

## LIST OF SYMBOLS

$[A]$	Coefficient matrix
$A$	Cross sectional area of the crack, normal to flow direction $x$
$a_0$	A constant which takes into account the residual opening in sinusoidal CMOD relation
$a_1, a_2, a_3, a_4$	Four of the six displacement constant of a triangular finite element
$B$	Width of dam at foundation level
$B'$	Width of dam at crack location other than foundation level
$b$	Crack opening at any distance $x$ from the crack mouth and time $t$
$\langle b \rangle$	Mean value of mechanical aperture $b$
$b_c$	A constant in exponential CMOD relation
$b_H$	Hydraulic aperture
$b_0$	Amplitude in sinusoidal CMOD relation
$b_m$	Crack mouth opening displacement (CMOD)
$b_{max}$	Maximum value CMOD
$b_{mr}$	Residual crack mouth opening displacement
$b'_{mr}$	Increased residual crack opening due dead storage in dam reservoir
$\dot{b}_m$	Crack mouth opening displacement rate (CMODrate)
$c$	Constant in CMOD rate relation
$C$	A constant in power spectrum function
$C_0$	A constant in sine hyperbolic CMOD rate equation
$C_2, C_3$	Constants in momentum equations for laminar and turbulent flow respectively

$[D]$	Coefficient matrix in linear strain-stress relation resulting from plane strain formulation
$D$	Structural size used in size effect law (SEL)
$D_h$	Hydraulic radius of the crack which is equal to $2b$
$d$	Separation distance between two reference planes used to measure crack aperture
$dA$	Infinitesimal area of control volume
$\left(\frac{dp}{dx}\right)_l$	Laminar pressure gradient
$\left(\frac{dp}{dx}\right)_t$	Turbulent pressure gradient
$E$	Elastic Modulus of concrete
$E'$	Young modulus equal to $E$ for plain stress and $E/(1 - \nu_0^2)$ for plane strain
$E_T$	Total energy of crack propagation
$dV$	Infinitesimal volume element of control volume
$\{F\}$	Force vectors
$F_i$	Force in direction of $i$
$F_s$	Factor of safety in sliding (FSS)
$F(t)$	Uplift force at any time $t$
$F_H(t)$	Horizontal hydrostatic force at upstream face of the dam.
$f$	Wave number of power spectra
$f_{ij}^{m_0}(\theta)$	Trigonometric function for crack deformation mode $m_0$ and stress $\sigma_{ij}$
$f_0(b_m)$	Function of $b_m$ used in sine hyperbolic CMOD rate equation
$G$	Crack driving force
$g$	Acceleration due of gravity
$H$	Water depth at full reservoir level (FRL)
$H_p$	Pressure head

$H_z$	Hurst exponent
$\Sigma H_0$	Summation of horizontal forces acting on the dam
$h$	Depth of crack location from full reservoir level (FRL)
$H_T$	Total head
$J$	Hydraulic gradient
$k$	A constant in exponential CMOD relation
$k_0$	A constants used in sine hyperbolic CMOD rate equation
$[k]$	Stiffness matrix
$K$	Hydraulic conductivity of crack
$K_I$	Stress intensity factor (SIF) for opening mode of the crack
$K_{IC}$	Fracture toughness
$(K_I)_P, (K_I)_M$	SIF in opening mode for prototype and model
$K_{max}$	Maximum SIF in cyclic loading
$K_{min}$	Minimum SIF in cyclic loading
$\Delta K_d$	Difference of maximum and minimum SIF values in cyclic loading
$K_n$	Normal stiffness of crack wall
$L$	Crack length
$L_H$	Crack length at dam foundation level
$L_h$	Crack length at level $h$ below FRL
$L_P, L_M$	Crack length for prototype and model
$L_s$	Stagnation length during closing phase of crack mouth
$L_{sp}$	Saturation length
$L_{spH}$	Saturation length in crack located at foundation level
$L_{sph}$	Saturation length in crack located at level $h$ below FRL.
$L_t$	Transition length, where laminar flow changes to turbulent flow

$L_{tu}$	Upstream transition length during closing phase of crack mouth
$L_{td}$	Downstream transition length during closing phase of crack mouth
$m$	Mass of water in control volume
$m_0$	Modes of crack deformation
$N$	Number of cycles in fatigue loading
$\mathbf{n}$	Outward unit normal vector on surface of control volume
$n$	Exponent in Louis (1969) momentum equation
$n_0$	Exponent in CMOD rate relation
$P(f)$	Power spectrum function of wave number $f$
$p$	Pressure as function space and time
$p_m$	Reservoir pressure at crack mouth
$p_s$	Stagnation pressure
$\{\mathbf{q}\}$	Nodal displacement vectors
$Q$	Discharge through the crack
$Q_m$	Discharge at crack mouth
$R$	Crack resistance force
$R_0$	Ratio of maximum and minimum SIF values in cyclic loading
$R_e$	Reynolds number
$T$	Time period of one opening-closing of crack walls
$T_0$	Fracture transmissivity
$\mathbf{U}$	Displacement vector
$U$	Strain energy
$u_j$	Component form of displacement vector
$(u_j, v_j)$	Horizontal and vertical displacement of a node $j$ of triangular finite element

$u_0$	One of the six displacement constant of a triangular finite element
$\mathbf{v}$	Water velocity vector
$v_0$	One of the six displacement constant of a triangular finite element
$v_x, v_y$	Velocity of fluid in $x$ and $y$ directions respectively
$v$	One dimensional velocity of water in crack
$\sum V_0(t)$	Summation of vertical forces acting on the dam (including uplift forces)
$w$	Depth of fracture
$W$	Weight of the dam
$W_s$	Work required to create new fracture surfaces
$z$	Location of crack
$z_0$	Parameter for correlation length used in crack aperture measurement
$z_1(x, y), z_2(x, y)$	Surface height functions used to measure the fracture aperture in $x - y$ plane
$\Pi$	Potential energy of crack propagation
$\alpha$	An exponent in power spectrum function
$\{\boldsymbol{\sigma}\}$	Stress tensor
$\sigma_b$	Standard deviation of mechanical aperture $b$
$\sigma_{br}$	Crack bridging stress in sine hyperbolic CMOD rate equation
$\sigma_N$	Nominal strength used in size effect law (SEL)
$\sigma_u$	Uniform boundary stress acting on the boundary for calculation of SIF
$\sigma_{uP}, \sigma_{uM}$	Uniform boundary stress acting on the boundary for calculation of SIF for prototype and model respectively
$\sigma_{ij}$	Stresses in the direction of $j$ on plane normal to $i$
$\delta_{ij}$	Kronecker delta

$\rho$	Density of water
$\varepsilon$	Average asperity height or absolute roughness of crack walls
$\epsilon$	Strain tensor
$\mu, \lambda$	Lame constants
$\lambda_0$	Ratio of crack lengths of prototype and model
$\mu_0$	Friction coefficient in sliding
$\epsilon_{ij}$	Indicial form of strain tensor
$\gamma$	Unit weight of water
$\omega$	Circular frequency of crack opening- closing cycle
$\omega_0$	Numerical correction factor that takes into account loading conditions, boundary conditions, and specimen geometry in calculation of SIF
$\omega_{0P}$	Numerical correction factor used in calculation of SIF for prototype and model respectively
$\theta$	Phase angle in sinusoidal CMOD relation
$\nu$	Kinematic viscosity of water
$\nu_0$	Poisson ratio