# **5.1 Introduction**

In chapters 3 and 4, we studied the different interesting properties of Cu doped Bi<sub>2</sub>Te<sub>3</sub>, effect of another non magnetic element Zn in the Bi<sub>2</sub>Te<sub>3</sub> has been discussed in this chapter.  $A_2B_3$  (A=Bi, Sb, B= Te, Se) type of materials are very important as thermoelectric (TE) devices since they have large thermoelectric power and therefore they are considered as a promising means of energy saving and power generation. These devices use two types of materials viz. n type and p type, connected in series. The efficiency of a TE materials can be evaluated by the dimensionless figure of merit,  $ZT = \{(\sigma s^2) T/\kappa\}$  where  $\sigma$ , s, T and  $\kappa$  are the electrical conductivity, Seebeck coefficient, temperature and thermal conductivity of the materials. Significant efforts have been made for increasing the thermoelectric figure of merit values in several material classes, including silicides [90], half-Heuslers [91,92], and tellurides (e.g. of Bi [93], Pb [94,95] and Ge [96]). By increasing the power factor (PF)  $=\sigma s^2$ or decreasing the thermal conductivity, we can improve the performance of a TE devices. Mobility of carrier and different scattering mechanisms control the transport properties. Carrier mobility is strongly influenced in presence of magnetic field, which in turn affects the transport properties including resistivity [97-99]. As a matter of fact, Magnetoresistance (MR) of a TE material gives valuable information regarding the mechanism affecting conductivity, and therefore is intimately related to the underlying physics towards obtaining materials with high ZT values. Furthermore, the materials having magnetoresistive response can open a new way for the dispersion and dynamics of the charge carriers which can be exploited for the technical use such as multifunctional electromagnetic applications, mechatronics and disc reading heads [34]. Zero band gap materials exhibit fascinating and superior electronic properties compared to non -zero band gap materials [100]. In zero band

gap materials the energy required to make a transition from valence band to conduction band can be arbitrarily low which leads to finite electrical conductivity under an infinitesimal perturbation. Moreover electrical transport properties such as resistance or conductance are very sensitive to external effect such as pressure, electrical and magnetic fields, is a unique feature in zero band gap materials. Abrikosov [35] has proposed a quantum model for the materials having zero-gap and linear dispersion. According to this model, magnetoresistance (MR) for the zero gap materials should be giant, linear and temperature independent which is ideal for practical applications. Besides these, based on two dimensional random register network Parish and Littlewood (PL) has given a classical model for the explanation of MR in the inhomogeneous system having strong disorder such as  $Ag_{2\pm\delta}Se$  and  $Ag_{2\pm\delta}Te$ , nonmagnetic graphene and InSb system [56-58].

When the TIs are doped by the magnetic element, weak localization (WL) effect is seen and as a result time reversal symmetry (TRS) breaking and surface state band gap opening could be realized [101-103]. Therefore, for the protection of TRS, we have doped nonmagnetic Zn in Bi<sub>2</sub>Te<sub>3</sub> topological insulator. In this chapter, it is reported that the doping of Zn in Bi<sub>2</sub>Te<sub>3</sub> TI is not only increasing the power factor (by enhancing simultaneously electrical conductivity and thermopower) but mobility and magnetoresistance also, and this decoupling of electrical conductivity and thermopower is the more effective way to enhance the thermoelectric power factor. The materials having such type of promising properties may be very useful for the application point of view such as in refrigeration, quantum computing, multifunctional electromagnetic applications, mechatronics and disc reading heads.

# 5.2 Results and Discussion

## 5.2.1 X- ray diffraction Analysis

In order to characterize the obtained single crystals, we performed X- ray diffraction patterns at room temperature shown in Fig. 5.1(a). All diffractions peaks have been exclusively labeled with



**Fig.5.1** (a) Room temperature X-ray diffraction patterns of  $Bi_{2-x}Zn_xTe_3$  (x=0, 0.10, 0.20) single crystals, (b) Variation of lattice parameter with Zn concentration for  $Bi_{2-x}Zn_xTe_3$  (x=0, 0.10, 0.20).

(00L) i.e. (003), (006), (0015), (0018) and (0021) indices, all indexed peak well matched with JCPDS card no-15-0863 with space group R-3m, indicating that the samples were single crystalline and the cleaved surface was the basal plane perpendicular to the c axis without

any secondary phases and impurity. An additional peak around  $2\theta=40^{0}$  for the samples is observed which might be due to the slight misalignment or slight tilt angle of the crystallinity of as cleaved single crystals. Around  $2\theta=54^{0}$  and  $64^{0}$ , a small splitting due to the difference in the wavelength of X-ray source of CuK<sub>a</sub> and CuK<sub>b</sub> radiation is observed.

The lattice parameter a=b obtained from the XRD analysis for the Hexagonal setting was 4.52 Å for x=0, and it slightly decreased with increasing Zn concentration and finally going to 4.42 Å for x=0.20 [shown in Fig. 5.1(b)], because the ionic radius of Zn is smaller than that of Bi, the obtained lattice parameter value well matched with the reported value [31]. In addition, there was shifting of the peaks towards lower angle in Zn-doped samples which might be due to the increase in *c* parameter from 30.43Å (for x=0) to 30.59Å (for x=0.20) as shown in Fig. 5.1(b). The slightly elongated *c* parameter in doped sample could not however compensate the decreased *a* or *b* parameters in maintaining same lattice volume, leading to smaller cell volume. Hence, it was obvious from the change in lattice parameters that the Bi atoms have been successfully substitution by the Zn.

#### **5.2.2 Electrical resistivity Analysis**

The resistivity behavior from 2K to 300K under zero magnetic field for  $Bi_{2-x}Zn_xTe_3$  (x=0, 0.10, 0.20) are displayed in the Fig. 5.2. It is obvious from the graph that the resistivity of doped samples first increases at x=0.10, and then it decreases for x=0.20. The presence of impurity (Zn) in the host material  $Bi_2Te_3$  may be a reason of increasing resistivity in doped sample up to x=0.10. But at the higher concentration at x=0.20, resistivity decreases which might be due to the increase in mobility which will be discussed in next section of this chapter.



**Fig.5.2** Temperature dependence of zero field electrical resistivity for  $Bi_{2-X}Zn_XTe_3$  samples (X=0, 0.10, 0.20) and Inset I is showing the field dependence of magnetization (MH) for  $Bi_{2-X}Zn_XTe_3$ (X=0.10 and 0.20) samples, Inset II is showing magnetization vs. temperature (MT) curve for X=0.10 sample and Inset III is showing MH curve for X=0.10 sample at different temperatures *viz.* 2K, 18K, 56K, 300K.

### 5.2.3 Magnetic Property Analysis

Magnetization (M) as a function of magnetic field (H) of the Zn doped  $Bi_{2-x}Zn_xTe_3$  (x=0.10, 0.20) single crystals was measured at 2K in the field range -2T to 2T in the inset I of Fig. 5.2. It is obvious from the M(H) curve that all the Zn doped  $Bi_2Te_3$  samples show ferromagnetism. It is also observed from M(H) curve that magnetization increases with increase of Zn content to x=0.10 but the value of magnetization decreases for x=0.20 (shown in inset I of Fig.5.2). Local magnetization of Zn atom may be the reason of induced ferromagnetism in our doped samples. We have also shown magnetization as a function of

temperature for x=0.10 (sample with highest magnetization value in the present investigation) in the Inset II of Fig.5.2. The anomaly around 55K may be an indication of local magnetization due to Zn atoms. The M(H) behavior of x=0.10 at different temperatures are shown in inset III Fig.5.2 which shows the evolution of ferromagnetism with temperature.

## **5.2.4 Thermoelectric Analysis**

The variation of thermo power (S) with temperature of the as-grown single crystals of  $Bi_{2-x}Zn_xTe_3$  (x=0, 0.10, 0.20) are also shown in inset of Fig. 5.3 in the temperature range of 2K-300K. The sign of the thermo power is found to be negative, which suggests that the majority of carriers are electrons. The maximum absolute value of S obtained in the case of pure  $Bi_2Te_3$  is 142.8µV/K at 300K, consistent with values reported by Cao et al. [68]. The S value initially increases with doping Zn and with further doping of Zn the value of S remains constant. This might be due to the fact that S is additive in nature. The S attains the maximum value at 227.9µV/K for x=0.20. To determine the efficiency of thermoelectric power we have calculated the power factor (PF) using the formula

### Power Factor= $\sigma S^2$

Where  $\sigma$  is the electrical conductivity and S is the thermopower. Variation of PF with temperature for the Bi<sub>2-x</sub>Zn<sub>x</sub>Te<sub>3</sub> (x=0, 0.10, 0.20) single crystals is shown in Fig. 5.3. It is observed that with the increase in temperature electrical resistivity increases in pure and x=0.10 doped samples but the increase in S is much larger than the increase of electrical resistivity which gives rise to the increase of power factor with increasing temperature for the x=0.10 sample. In x=0.20 sample further increment in PF is observed. In fact, the convenient route to enhance the PF for TE materials is the use of dopants [104-105]. A lot of work has been done for the enhancement of thermopower and the power factor in Bi<sub>2</sub>Te<sub>3</sub> [106-110].

The reported value of the PF by Na et al in  $Bi_2Te_3$  thin film was  $1.47x10^{-3}$  W/K<sup>2</sup>m [106],whereas Shang have found the value as  $7.08x10^{-4}$  W/K<sup>2</sup>m for the sputtered  $Bi_2Te_3$  thin film [107].The PF achieved by



Fig.5.3 Variation of power factor (PF) as a function of temperature for  $Bi_{2-x}Zn_xTe_3$ . Inset: represents the thermopower of the  $Bi_{2-x}Zn_xTe_3$ .

Bottner et al. was  $1.57 \times 10^{-3}$  W/K<sup>2</sup>m for *n*-type Bi<sub>2</sub>Te<sub>3</sub> materials [108]. The PF value reported by Han et al. was below  $2.4 \times 10^{-3}$  W/K<sup>2</sup>m at room temperature in Bi<sub>2</sub>Te<sub>3-x</sub>Se<sub>x</sub> alloys [109]. Jiang et al have found that it was 2.7 X  $10^{-4}$  W/K<sup>2</sup>m and  $2.2 \times 10^{-4}$  W/K<sup>2</sup>m in *p*-type and *n*type ZnO/Bi<sub>2</sub>Te<sub>3</sub> composite, respectively, at room temperature [110]. In our case, obtained value of PF was much larger than those reported, which will be discussed below.

### **5.2.5 Hall Analysis**

In order to confirm the carrier type and to determine its mobility and concentration we have performed Hall measurement on the pure and doped samples. Figs 5.4(a) and (b) show the variation of Hall resistivity as a function of applied magnetic field at different temperatures for x=0 and 0.20 samples respectively. Both samples were showing



**Fig. 5.4** (a) Magnetic field dependence of the Hall resistivity at different temperatures for  $Bi_2Te_3$  (b) Magnetic field dependence of the Hall resistivity at different temperatures for x=0.20 sample. Inset: Variation of mobility as a function of temperature for  $Bi_{2-x}Zn_xTe_3$  (x=0, 0.10, 0.20).

a negative slope of Hall Effect indicating *n* type carrier for the entire range of doping and temperature of measurement, which was also consistent with the negative S of the pure and Zn doped samples. We have determined the carrier concentration at different temperatures from the Hall data using the formula N=1/R<sub>H</sub>e, where R<sub>H</sub> is the Hall coefficient and e is the charge of electron. As the temperature was increasing N value was also increasing, which should be attributed to the increased bulk contribution. But the estimated carrier concentration was remain almost constant (~10<sup>19</sup>) upon doping which was also consistent with the reported values [49, 111]. The carrier mobility ( $\mu$ ) has been evaluated using the relation  $\mu = \frac{1}{\rho Ne}$ , where  $\rho$  is the electrical resistivity of the samples. It is clear from the inset of Fig. 5.4 (b) that mobility decreases with increasing temperature as in a typical metal. At low temperatures, the mobility first decreases for x = 0.10 and then increases substantially for x = 0.20 which is obvious from inset of Fig. 5.4(b).

#### 5.2.6 Study of magnetoresistance

Variation of magnetoresistance as a function of applied magnetic field under different temperatures are shown in Fig.5.5. Magnetoresistance (MR) of the samples has been defined as,  $MR\% = \frac{R(H) - R(0)}{R(0)} X100\%$  where R(H) is the resistance at applied magnetic field H, R(0) is the measured resistance at H=0. MR for all the samples increases with applied field but decreases with increasing temperature. A clear linear and non-saturating MR can be seen for the entire range of temperature and field of measurement for all of the samples as shown in fig. 5.5. A clear dip could be seen in the doped samples x=0.10, 0.20 [shown in inset of fig. 5.5(d)] which is not present in case of pure sample x=0. Moreover, the observed maximum

MR reaches ~400% for x=0.10 sample and is almost 16% higher than the parent (x=0) sample.

It is obvious from the MR graph that it is completely symmetric for all the undoped and doped samples with respect to the reversal of the magnetic field direction, ruling out any possible contribution from Hall voltage. Moreover, it is obvious from the MR curve that for the low doped sample (x=0.1), it is completely linear without any sign of saturation except at the very low field where a dip in MR is observed which might be due to the existence of weak antilocalization (WAL) that results from the surface state. As the Zn content increases the MR dip is broadened indicating reduction of the surface state [shown in inset of Fig. 5.5(d)]. As we increase temperature, MR becomes linear for intermediate temperature range and again at higher temperature i.e. 300K it is showing quadratic behavior. Similar type of quadratic growth behavior without any sign of saturation has been seen at high temperature in Bi<sub>2</sub>Te<sub>3</sub> films by Wang et al.[36]. As is mentioned above, the sharp resistance dip at T=2K is an indication of the presence of a weak antilocalization (WAL) effect [50,112] and as we increase temperature, MR dip broadened at low field because at higher T phase coherence length decreases [50].

To understand the origin of observed MR we have considered the theoretical models viz. quantum model by Abrikosov [35] and classical model by Parish and Littlewood (PL) [80]. According to the quantum model [35], when extreme quantum limit  $\hbar\omega_c > E_F$  is satisfied, all the electrons are condensed into one landau level where  $\hbar\omega_c$  is the cyclotron energy and  $E_F$  is the Fermi energy. But later experimental studies indicate that LMR could appear even at smaller field when electron occupies several Landau levels [58]. We have estimated the crossover field using the inequality  $n_0 \ll (\frac{e_H}{h_c})^{3/2}$  considering the carrier density of the order

of  $10^{19}$ /cm<sup>3</sup> from Hall measurement, the estimated crossover field was larger than 10T where  $n_0$  is the carrier concentration, e is the electron charge, H is the strength of applied field and c is the speed of light. But in our case we have crossover field less than 3T (estimated from dMR/dH). Moreover, according to generic quantum description of galvano-magnetic phenomenon, the longitudinal MR can be represented as  $\rho_{xx} = \rho_{yy} = \frac{N_i H}{\pi N^2 ec}$ , where  $\rho_{xx}$  and  $\rho_{yy}$ 



**Fig.5.5** (a, b, c) Normalized MR as a function of magnetic field at different temperatures  $Bi_{2-x}Zn_xTe_3$  (x=0, 0.10, 0.20). (d) Variation of mobility and MR as a function of temperature for the sample x=0.20 at low field. Inset: Variation of MR at 2K for  $Bi_{2-x}Zn_xTe_3$  (x=0, 0.10, 0.20).

Quantum MR should be linear down to very small fields and should be nonsaturating and are the transverse component of magnetoresistance,  $N_i$  is the concentration of static scattering centers, *N* is the density of electrons [35]. According to this formula resistance is inversely related to the square of the carrier concentration which is also not well matched with our experimental data. Moreover, this positive and more importantly it should be temperature independent but in our case MR is temperature independent up to 10K only and for the higher temperatures MR is strongly temperature dependent and therefore we conclude that Abrikosov quantum model may not be applicable here.

According to the classical model [80], magnitude of the fluctuations in mobility is an important factor for the origin of MR. Furthermore, in classical case it is expected that the value of crossover field shifts with the temperature, as fluctuations in mobility would dominate at higher temperatures. It is observed in Fig. 5.5(d) that both mobility and MR decrease with increase of temperature and the nature of variations are similar. This behavior is consistent with the PL model [80], hence we expect that the better explanation may be close to classical case.

From the above discussion it is clear that Zn doping enhances the bulk contribution and the bulk contribution playing the significant role in MR and also to increase the mobility. Moreover, it is very interesting that while moving from x=0.10 to x=0.20, both  $\sigma$  and S increase which is very unusual. In fact, in most cases, as S decreases  $\sigma$  increases and viceversa. The simultaneous enhancement of  $\sigma$  and S is observed in x=0.20 sample indicating that S is dominated by bulk. It is observed that up to x=0.10 the coupling between  $\sigma$  and S persists. But with further increase of doping concentration  $\sigma$  and S is decoupled. For both the cases PF increases. For the former case the enhancement of S is more effective than the decrease in  $\sigma$ . On the other hand, in the latter case both  $\sigma$  and S increase which enhance the PF significantly. In fact, the thermopower and the electrical conductivity are both intimately related with the carrier concentration and mobility. In the present investigation, it is observed that the mobility increases significantly for highest Zn doped sample [inset of Fig. 5.4(b)]. In general, in conventional semiconductors, the carrier mobility is lowered by induced defects. These defects which are produced by doping are the scattering centers. Moreover, it has already been reported that in addition to the bulk transport,  $Bi_2Te_3$  exhibits significant surface transport, which is attributed to the topological insulating state [111]. In the present case the defects (created with Zn doping) cause the unusual mobility behavior by modifying the relative contribution of conduction electrons between the bulk and the surface. With Zn doping the bulk state is enhanced in expense to the surface state than in the undoped sample where surface conduction weighs more as is clear from the MR and Hall data. Therefore, although  $\mu$  initially decreases with Zn doping, the  $\mu$  shows an increase with further doping [as shown in inset of Fig. 5.4(b)], because with doping the higher-mobility bulk conduction plays a much more significant role than the surface conduction.

The simultaneous enhancement of S and  $\sigma$  is observed only in relatively high doped samples, which suggests that the thermopower is dominated by the bulk contribution that can be tailored by the defects. In the relaxation time model, the thermopower in the degenerate doping limit is given by:

$$S = \frac{K}{e} \left(\frac{\pi^2 KT}{3\varepsilon_F}\right) \left(\frac{3}{2} + r\right)$$

Where *r* is the index of the electron relaxation time related to kinetic energy [113] and  $\varepsilon_{\rm F}$ , the Fermi energy is measured from the conduction band edge. The above equation not only predicts the ordinary decrease of S as *n* increases (through  $\varepsilon_{\rm F}$ ), but also an increase in S when *r* increases. The former leads to the conventional inverse coupling between S and  $\sigma$ , while the latter allows the decoupling of them, as seen in the present case. In fact, *r* varies from -1/2

for acoustic phonon scattering to 3/2 for ionized impurity scattering [113]. Initially for the undoped and low doped samples, the measured S follows the trend with calculation using r =-1/2, indicating that electrons are mostly scattered by phonons in these samples. This is consistent with theoretical prediction that electrical transport in Bi<sub>2</sub>Te<sub>3</sub> at similar carrier concentrations ( $\approx 1 \times 10^{19}$  cm<sup>-3</sup>) is limited by phonon scattering [114]. However, the high doping causes a transition of the scattering mechanism from phonon-dominated (r = -1/2) to impurity-dominated (r = 3/2); as a result, the thermopower is drastically enhanced. This transition is also confirmed by the fact that the mobility  $\mu$  of undoped sample increases rapidly at low temperatures, while  $\mu$  is less temperature-sensitive for doped sample. The defect induced decoupling of S and  $\sigma$  naturally leads to a significant increase in the thermoelectric power factor,  $S^2\sigma$ , as shown in the Fig. 5.3. It reaches a peak value of 4.64X  $10^{-3}$  W/K<sup>2</sup>m for x = 0.20 which is two times larger than that of the undoped Bi<sub>2</sub>Te<sub>3</sub> (2.1x10<sup>-3</sup>  $W/K^2m$ ). The value of PF reported in the present investigation in Zn doped Bi<sub>2</sub>Te<sub>3</sub> TI system is the largest to the best of our knowledge. Moreover, it is expected that the thermal conductivity will also be reduced for the highly doped samples. Therefore, a significant improvement of the thermoelectric performance can be achieved through a proper doping. Similar behavior is observed by inducing native defects in topological insulator [115].

### **5.3 Conclusions**

Electrical resistivity, magnetotransport and thermoelectric properties of  $Bi_{2-x}Zn_xTe_3$  single crystals were studied. Magnetoresistance shows the linear field dependence and with Zn content the MR value increases. The MR behavior above 10K cannot be explained with quantum model, but is consistent with the classical model. The mobility initially decreases with Zn doping but with further doping mobility increases indicating increasing contribution

of bulk in expense of surface state. For the x = 0.20 sample, the electrical conductivity and thermopower are simultaneously enhanced, leading to a significant enhancement of thermoelectric power factor.