

Appendix A:

At $y=0$ $A_n(\xi)=B_n(\xi)+C_n(\xi)$

and $A_n(\xi)=\frac{\mu_0 \chi}{\mu_1 \eta} [B_n(\xi)+C_n(\xi)]$

$$B_n(\xi)=\frac{A_n(\xi)}{2} \left[1 + \frac{\mu_1 \eta}{\mu_0 \chi} \right]$$

$$C_n(\xi)=\frac{A_n(\xi)}{2} \left[1 - \frac{\mu_1 \eta}{\mu_0 \chi} \right]$$

At $y=c$ $D_n(\xi)e^{\gamma c}+E_n(\xi)e^{-\gamma c}=B_n(\xi)e^{\chi c}+C_n(\xi)e^{-\chi c}$

$$D_n(\xi)e^{\gamma c}-E_n(\xi)e^{-\gamma c}=\frac{\mu_2 \chi}{\mu_1 \gamma} [B_n(\xi)e^{\chi c}+C_n(\xi)e^{-\chi c}]$$

$$D_n(\xi)=\frac{A_n(\xi)}{2} e^{\gamma c} \left[\cosh \chi c + \frac{\mu_2 \chi}{\mu_1 \gamma} \sinh \chi c + \frac{\mu_1 \eta}{\mu_0 \chi} \sinh \chi c + \frac{\mu_2 \eta}{\mu_0 \gamma} \cosh \chi c \right]$$

$$E_n(\xi)=\frac{A_n(\xi)}{2} e^{-\gamma c} \left[\cosh \chi c - \frac{\mu_2 \chi}{\mu_1 \gamma} \sinh \chi c + \frac{\mu_1 \eta}{\mu_0 \chi} \sinh \chi c - \frac{\mu_2 \eta}{\mu_0 \gamma} \cosh \chi c \right]$$

At $y=b$,

$$F_n(\xi)e^{\eta b}+I_n(\xi)e^{-\eta b}=D_n(\xi)e^{\gamma b}+E_n(\xi)e^{-\gamma b}$$

$$F_n(\xi)e^{\eta b}-I_n(\xi)e^{-\eta b}=\frac{\mu_0}{\eta} J_2(\xi) + \frac{\mu_0 \gamma}{\mu_2 \eta} [D_n(\xi)e^{\gamma b}-E_n(\xi)e^{-\gamma b}]$$

$$F_n(\xi) = \frac{\mu_0}{2\eta} J_2(\xi) e^{\eta b} + \frac{A_n(\xi)}{2} e^{\eta b} \left[\begin{array}{l} \cosh\chi c \cosh\gamma(b-c) + \frac{\mu_2 \chi}{\mu_1 \gamma} \sinh\chi c \sinh\gamma(b-c) + \\ \frac{\mu_1 \eta}{\mu_0 \chi} \sinh\chi c \cosh\gamma(b-c) + \frac{\mu_2 \eta}{\mu_0 \gamma} \cosh\chi c \sinh\gamma(b-c) \\ + \frac{\mu_0 \gamma}{\mu_2 \eta} \cosh\chi c \sinh\gamma(b-c) + \frac{\mu_0 \chi}{\mu_1 \eta} \sinh\chi c \cosh\gamma(b-c) \\ + \frac{\mu_1 \gamma}{\mu_2 \chi} \sinh\chi c \sinh\gamma(b-c) + \cosh\chi c \cosh\gamma(b-c) \end{array} \right]$$

$$I_n(\xi) = -\frac{\mu_0}{2\eta} J_2(\xi) e^{\eta b} + \frac{A_n(\xi)}{2} e^{\eta b} \left[\begin{array}{l} \cosh\chi c \cosh\gamma(b-c) + \frac{\mu_2 \chi}{\mu_1 \gamma} \sinh\chi c \sinh\gamma(b-c) + \\ \frac{\mu_1 \eta}{\mu_0 \chi} \sinh\chi c \cosh\gamma(b-c) + \frac{\mu_2 \eta}{\mu_0 \gamma} \cosh\chi c \sinh\gamma(b-c) \\ - \frac{\mu_0 \gamma}{\mu_2 \eta} \cosh\chi c \sinh\gamma(b-c) - \frac{\mu_0 \chi}{\mu_1 \eta} \sinh\chi c \cosh\gamma(b-c) \\ - \frac{\mu_1 \gamma}{\mu_2 \chi} \sinh\chi c \sinh\gamma(b-c) - \cosh\chi c \cosh\gamma(b-c) \end{array} \right]$$

At $y=a$ $-\frac{\eta}{\mu_0} [F_n(\xi) e^{\eta a} - I_n(\xi) e^{-\eta a}] = -J_1(\xi)$

$$K(\xi) = \left[\frac{\mu_1 \xi}{\mu_0 \chi} \sinh\chi c \cdot \cosh\gamma(b-c) \cdot \sinh\xi(a-b) + \frac{\mu_3 \chi}{\mu_1 \xi} \sinh\chi c \cdot \cosh\gamma(b-c) \cdot \cosh\xi(a-b) \right. \\ \left. + \frac{\mu_2 \chi}{\mu_1 \gamma} \sinh\chi c \cdot \sinh\gamma(b-c) \cdot \sinh\xi(a-b) + \frac{\mu_3 \mu_1 \gamma}{\mu_0 \mu_2 \chi} \sinh\chi c \cdot \sinh\gamma(b-c) \cdot \cosh\xi(a-b) \right. \\ \left. + \frac{\mu_3}{\mu_0} \cosh\chi c \cdot \cosh\gamma(b-c) \cdot \cosh\xi(a-b) + \frac{\mu_2 \xi}{\mu_0 \gamma} \cosh\chi c \cdot \sinh\gamma(b-c) \cdot \sinh\xi(a-b) \right. \\ \left. + \cosh\chi c \cdot \cosh\gamma(b-c) \cdot \sinh\xi(a-b) + \frac{\mu_3 \gamma}{\mu_2 \xi} \cosh\chi c \cdot \sinh\gamma(b-c) \cdot \cosh\xi(a-b) \right]$$

$$W(\xi, a) = \left[me^{\pm j0.5k\tau} \sinh\xi(a-b) K(\xi) \right] - \left[1 + me^{\pm j0.5k\tau} \cosh\xi(a-b) \right]$$

$$\left[\frac{\mu_2 \chi}{\mu_1 \gamma} \sinh\chi c \cdot \sinh\gamma(b-c) \cdot \cosh\xi(a-b) + \frac{\mu_3 \mu_1 \gamma}{\mu_0 \mu_2 \chi} \sinh\chi c \cdot \sinh\gamma(b-c) \cdot \sinh\xi(a-b) \right]$$

$$\begin{aligned}
 & + \frac{\mu_1 \xi}{\mu_0 \chi} \sinh \chi c \cdot \cosh \gamma (b-c) \cdot \cosh \xi (a-b) + \frac{\mu_3 \gamma}{\mu_1 \xi} \sinh \chi c \cdot \cosh \gamma (b-c) \cdot \sinh \xi (a-b) \\
 & + \cosh \chi c \cdot \cosh \gamma (b-c) \cdot \cosh \xi (a-b) + \frac{\mu_3}{\mu_0} \cosh \chi c \cdot \cosh \gamma (b-c) \cdot \sinh \xi (a-b) \\
 & + \frac{\mu_2 \xi}{\mu_0 \gamma} \cosh \chi c \cdot \sinh \gamma (b-c) \cdot \cosh \xi (a-b) + \frac{\mu_3 \gamma}{\mu_2 \xi} \cosh \chi c \cdot \sinh \gamma (b-c) \cdot \sinh \xi (a-b)]
 \end{aligned}$$

$$\begin{aligned}
 H(\xi) = & [\cosh \gamma d \cosh \xi (c-d) \cosh \chi (b-c) \sinh \chi (a-b) + \frac{\gamma}{\xi} \sinh \gamma d \sinh \xi (c-d) \cosh \chi (b-c) \sinh \chi (a-b) \\
 & + \frac{\xi}{\gamma} \sinh \gamma d \cosh \xi (c-d) \cosh \chi (b-c) \sinh \chi (a-b) + \cosh \gamma d \sinh \xi (c-d) \cosh \chi (b-c) \sinh \chi (a-b) \\
 & + \frac{\mu_4 \xi}{\mu_0 \chi} \cosh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \sinh \chi (a-b) + \frac{\mu_4 \gamma}{\mu_0 \chi} \sinh \gamma d \cosh \xi (c-d) \sinh \chi (b-c) \sinh \chi (a-b) \\
 & + \frac{\xi^2}{\gamma \chi} \frac{\mu_4}{\mu_0} \sinh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \sinh \chi (a-b) + \frac{\mu_4 \xi}{\mu_0 \chi} \cosh \gamma d \cosh \xi (c-d) \sinh \chi (b-c) \sinh \chi (a-b) \\
 & + \frac{\mu_5}{\mu_4} \cosh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \cosh \chi (a-b) + \frac{\gamma}{\xi} \frac{\mu_5}{\mu_4} \sinh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \sinh \chi (a-b) \\
 & + \frac{\mu_5 \xi}{\mu_4 \gamma} \sinh \gamma d \cosh \xi (c-d) \sinh \chi (b-c) \cosh \chi (a-b) + \frac{\mu_5}{\mu_4} \cosh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \cosh \chi (a-b) \\
 & + \frac{\mu_5 \xi}{\mu_0 \chi} \cosh \gamma d \sinh \xi (c-d) \cosh \chi (b-c) \cosh \chi (a-b) + \frac{\mu_5 \gamma}{\mu_0 \chi} \sinh \gamma d \cosh \xi (c-d) \cosh \chi (b-c) \cosh \chi (a-b) \\
 & + \frac{\xi^2}{\gamma \chi} \frac{\mu_5}{\mu_0} \sinh \gamma d \sinh \xi (c-d) \cosh \chi (b-c) \cosh \chi (a-b) + \frac{\mu_5 \xi}{\mu_0 \chi} \cosh \gamma d \cosh \xi (c-d) \cosh \chi (b-c) \cosh \chi (a-b)]
 \end{aligned}$$

$$\begin{aligned}
 G(\xi, a) = & [\cosh \gamma d \cosh \xi (c-d) \cosh \chi (b-c) \cosh \chi (a-b) + \frac{\gamma}{\xi} \sinh \gamma d \sinh \xi (c-d) \cosh \chi (b-c) \cosh \chi (a-b) \\
 & + \frac{\xi}{\gamma} \sinh \gamma d \cosh \xi (c-d) \cosh \chi (b-c) \cosh \chi (a-b) + \cosh \gamma d \sinh \xi (c-d) \cosh \chi (b-c) \cosh \chi (a-b) \\
 & + \frac{\mu_4 \xi}{\mu_0 \chi} \cosh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \cosh \chi (a-b) + \frac{\mu_4 \gamma}{\mu_0 \chi} \sinh \gamma d \cosh \xi (c-d) \sinh \chi (b-c) \cosh \chi (a-b) \\
 & + \frac{\xi^2}{\gamma \chi} \frac{\mu_4}{\mu_0} \sinh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \cosh \chi (a-b) + \frac{\mu_4 \xi}{\mu_0 \chi} \cosh \gamma d \cosh \xi (c-d) \sinh \chi (b-c) \cosh \chi (a-b) \\
 & + \frac{\mu_5}{\mu_4} \cosh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \sinh \chi (a-b) + \frac{\gamma}{\xi} \frac{\mu_5}{\mu_4} \sinh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \cosh \chi (a-b) \\
 & + \frac{\mu_5 \xi}{\mu_4 \gamma} \sinh \gamma d \cosh \xi (c-d) \sinh \chi (b-c) \sinh \chi (a-b) + \frac{\mu_5}{\mu_4} \cosh \gamma d \sinh \xi (c-d) \sinh \chi (b-c) \sinh \chi (a-b) \\
 & + \frac{\mu_5 \xi}{\mu_0 \chi} \cosh \gamma d \sinh \xi (c-d) \cosh \chi (b-c) \sinh \chi (a-b) + \frac{\mu_5 \gamma}{\mu_0 \chi} \sinh \gamma d \cosh \xi (c-d) \cosh \chi (b-c) \sinh \chi (a-b) \\
 & + \frac{\xi^2}{\gamma \chi} \frac{\mu_5}{\mu_0} \sinh \gamma d \sinh \xi (c-d) \cosh \chi (b-c) \sinh \chi (a-b) + \frac{\mu_5 \xi}{\mu_0 \chi} \cosh \gamma d \cosh \xi (c-d) \cosh \chi (b-c) \sinh \chi (a-b)]
 \end{aligned}$$

Appendix B:

Table B.1 Details of POPAMPs LM675 and LM3886

Parameters	LM3886 [Datasheet, LM3886]	LM675 [Datasheet, LM675]
Supply Voltage ($V^+ + V^-$)	84V	30 V
Differential Input Voltage	60V	16V to 60V
Output Current	7A to 11A	3A max
Temperature Range	-20°C to +85°C	0°C to +70°C
Input Bias Current	1 μ A	2 μ A
Open Loop Voltage Gain	90dB	90dB

Appendix C: Flow Chart of the Performance and Electromagnetic Field Calculation