.030112	0.029507	0.028560	0.028692	0.030073
60 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	0.485604	1.650022	1.877070	2.071251	1.788214	1.746596
$q_e$	1.006216	0.451386	0.442267	0.426546	0.432874	0.433933
$R^2_{adj}$	-50.236067	0.859851	0.891164	0.939947	0.910866	0.904061
<b>ERRSQ</b>	2.026380	0.007791	0.008019	0.009966	0.010013	0.010083
<b>HYBRID</b>	48.387240	0.196330	0.189969	0.220698	0.237153	0.241875
<b>MPSD</b>	402.029509	22.301652	21.807106	18.741811	18.768942	18.764552
<b>ARE</b>	102.567772	5.689708	5.563538	4.781504	4.788426	4.787306
<b>EABS</b>	4.929130	0.260784	0.259516	0.229736	0.226122	0.225461
<b>SUM</b>	5.000000	0.171754	0.169018	0.149323	0.149088	0.149064
70 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_2$	2.654376	3.245763	3.313450	3.508510	3.522201	3.538841
$q_e$	0.456552	0.448717	0.447791	0.446817	0.446330	0.445742
$R^2_{adj}$	0.948842	0.981517	0.982462	0.978243	0.979330	0.980503
<b>ERRSQ</b>	0.000994	0.000483	0.000487	0.000572	0.000569	0.000569
<b>HYBRID</b>	0.029048	0.011570	0.011438	0.013179	0.013052	0.012988
<b>MPSD</b>	7.251265	5.144831	5.058836	4.702796	4.709531	4.717595
<b>ARE</b>	1.849979	1.312575	1.290635	1.199801	1.201519	1.203576
<b>EABS</b>	0.083112	0.064508	0.064275	0.062243	0.062460	0.062721
<b>SUM</b>	5.000000	3.078772	3.052540	3.074417	3.071625	3.075321

**Table 4 A. Langmuir isotherm parameters determined by different error functions for removal of cadmium by nano crystalline iron oxide/ hydroxide**

<b>20 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	9.178522	8.819844	8.788571	8.971476	8.972358	8.972829
<b>b</b>	1.415303	2.355058	2.418447	2.419003	2.417793	2.415995
<b>R<sup>2</sup><sub>adj</sub></b>	0.156448	0.540342	0.538852	0.427375	0.426668	0.426733
<b>ERRSQ</b>	0.910224	0.495988	0.497595	0.617883	0.618647	0.618577
<b>HYBRID</b>	4.149926	2.127358	2.120922	2.704243	2.707651	2.707359
<b>MPSD</b>	13.142910	9.113284	9.021678	8.005993	8.005709	8.010597
<b>ARE</b>	4.552838	3.156934	3.125201	2.773357	2.773259	2.774952
<b>EABS</b>	1.722678	1.245360	1.237135	1.087552	1.087420	1.087991
<b>SUM</b>	5.000000	3.167252	3.148753	3.180075	3.181615	3.182543
<b>30 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	9.159187	8.779024	8.749236	8.863209	8.838112	8.883791
<b>b</b>	1.527206	2.739805	2.815313	2.915544	2.958728	2.880950
<b>R<sup>2</sup><sub>adj</sub></b>	-0.008331	0.526614	0.525081	0.462223	0.475731	0.449150
<b>ERRSQ</b>	1.047284	0.491673	0.493265	0.558552	0.544522	0.572130
<b>HYBRID</b>	4.773990	2.087798	2.081423	2.411674	2.344568	2.474873
<b>MPSD</b>	13.642812	8.942603	8.847326	7.876378	7.879506	7.874116
<b>ARE</b>	4.726009	3.097809	3.064804	2.728457	2.729541	2.727674
<b>EABS</b>	1.790012	1.230085	1.221293	1.084833	1.088059	1.082227
<b>SUM</b>	5.000000	2.904958	2.886264	2.799207	2.774015	2.823623
<b>40 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	9.465215	8.992000	8.958779	9.063548	9.065119	9.062890
<b>b</b>	1.612484	3.201859	3.302613	3.470649	3.448899	3.479488
<b>R<sup>2</sup><sub>adj</sub></b>	-0.182791	0.572770	0.571061	0.517054	0.519726	0.515966
<b>ERRSQ</b>	1.480047	0.534600	0.536739	0.604319	0.600975	0.605680
<b>HYBRID</b>	6.747769	2.218136	2.209677	2.542312	2.528194	2.548063
<b>MPSD</b>	14.044500	9.025373	8.963372	8.007822	8.047526	7.991925
<b>ARE</b>	4.865158	3.126481	3.105003	2.773991	2.787745	2.768484
<b>EABS</b>	1.835950	1.267457	1.265922	1.128979	1.133581	1.127141
<b>SUM</b>	5.000000	2.665535	2.656062	2.540353	2.544163	2.538860

**Table 4 A (continued). Langmuir isotherm parameters determined by different error functions for removal of cadmium by nano crystalline iron oxide/ oxide hydroxide**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	10.109180	9.207785	9.149799	8.768906	8.921245	10.529087
<b>b</b>	3.059696	87.446158	90.731335	117.797714	106.864862	1.640053
<b>R<sup>2</sup><sub>adj</sub></b>	-16.819503	0.075194	0.069268	-0.264837	-0.069614	-19.738547
<b>ERRSQ</b>	39.033977	2.025806	2.038786	2.770650	2.343011	45.428200
<b>HYBRID</b>	173.218426	7.529880	7.482503	9.531153	8.219586	201.917537
<b>MPSD</b>	58.629187	17.657378	17.525816	16.830266	16.970596	57.458997
<b>ARE</b>	20.309746	6.116695	6.071121	5.830175	5.878787	19.904380
<b>EABS</b>	7.850088	2.765180	2.762656	2.767937	2.747953	7.607190
<b>SUM</b>	4.717113	1.036475	1.031716	1.034918	1.021250	4.929140
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	10.095900	9.669619	9.639493	9.953582	9.850567	9.976930
<b>b</b>	4.220281	10.094534	10.356056	9.563112	10.074380	9.575626
<b>R<sup>2</sup><sub>adj</sub></b>	-0.752199	0.711319	0.710140	0.581420	0.646151	0.556073
<b>ERRSQ</b>	3.729076	0.614380	0.616888	0.890833	0.753071	0.944777
<b>HYBRID</b>	16.278299	2.234922	2.225664	3.364764	2.825366	3.571888
<b>MPSD</b>	21.997269	10.178755	10.112181	9.256860	9.306055	9.402741
<b>ARE</b>	7.620078	3.526024	3.502962	3.206670	3.223712	3.257205
<b>EABS</b>	3.041846	1.599128	1.598933	1.415978	1.448426	1.440957
<b>SUM</b>	5.000000	1.753214	1.747201	1.752728	1.697789	1.801393
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>Q<sub>o</sub></b>	10.070490	9.813071	9.791033	10.046016	10.009720	9.988972
<b>b</b>	5.896674	10.781385	10.943496	10.102361	10.244551	10.327591
<b>R<sup>2</sup><sub>adj</sub></b>	0.079861	0.778063	0.777512	0.705648	0.725273	0.735074
<b>ERRSQ</b>	2.071456	0.499633	0.500874	0.662657	0.618476	0.596412
<b>HYBRID</b>	8.733243	1.790247	1.785848	2.450360	2.282211	2.197205
<b>MPSD</b>	18.231698	7.648514	7.652504	6.949808	7.027686	7.072076
<b>ARE</b>	6.315646	2.649523	2.650905	2.407484	2.434462	2.449839
<b>EABS</b>	2.601482	1.235360	1.242214	1.088375	1.107792	1.118873
<b>SUM</b>	5.000000	1.760094	1.763262	1.781232	1.756657	1.745401

**Table 4 B. Freundlich isotherm parameters determined by different error functions for removal of cadmium by nano crystalline iron oxide/hydroxide**

20 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	6.725584000	0.935814130	0.942871802	0.877654809	1.113323418	0.760509209
$1/n$	0.10034000	0.86533039	0.87490699	0.86652438	0.68309825	1.00000000
$R^2_{adj}$	-66.960562054	-60.205382248	-60.290378163	-61.106248349	-61.106248438	-61.106251168
ERRSQ	73.331975439	66.042885051	66.134598806	67.014953097	67.014953194	67.014956139
HYBRID	325.223121782	290.616505747	290.260859924	296.701651304	296.701651796	296.701666724
MPSD	122.339132737	119.650054768	120.807382737	115.882259433	115.882259618	115.882265245
ARE	42.379518731	41.447994797	41.848904966	40.142792207	40.142792271	40.142794220
EABS	16.275011207	16.099204870	16.293439330	15.466855395	15.466855418	15.466856123
SUM	5.000000000	4.739429361	4.770440999	4.670945834	4.670945841	4.670946062
30 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	6.836440000	0.873723829	0.945715622	0.891657490	0.885369223	0.920820977
$1/n$	0.094300034	0.930938694	0.875735482	0.852916401	0.858974147	0.825903531
$R^2_{adj}$	-75.979525197	-65.148870662	-65.232373139	-66.212705712	-66.212706680	-66.212705736
ERRSQ	79.953316905	68.704263963	68.790992220	69.809195966	69.809196971	69.809195991
HYBRID	352.962880617	301.807423697	301.471938718	308.476471275	308.476476254	308.476471401
MPSD	125.869788703	121.510510872	122.671995390	117.364782341	117.364784108	117.364782386
ARE	43.602573834	42.092475697	42.494825736	40.656353207	40.656353819	40.656353222
EABS	16.764055228	16.388317854	16.581788342	15.697756670	15.697756891	15.697756675
SUM	5.000000000	4.622693446	4.652823827	4.548341376	4.548341444	4.548341378
40 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	7.035500000	0.910790417	0.929138149	0.899953852	0.899953852	0.899953654
$1/n$	0.0978899814	1.000000000	1.000000000	1.000000000	1.000000000	1.000000000
$R^2_{adj}$	-70.946079202	-58.023191305	-58.111394459	-58.053959546	-58.053959546	-58.053960671
ERRSQ	90.027387440	73.856751758	73.967121908	73.895252596	73.895252596	73.895254003
HYBRID	390.729365337	320.068515753	319.654619723	320.701808490	320.701808490	320.701822700
MPSD	132.548819294	120.828851480	122.099866790	120.078181750	120.078181750	120.078193440
ARE	45.916257900	41.856341957	42.296634576	41.596302334	41.596302334	41.596306384
EABS	17.968067241	16.516428206	16.737975231	16.385580703	16.385580703	16.385582186
SUM	5.000000000	4.381907515	4.413582299	4.365347053	4.365347053	4.365347364

**Table 4 B (continued). Freundlich isotherm parameters determined by different error functions for removal of cadmium by nano crystalline iron oxide/ oxide hydroxide**

50 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	8.496303000	1.319686094	1.344791505	1.662777270	1.662777270	1.662776481
$1/n$	0.04914000	1.00000000	1.00000000	1.00000000	1.00000000	1.00000000
$R^2_{adj}$	-108.649341916	-46.622969682	-46.671001255	-55.593358011	-55.593358011	-55.593316741
ERRSQ	240.189067462	104.319063642	104.424277760	123.968877949	123.968877949	123.968787547
HYBRID	927.350757717	432.928381206	432.565698704	490.750180340	490.750180340	490.749891518
MPSD	229.425317035	140.984918627	140.371969501	132.608340762	132.608340762	132.608360031
ARE	79.475261129	48.838608433	48.626276627	45.936876742	45.936876742	45.936883417
EABS	34.503817329	20.393026254	20.319342749	19.386065660	19.386065660	19.386067977
SUM	5.000000000	2.721228379	2.713796470	2.763183456	2.763183456	2.763183003
60 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	8.280947000	1.324180670	1.347842510	1.663098204	1.663229271	1.666171547
$1/n$	0.07948001	1.00000000	1.00000000	1.00000000	0.99992189	0.99815597
$R^2_{adj}$	-91.383882741	-58.702643914	-58.743894757	-67.165635012	-67.165692920	-67.165678630
ERRSQ	196.613839113	127.060756454	127.148547596	145.071919447	145.072042689	145.072012276
HYBRID	769.549649003	515.549501685	515.250167420	568.385719608	568.386110479	568.386014021
MPSD	202.846420245	155.354021448	155.035040117	150.785130562	150.785114930	150.785118788
ARE	70.268061200	53.816211662	53.705713287	52.233501432	52.233496017	52.233497353
EABS	30.366995624	22.769055413	22.735521616	22.288738095	22.288736451	22.288736857
SUM	5.000000000	3.597718316	3.593526522	3.697118861	3.697119788	3.697119559
70 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$K_F$	8.452010000	1.340221952	1.360371940	1.964348602	2.036562729	0.986199043
$1/n$	0.07662002	1.00000000	1.00000000	1.00000000	0.96454109	0.98889769
$R^2_{adj}$	-95.210682554	-64.112229208	-64.138549287	-89.363493482	-89.363479213	-72.747118539
ERRSQ	216.593527455	146.583383781	146.642636647	203.430089952	203.430057829	166.022609131
HYBRID	834.810787651	583.843950006	583.643223965	763.984154933	763.984049624	656.967980955
MPSD	210.619718405	170.348937883	170.305996304	169.018863500	169.018863875	171.126728588
ARE	72.960810671	59.010603086	58.995727686	58.549851804	58.549851934	59.280037689
EABS	31.890250658	25.362729627	25.367325840	25.505092916	25.505092876	25.279479514
SUM	5.000000000	3.789050140	3.788819624	4.259127880	4.259127608	3.971168693

**Table 4 C. Pseudo-first order kinetic parameters determined by different error functions for removal of cadmium by iron oxide/ hydroxide**

<b>20 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.232258	1.477969	1.518913	1.639481	1.702439	1.621277
<b>q<sub>e</sub></b>	1.438401	4.740006	4.723540	4.848494	4.778288	4.870045
<b>R<sup>2</sup><sub>adj</sub></b>	-128.461349	0.382212	0.379762	0.216498	0.323911	0.166078
<b>ERRSQ</b>	189.678128	0.905141	0.908731	1.147935	0.990560	1.221807
<b>HYBRID</b>	315.572059	1.563954	1.557937	2.035607	1.732173	2.170324
<b>MPSD</b>	319.955022	20.073321	20.174124	18.945185	18.865049	18.966439
<b>ARE</b>	76.907616	4.825026	4.849256	4.553856	4.534593	4.558965
<b>EABS</b>	53.333037	3.277270	3.309241	3.046399	3.078947	3.035899
<b>SUM</b>	5.000000	0.196653	0.197882	0.188047	0.186365	0.188799
<b>30 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.261206	1.561067	1.590424	1.749198	1.786425	1.759464
<b>q<sub>e</sub></b>	1.053222	4.822646	4.812069	4.888296	4.856178	4.883054
<b>R<sup>2</sup><sub>adj</sub></b>	-203.207765	0.462944	0.461576	0.356578	0.400136	0.363809
<b>ERRSQ</b>	229.498694	0.603570	0.605108	0.723110	0.674157	0.714983
<b>HYBRID</b>	373.304363	1.051180	1.048655	1.275347	1.183333	1.260469
<b>MPSD</b>	344.398591	14.548979	14.853221	11.863091	12.580188	11.920730
<b>ARE</b>	82.783119	3.497139	3.570270	2.851532	3.023901	2.865387
<b>EABS</b>	58.660910	2.383145	2.443390	1.914156	2.054172	1.927061
<b>SUM</b>	5.000000	0.130561	0.133355	0.108090	0.114181	0.108569
<b>40 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>1</sub></b>	0.223644	2.031740	2.046810	2.142038	2.141502	2.136368
<b>q<sub>e</sub></b>	0.725805	4.856745	4.852725	4.866797	4.867159	4.870498
<b>R<sup>2</sup><sub>adj</sub></b>	-553.205601	0.497238	0.496767	0.482676	0.482429	0.479856
<b>ERRSQ</b>	272.631756	0.247325	0.247557	0.254489	0.254610	0.255876
<b>HYBRID</b>	436.676889	0.402965	0.402593	0.416005	0.416258	0.418826
<b>MPSD</b>	369.393544	9.246652	9.356882	8.697901	8.697935	8.698781
<b>ARE</b>	88.791158	2.222618	2.249115	2.090715	2.090723	2.090927
<b>EABS</b>	63.945852	1.586240	1.607476	1.495293	1.495188	1.494295
<b>SUM</b>	5.000000	0.076700	0.077629	0.072363	0.072362	0.072363

Table 4 C (continued). Pseudo-first order kinetic parameters determined by different error functions for removal of cadmium by iron oxide/ oxide hydroxide

50 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.348306	1.972989	1.983885	2.084938	2.068707	2.069824
$q_e$	0.636136	4.926241	4.923366	4.960478	4.976243	4.975440
$R^2_{adj}$	-601.782960	0.607912	0.607655	0.548151	0.505719	0.508136
<b>ERRSQ</b>	282.288353	0.183618	0.183739	0.211605	0.231476	0.230344
<b>HYBRID</b>	445.716613	0.309441	0.309249	0.358183	0.391280	0.389413
<b>MPSD</b>	370.627497	6.921924	6.967191	5.685974	5.660611	5.660827
<b>ARE</b>	89.087763	1.663824	1.674704	1.366738	1.360642	1.360694
<b>EABS</b>	65.062232	1.180964	1.190155	0.964557	0.957337	0.957533
<b>SUM</b>	5.000000	0.056848	0.057234	0.047061	0.046958	0.046954
60 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.535954	1.713677	1.983885	2.084938	2.068707	1.797467
$q_e$	1.370566	4.929627	4.923366	4.960478	4.976243	4.981371
$R^2_{adj}$	-290.680438	0.771150	0.770851	0.739355	0.692489	0.691381
<b>ERRSQ</b>	196.137632	0.153888	0.154089	0.175268	0.206783	0.207528
<b>HYBRID</b>	311.254617	0.256277	0.309249	0.291732	0.344239	0.345463
<b>MPSD</b>	310.385916	6.832148	6.858113	5.869230	5.657693	5.656200
<b>ARE</b>	74.607489	1.642244	1.648485	1.410787	1.359940	1.359581
<b>EABS</b>	54.240441	1.162800	1.169730	1.003857	0.959932	0.959609
<b>SUM</b>	5.000000	0.067069	0.067536	0.058157	0.056314	0.056306
70 mg/l	LTFM	ERRSQ	HYBRID	MPSD	ARE	EABS
$k_1$	0.261114	2.270661	2.277328	2.353420	2.349446	2.349493
$q_e$	0.174590	4.964477	4.962933	4.988797	4.990890	4.990836
$R^2_{adj}$	-1278.923555	0.620403	0.620276	0.573859	0.568223	0.568387
<b>ERRSQ</b>	344.246238	0.102096	0.102130	0.114614	0.116130	0.116086
<b>HYBRID</b>	537.243094	0.169314	0.169261	0.190593	0.193081	0.193009
<b>MPSD</b>	404.513103	3.949302	4.009674	2.891705	2.871447	2.871607
<b>ARE</b>	97.232849	0.949294	0.963806	0.695079	0.690210	0.690249
<b>EABS</b>	71.839473	0.679175	0.690345	0.492194	0.488342	0.488374
<b>SUM</b>	5.000000	0.029592	0.030046	0.021836	0.021691	0.021692

**Table 4 D. Pseudo-second order kinetic parameters determined by different error functions for removal of cadmium by iron oxide/ oxide hydroxide**

<b>20 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.342145	0.550210	0.570419	0.422719	0.425779	0.427007
<b>q<sub>e</sub></b>	5.129520	4.987197	4.973184	5.093321	5.089145	5.086839
<b>R<sup>2</sup><sub>adj</sub></b>	0.985960	0.992551	0.992518	0.990608	0.990735	0.990794
<b>ERRSQ</b>	0.512523	0.271917	0.273142	0.342847	0.338196	0.336052
<b>HYBRID</b>	0.987011	0.481769	0.479647	0.639116	0.630133	0.626124
<b>MPSD</b>	8.906907	9.641302	9.880146	8.512332	8.509217	8.510499
<b>ARE</b>	2.299753	2.489373	2.551043	2.197875	2.197070	2.197402
<b>EABS</b>	1.450775	1.669005	1.718904	1.421445	1.422876	1.424027
<b>SUM</b>	4.647002	3.941278	4.018896	3.866534	3.848559	3.841243
<b>30 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.556448	0.648153	0.659667	0.692810	0.707581	0.691245
<b>q<sub>e</sub></b>	5.070480	5.032669	5.026120	5.052121	5.046712	5.052712
<b>R<sup>2</sup><sub>adj</sub></b>	0.995305	0.995808	0.995800	0.995186	0.995135	0.995191
<b>ERRSQ</b>	0.170129	0.151912	0.152189	0.174435	0.176308	0.174274
<b>HYBRID</b>	0.308945	0.269129	0.268664	0.308219	0.311245	0.307965
<b>MPSD</b>	6.004263	6.359106	6.499394	5.694426	5.729744	5.698186
<b>ARE</b>	1.550294	1.641914	1.678136	1.470294	1.479414	1.471265
<b>EABS</b>	1.022937	1.100210	1.128424	0.971653	0.979873	0.972221
<b>SUM</b>	4.722986	4.668197	4.736467	4.604570	4.643185	4.604489
<b>40 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	0.715079	1.073204	1.087236	0.879715	0.880095	0.879451
<b>q<sub>e</sub></b>	5.059961	4.994153	4.991287	5.040067	5.039869	5.040206
<b>R<sup>2</sup><sub>adj</sub></b>	0.996157	0.998573	0.998571	0.998063	0.998066	0.998061
<b>ERRSQ</b>	0.138029	0.051256	0.051326	0.069584	0.069475	0.069660
<b>HYBRID</b>	0.243125	0.084324	0.084208	0.118977	0.118791	0.119108
<b>MPSD</b>	4.449628	3.884584	3.908478	3.479631	3.479219	3.479927
<b>ARE</b>	1.148889	1.002995	1.009165	0.898437	0.898330	0.898513
<b>EABS</b>	0.781008	0.711808	0.717175	0.621800	0.621764	0.621827
<b>SUM</b>	5.000000	3.375602	3.393239	3.353650	3.351867	3.354907



**Table 4 D (continued). Pseudo-second order kinetic parameters determined by different error functions for removal of cadmium by iron oxide/ oxide hydroxide**

<b>50 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	1.361301	1.106393	1.107390	1.230498	1.227507	1.235431
<b>q<sub>e</sub></b>	5.032966	5.054675	5.053964	5.047478	5.048975	5.045022
<b>R<sup>2</sup><sub>adj</sub></b>	0.998463	0.998885	0.998885	0.998738	0.998733	0.998743
<b>ERRSQ</b>	0.055398	0.040181	0.040186	0.045495	0.045674	0.045290
<b>HYBRID</b>	0.094474	0.067990	0.067982	0.077348	0.077669	0.076962
<b>MPSD</b>	2.590319	2.671769	2.678088	2.291019	2.291428	2.290349
<b>ARE</b>	0.668818	0.689848	0.691479	0.591539	0.591644	0.591366
<b>EABS</b>	0.466551	0.484646	0.485862	0.417060	0.417077	0.417032
<b>SUM</b>	4.894707	4.437762	4.444994	4.209287	4.216261	4.200959
<b>60 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	1.298086	0.864691	0.864367	0.887372	0.887316	0.886706
<b>q<sub>e</sub></b>	5.033979	5.085253	5.085159	5.078186	5.078233	5.078540
<b>R<sup>2</sup><sub>adj</sub></b>	0.997682	0.999660	0.999660	0.999649	0.999649	0.999650
<b>ERRSQ</b>	0.084004	0.012331	0.012332	0.012726	0.012723	0.012696
<b>HYBRID</b>	0.148381	0.019733	0.019732	0.020401	0.020396	0.020354
<b>MPSD</b>	3.903417	1.875416	1.875610	1.793901	1.793820	1.796571
<b>ARE</b>	1.007858	0.484230	0.484280	0.463183	0.463162	0.463873
<b>EABS</b>	0.687706	0.351682	0.351684	0.337804	0.337785	0.338271
<b>SUM</b>	5.000000	1.752075	1.752179	1.699332	1.699186	1.700710
<b>70 mg/l</b>	<b>LTFM</b>	<b>ERRSQ</b>	<b>HYBRID</b>	<b>MPSD</b>	<b>ARE</b>	<b>EABS</b>
<b>k<sub>2</sub></b>	2.720534	1.566975	1.561585	1.662655	1.660936	1.659246
<b>q<sub>e</sub></b>	5.019324	5.057229	5.057161	5.052114	5.052760	5.053112
<b>R<sup>2</sup><sub>adj</sub></b>	0.997705	0.999025	0.999025	0.999003	0.999003	0.999003
<b>ERRSQ</b>	0.082447	0.035011	0.035018	0.035816	0.035826	0.035820
<b>HYBRID</b>	0.138039	0.056848	0.056838	0.058398	0.058426	0.058419
<b>MPSD</b>	3.063138	2.670083	2.684626	2.465896	2.462399	2.462863
<b>ARE</b>	0.790899	0.689412	0.693167	0.636691	0.635789	0.635909
<b>EABS</b>	0.555456	0.500271	0.502959	0.462522	0.461817	0.461922
<b>SUM</b>	5.000000	3.480496	3.494833	3.300197	3.296978	3.297349

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# *Forwarded*

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## Undertaking from the Candidate

*I, Deepak Gusain, research scholar under the supervision of Prof. Y.C. Sharma, Department of Chemistry, IIT (BHU) Varanasi give undertaking that the thesis entitled "Synthesis and characterization of some nano adsorbents and their application in removal of selected metallic pollutants from aqueous solutions" submitted by me for the degree of Doctor of Philosophy is a record of first-hand research work carried out by me during the period of study.*

*I avail myself to responsibility such as an act will be taken on the behalf of me, mistakes, errors of facts, and misinterpretation are of course entirely my own.*

*Date.....*

*Place: Varanasi*

*(Deepak Gusain)*

## ANNEXURE-E

### **Candidate's Declaration**

*I, Deepak Gusain, certify that the work embodies in this Ph.D. thesis is my own bonafide work carried out by me under the supervision of Prof. Y. C. Sharma, Department of Chemistry, IIT (BHU) Varanasi for a period of approximately 5 years and 2 months from (March, 2011 to May, 2016) at Indian Institute of Technology (Banaras Hindu University), Varanasi. The matter embodied in this Ph.D. thesis has not been submitted for the award of any other degree / diploma.*

*I declare that I have faithfully acknowledged, given credit to and referred to the research workers wherever their works have been cited in the text and the body of the thesis. I further certify that I have not willfully lifted up some other's works, para, text, data, results, etc. reported in the journals, books, magazines, reports, dissertations, thesis, etc., or available at websites and included them in this Ph.D. thesis and cited as my own work.*

*Date:*

*Place : Varanasi*

*(Deepak Gusain)*

---

### **Certificate from the Supervisor/Co-supervisor**

*This is to certify that the above statement made by the candidate is correct to the best of our knowledge.*

*(Prof. V. K. Singh)*  
*Co-supervisor*

*(Prof. Y. C. Sharma)*  
*Supervisor*

*(Prof. R. B. Rastogi)*  
*Head*

**PRE SUBMISSION SEMINAR COMPLETION**

**CERTIFICATE**

*This is to certify that Mr. Deepak Gusain, a bonafide research scholar of Department of Chemistry, Indian Institute of Technology (Banaras Hindu University) Varanasi, has successfully completed the pre-submission seminar requirement on the topic "Synthesis and characterization of some nano adsorbents and their application in removal of selected metallic pollutants from aqueous solutions" on dated 19-05-2016 which is a part of this Ph.D. programme.*

*Date:*

*(Prof. Y. C. Sharma)*

*(Prof. R. B. Rastogi)*

*Place: Varanasi*

*Supervisor*

*Head*

**Course Work / Comprehensive Examination / Pre  
Submission Seminar Completion Certificate**

*This is to certify that Mr. Deepak Gusain, a bonafide research scholar of Department of Chemistry, Indian Institute of Technology (Banaras Hindu University), Varanasi has successfully completed the course work / comprehensive examination / pre-submission seminar requirement which is a part of his Ph.D. programme.*

*Date:*

*Place: Varanasi*

*Head  
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Varanasi*

## Copyright Transfer Certificate

**Title of the Thesis:** “Synthesis and characterization of some nano adsorbents and their application in removal of selected metallic pollutants from aqueous solutions”.

**Candidate’s Name:** Deepak Gusain

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**(Deepak Gusain)**

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## List of Symbols

$\epsilon_r$	Error of prediction in regression equation
$^\circ$	Degree for measurement of plane angle
<b>A</b>	Arrhenius factor
$\text{\AA}$	Angstrom
<b>A<sub>1</sub></b>	Constant ( $0.509 \text{ mol}^{-1/2} \text{ kg}^{1/2}$ )
<b>AAS</b>	Atomic absorption spectroscopy
<b>AdjMS</b>	Adjusted mean squares
<b>AdjSS</b>	Adjusted sum of squares
<b>ANOVA</b>	Analysis of variance
<b>ARE</b>	Average relative error
<b>b</b>	Langmuir constant
<b>B</b>	Calculable mathematical function of F (fractional attainment)
<b>BBD</b>	Box-Behnken design
<b>Bt</b>	Calculable mathematical function of F(t) at different time t
<b>ca.</b>	Circa or approximately
<b>CCD</b>	Central composite design
<b>CCF</b>	Face centered central composite design
<b>C<sub>e</sub></b>	Concentration of adsorbate at equilibrium
<b>C<sub>i</sub></b>	Initial concentration of adsorbate
<b>C<sub>b</sub></b>	Intercept of Boyd plot
<b>C<sub>s</sub></b>	Concentration of adsorbate in solid
<b>cm<sup>-1</sup></b>	Wavenumber
<b>cm<sup>3</sup>/g</b>	Centimeter cubed per gram
<b>Coef</b>	Coefficient
<b>Conc.</b>	Concentration
<b>C<sub>w</sub></b>	Concentration of adsorbate in liquid
<b>DF</b>	Degree of freedom
<b>D<sup>i</sup></b>	Effective diffusion constant
<b>DTA</b>	Differential thermal analysis
<b>E<sub>a</sub></b>	Activation energy
<b>EABS</b>	The sum of the absolute errors
<b>emu/g</b>	Magnetization per gram
<b>ERRSQ</b>	The sum of the square of the errors
<b>eV</b>	Electron volt
<b>F</b>	F Value by dividing the factor mean square by the error of mean square
<b>F(t)</b>	Fractional attainment at time t

<b>FTIR</b>	Fourier transform infrared spectroscopy
<b>g</b>	Gram
<b>g L<sup>-1</sup></b>	Gram per litre
<b>h</b>	Hour
<b>HYBRID</b>	Hybrid fractional error function
<b>IARC</b>	International agency for research on cancer
<b>I<sub>e</sub></b>	Ionic strength
<b>K</b>	Kelvin
<b>k</b>	Number of factors
<b>k<sub>1</sub></b>	Pseudo- first order rate constant
<b>k<sub>2</sub></b>	Pseudo- second order rate constant
<b>k<sub>diff</sub></b>	Intraparticle diffusion rate constant
<b>K<sub>F</sub></b>	Freundlich constant
<b>kg</b>	Kilogram
<b>kJ mol<sup>-1</sup></b>	Kilo Joule per mole
<b>kJ mol<sup>-1</sup> K<sup>-1</sup></b>	Kilo Joule per mole per kelvin
<b>K<sub>L</sub></b>	Thermodynamic equilibrium constant
<b>km<sup>3</sup></b>	Cubic kilometer
<b>K<sub>p</sub> or K<sub>c</sub></b>	Thermodynamic equilibrium constant derived from partition method
<b>L</b>	Litre
<b>LTFM</b>	Linear transform
<b>M</b>	Molar
<b>m<sup>2</sup>/g</b>	Square meters per gram
<b>mg</b>	Milligram
<b>mg L<sup>-1</sup></b>	Milligram per litre
<b>min</b>	Minute
<b>mol</b>	mole
<b>MPSD</b>	Maquardt percent standard deviation
<b>MS</b>	Mean square
<b>N</b>	Number of runs
<b>NTP</b>	National toxicology program
<b>nm</b>	Nanometer
<b>n<sub>0</sub></b>	Number of central runs
<b>OEHHA</b>	Office of environmental health hazard assessment
<b>p</b>	p value or calculated probability
<b>pH<sub>zpc</sub></b>	pH at zero point of charge
<b>PRESS</b>	Predicted sum of squares

<b>q<sub>e</sub></b>	Amount of adsorbate adsorbed on per unit gram of adsorbent at equilibrium
<b>Q<sub>o</sub></b>	Langmuir constant
<b>q<sub>t</sub></b>	Amount of adsorbate adsorbed at time t in per unit gram of adsorbent
<b>r</b>	Radius of the particle
<b>R</b>	Gas constant (8.314 J mol <sup>-1</sup> K <sup>-1</sup> )
<b>R<sup>2</sup></b>	Coefficient of determination
<b>R<sup>2</sup><sub>adj</sub></b>	Adjusted coefficient of determination
<b>rpm</b>	Rotations per minute
<b>RSM</b>	Response surface methodology
<b>R-Sq(pred)</b>	Predicted coefficient of determination
<b>S</b>	Square root of error mean square
<b>SE Coef</b>	Standard error of coefficient
<b>SEM</b>	Scanning electron microscope
<b>Seq SS</b>	Sequential sum of squares
<b>SS</b>	Sum of squares
<b>t</b>	Time
<b>T</b>	Temperature
<b>TEM</b>	Transmission electron microscope
<b>Temp.</b>	Temperature
<b>TGA</b>	Thermogravimetric analysis
<b>USEPA</b>	United states environmental protection agency
<b>V</b>	Volume
<b>W</b>	Weight
<b>W<sub>1</sub></b>	Full width at half maxima
<b>WHO</b>	World health organization
<b>X1</b>	Variable studied in RSM
<b>X2</b>	Variable studied in RSM
<b>X3</b>	Variable studied in RSM
<b>X4</b>	Variable studied in RSM
<b>X<sub>i</sub></b>	Coded in dependent process variable
<b>X<sub>j</sub></b>	Coded independent process variable
<b>XPS</b>	X-ray photoelectron spectroscopy
<b>XRD</b>	X-ray diffraction
<b>z</b>	Charge on ion
<b>β<sub>0</sub></b>	Offset term in regression equation
<b>β<sub>i</sub></b>	Linear effect in regression equation

$\beta_{ii}$	Square effect in regression equation
$\beta_{ij}$	Interaction effect in regression equation
$\gamma_e$	Activity coefficient
$\Delta G^\circ$	Change in standard free energy
$\Delta H^\circ$	Change in standard enthalpy
$\Delta S^\circ$	Change in standard entropy
$\theta$	Plane angle
$\theta/s$	Plane angle per second
$\lambda$	Wavelength of X-ray
$\pi$	Mathematical constant