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## **List of Acronyms**

FOC Fractional Order Control

PID Proportional Integral and Derivative

FOPID Fractional Order Proportional Integral and Derivative

FOPI Fractional Order Proportional and Integral

CRONE Commande Robuste d'Ordre Non-Entier

NINTEGER Non-Integer

FOMCON Fractional Order Modeling and Control

TID Tilted Integral and Derivative

FO[PD] Fractional Order of Proportional and Derivative

FO[PI] Fractional Order of Proportional and Integral

IMC Internal Model Control

TE Trial and Error

ZN Ziegler and Nichols

NM Nelder's Mead

GWO Grey Wolf Optimizer

MGWO Modified Grey Wolf Optimizer

PSO Particle Swarm Optimization

GA Genetic Algorithm

PWM Pulse Width Modulation

ITAE Integral Time Weighted Absolute Error

IAE Integral of Absolute Error

ISE Integral of Squire Error

ITSE Integral Time Weighted Squire Error

RT Rise-time

ST Settling-time

MP Peak Overshoot

GM Gain Margin

PM Phase Margin

AVR Automatic Voltage Regulator

STS Spherical Tank System

NMP Non-minimum Phase System

MLS Magnetic Levitation System

RLM Root Locus Method

AGC Automatic Generation Control

FPAA Field Programmable Analog Array

IR Infra Red

SOM Symmetrical Optimum

MIGO MS Constrained Integral Gain Optimization

DE Differential Evolution

IEMGA Improved Electromagnetism-Like Algorithm with Genetic

Algorithm

IMC Internal Model Control

ZN Ziegler-Nichol's

FOILC Fractional Order Iterative Learning Controller

GUI Graphical User Interface

## **List of Symbols**

n Positive Integer  $\Re^+$ Positive real Number Fractional power greater than zero t,TTime in second Γ Gamma function  $E_{\varsigma}$ Millage-Leffler function Fractional parameter  $\varsigma, \tau$  $v, m, \theta$ Order of fraction derivative Angular frequency w Laplace of a function LLaplace domain Real constant  $\alpha, \sigma$ Gain coefficient of tilted controller  $T_D$ i, KPositive integer constant  $K_{P}$ Proportional gain constant  $K_{I}$ Integral gain constant  $K_D$ Derivative gain constant λ Fractional power of integral term Fractional power of derivative term μ Error eSecond level of hierarchy of the grey wolves β δ Third level of hierarchy of the grey wolves Initialization of summation k Infinite  $\infty$ Lower frequency bound  $W_b$ Higher frequency bound  $W_h$ 

$b_{\scriptscriptstyle m}$	Coefficient of numerator polynomial in generalized fractional order
	transfer function
$a_{n}$	Coefficient of numerator polynomial generalized fractional order transfer
	function
U(s)	Laplace transform of Input in fractional order transfer function
Y(s)	Laplace transform of output in fractional order transfer function
E,F	Input matrix in state-space representation of fractional order system
G,H	Output matrix in state-space representation of fractional order system
Ψ	Represents a plane
$\phi$	Angle in $\psi$ – plane
$\pi$	Angle in radians
$R_e$	Real axis
$I_{m}$	Imaginary axis
$V_n$	$n^{th}$ vertex of simplex
$\mathcal{V}_{centroid}$	Vertex of centroid
$\mathcal{V}_{reflect}$	Reflected vertex
l	Coefficient of reflection
ρ	Coefficient of expansion
ð	Coefficient of contraction
$\eta$	Coefficient of shrinking